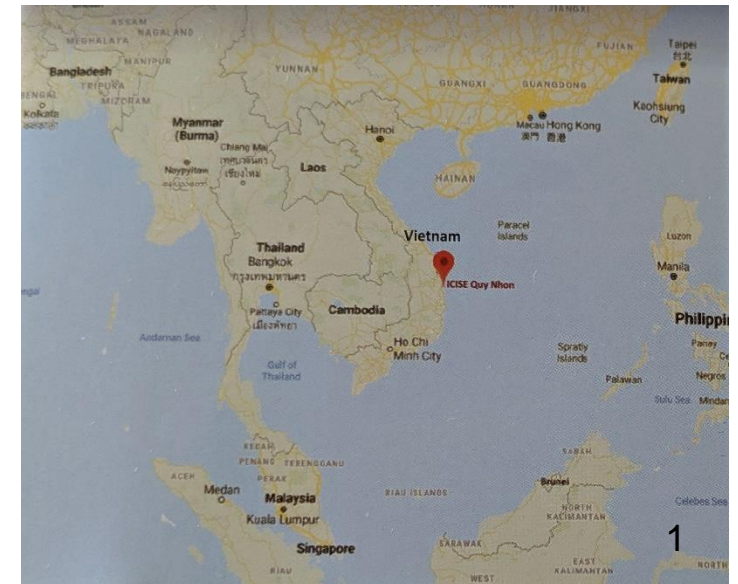


Interstellar and Intergalactic Medium

1. Overview
 2. Gas and dust
 3. Star Formation
-

Wen-Ping CHEN
National Central University
Taiwan

VSOA9 2025 July 07~12 @ Quy Nhon, Vietnam



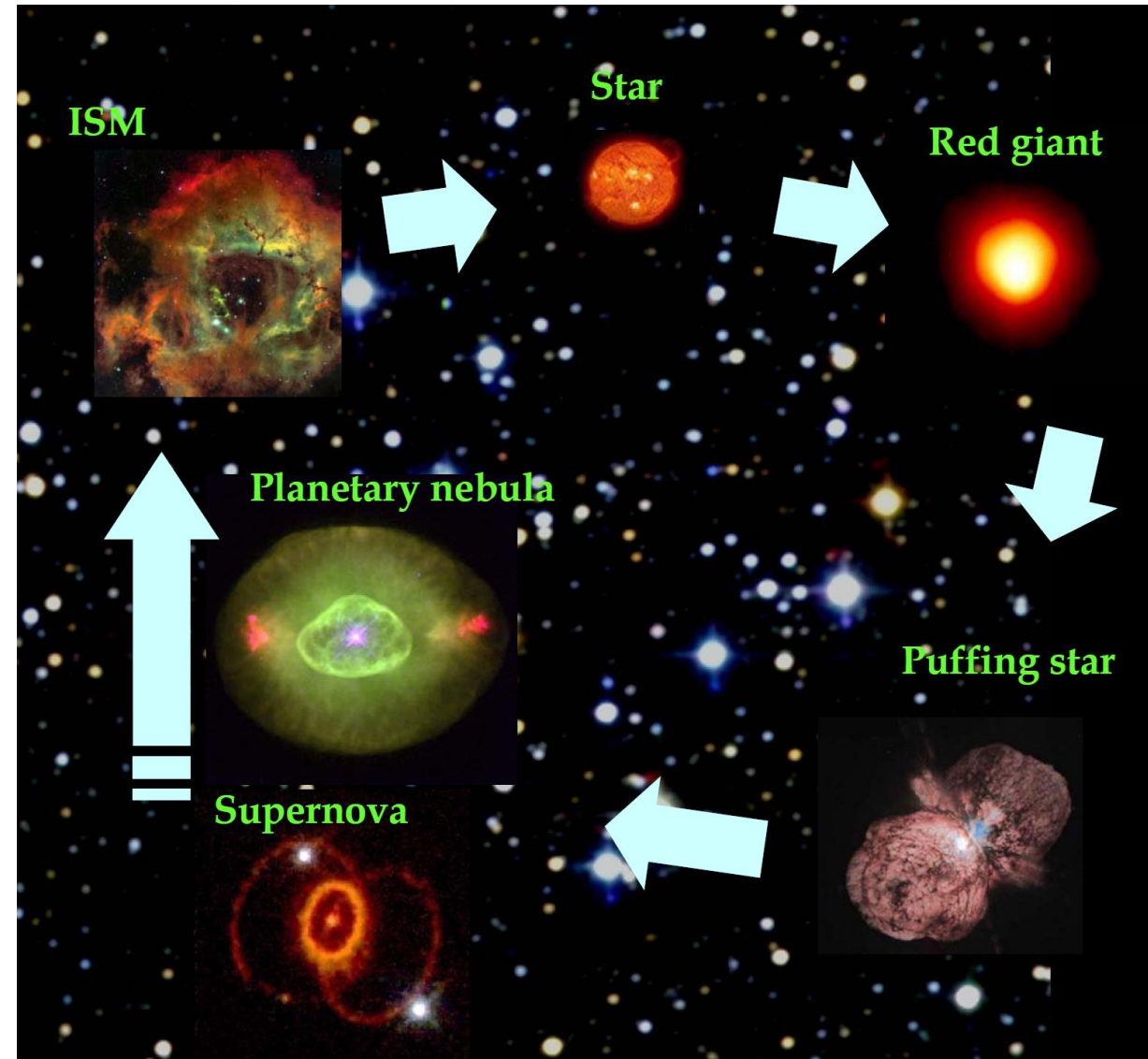
Interstellar Medium and Radiation

<http://www.astro.ncu.edu.tw/~wchen/Courses/ISM/index.htm>

Space is not completely empty, but filled with **interstellar medium** (ISM) of various format (*atomic, molecular, ionized*) under drastically different conditions (*temperature, pressure, density, etc.*) cf. IGM, ICM

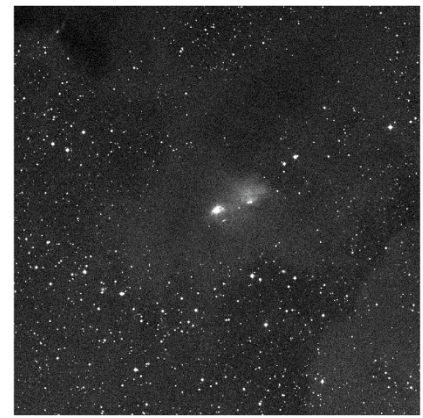
Stars are formed out of, and continue to interact with, the ISM.

When stars end their lives, they return enriched “complex” stellar matter back to the ISM, with which the next generation of stars (and planets) are formed.



Discovery of the Interstellar Medium

- 1811 William Herschel: “*holes in the starry sky*”
- 1904 J. F. Hartmann “*stationary*” calcium lines in the spectroscopic binary δ Orionis \rightarrow of interstellar origin
- 1919 E. E. Barnard catalog of dark nebulae
- Photography \rightarrow emission and reflection nebulae; dark clouds
- 1926 Sir Arthur Eddington lectured “*Diffuse Matter in Space*”
- 1927 Otto Struve “Interstellar Calcium”
- 1930 Robert J. Trumpler: absorption \nearrow as distance \nearrow
 \rightarrow beginning of ISM as a new branch of astronomy



1904

INVESTIGATIONS ON THE SPECTRUM AND ORBIT OF δ ORIONIS.¹

By J. HARTMANN.

ONE of the first results obtained by M. Deslandres with the new spectrograph attached to the 62 cm refractor of the observatory at Meudon was the discovery of the "oscillation" of δ *Orionis*. I use the term "oscillation" in place of the ponderous expression "variability of velocity in the line of sight;" but the idea of oscillation is still somewhat broader, as it includes every sort of periodic variation in the spectrum, without saying anything as to its explanation.

After the publication² of the discovery mentioned, which was communicated to the Paris Academy on February 12, 1900, Director Vogel instructed the observers in the field of stellar spectroscopy at Potsdam to undertake to confirm the interesting phenomenon, and the observations made with the four different spectrographs then in use here proved beyond a doubt that δ *Orionis* belongs to the number of oscillating stars. A confirmation of the discovery was also given by three observations by Wright with the Mills spectrograph of the Lick Observatory.

Deslandres derived from his eleven observations a period of 1.92 days, and concluded that the orbit was very eccentric. The observations which I made at that time with the large Spectrograph III (with three prisms) attached to the 80 cm refractor could not, however, be brought into accord with that length of period; and since the measures showed that the star could be more advantageously observed with low dispersion, on account of the extreme diffuseness of its lines, I included it in the program of Spectrograph I (with only one prism). With this

THE ASTROPHYSICAL JOURNAL

AN INTERNATIONAL REVIEW OF SPECTROSCOPY
AND ASTRONOMICAL PHYSICS

VOLUME XLIX

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NUMBER I

PLATE I

ON THE DARK MARKINGS OF THE SKY

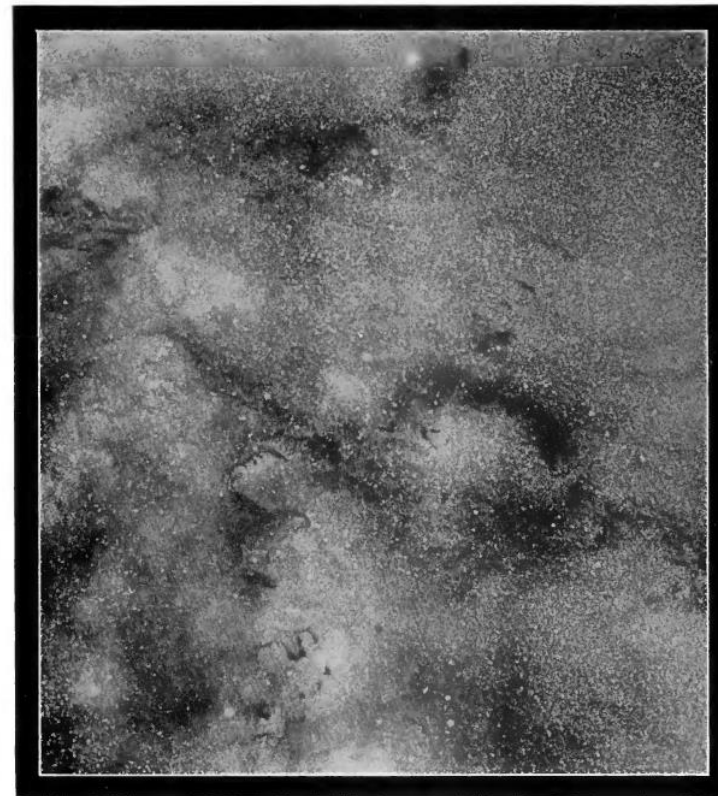
WITH A CATALOGUE OF 182 SUCH OBJECTS

By E. E. BARNARD

It would be unwise to assume that all the dark places shown on photographs of the sky are due to intervening opaque masses between us and the stars. In a considerable number of cases no other explanation seems possible, but some of them are doubtless only vacancies.

1919

North



REGION NORTH OF THETA OPHIUCHI

$\alpha = 17^h 13^m$, $\delta = -21^\circ 0'$

Scale: $1^{mm} = 234''$

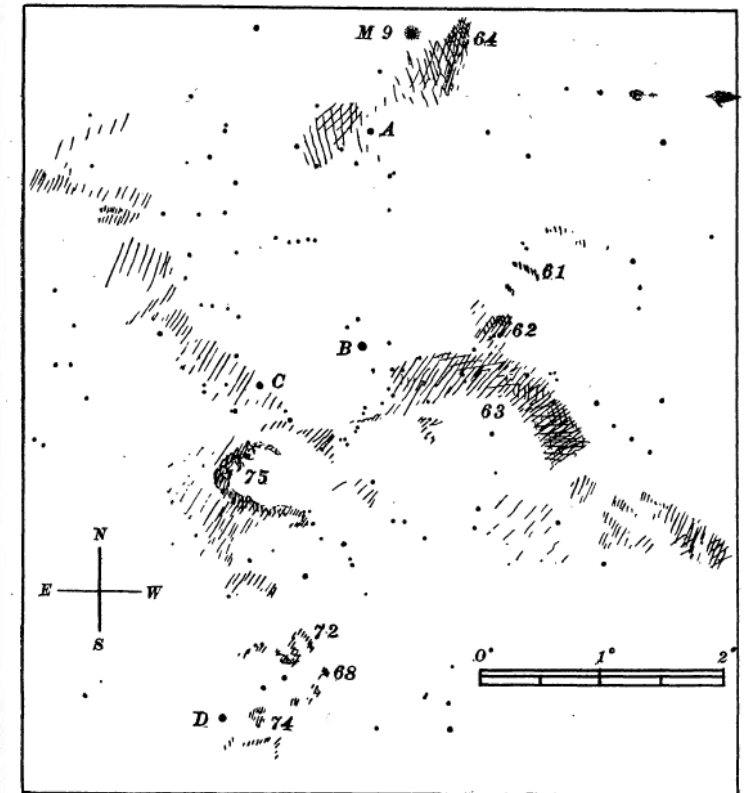


FIG. 2.—Sketch map of Plate I

- ◆ The air we breathe: 10^{19} molecules per cc.
- ◆ A typical diffuse ISM cloud: 1 particle per cc.
- ◆ This includes gas and dust. No liquid (why not?)
- ◆ Mutual gravitational force brings them closer together → denser

Gas remains transparent, but dust (grains) blocks background luminous sources.

- ◆ These “dark clouds” are dense ($10^4/\text{cm}^3$) and cold (a few K or -260°C) ; seen silhouetted

Barnard 72 in Ophiuchus



<http://www.robgendlerastropics.com/B72JMM.jpg>



Star Shadows Remote Observatory

Horsehead Nebula



Hubble
Heritage

NASA, ESA, and The Hubble Heritage Team (STScI/AURA) • Hubble Space Telescope WFPC2 • STScI-PRC01-12

(Bok) Globules silhouetted
against emission nebulosity



© Anglo-Australian Observatory

Photograph by David Malin

A dark cloud core seen
against a star field

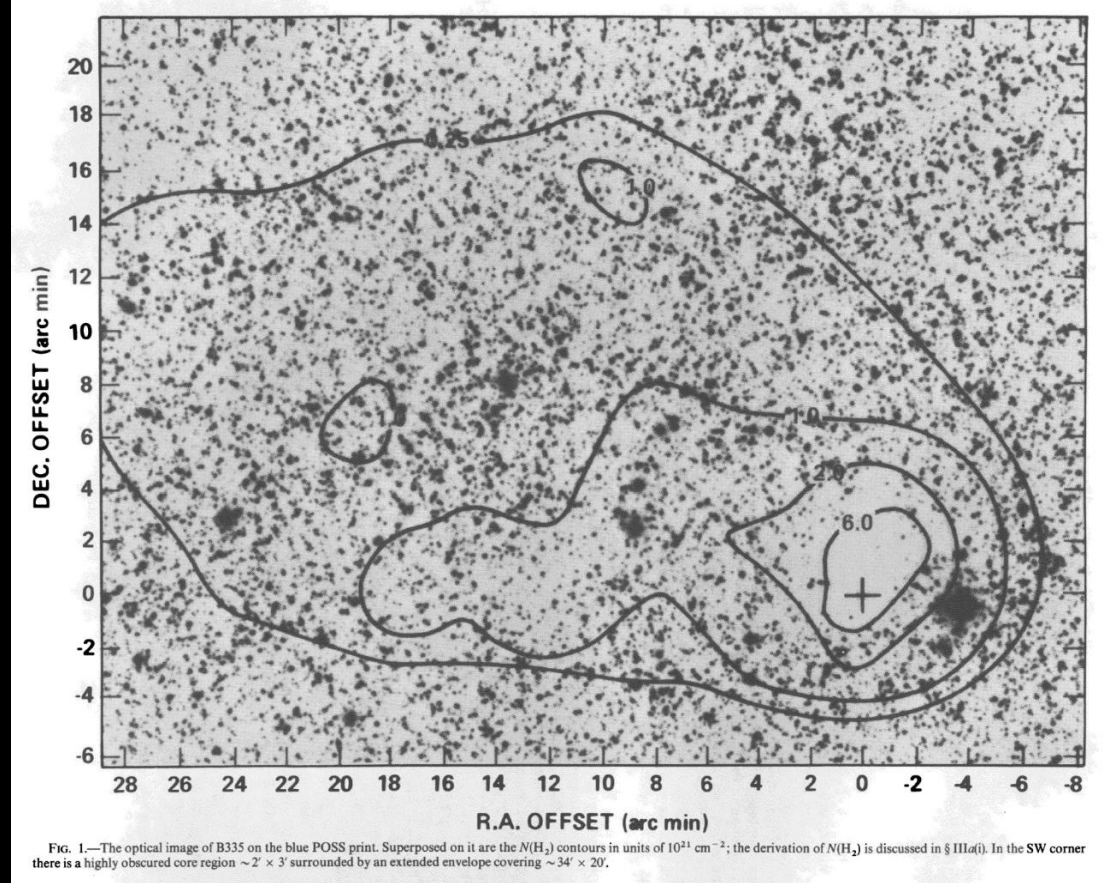


FIG. 1.—The optical image of B335 on the blue POSS print. Superposed on it are the $N(\text{H}_2)$ contours in units of 10^{21} cm^{-2} ; the derivation of $N(\text{H}_2)$ is discussed in § IIIa(i). In the SW corner there is a highly obscured core region $\sim 2' \times 3'$ surrounded by an extended envelope covering $\sim 34' \times 20'$.

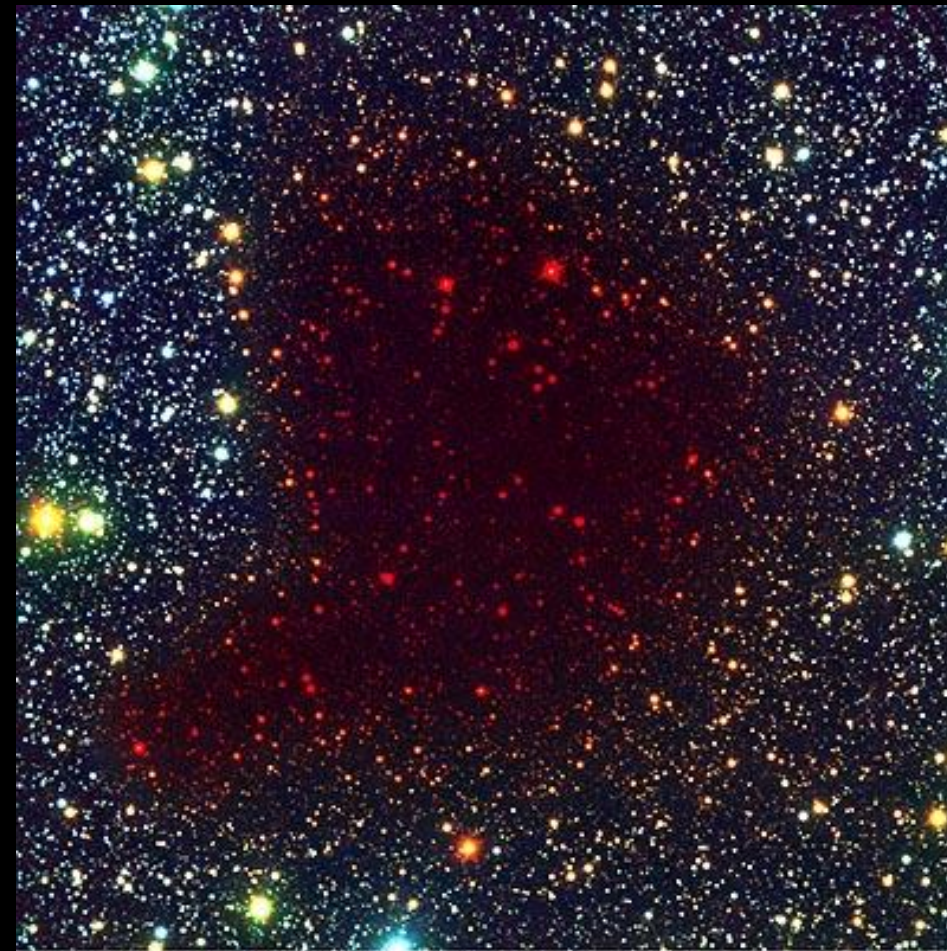
Frerking et al. (1987)

Optical Composite



Pre-Collapse Black Cloud B68 (visual view)
(VLT ANTU + FORS 1)

Optical/IR composite



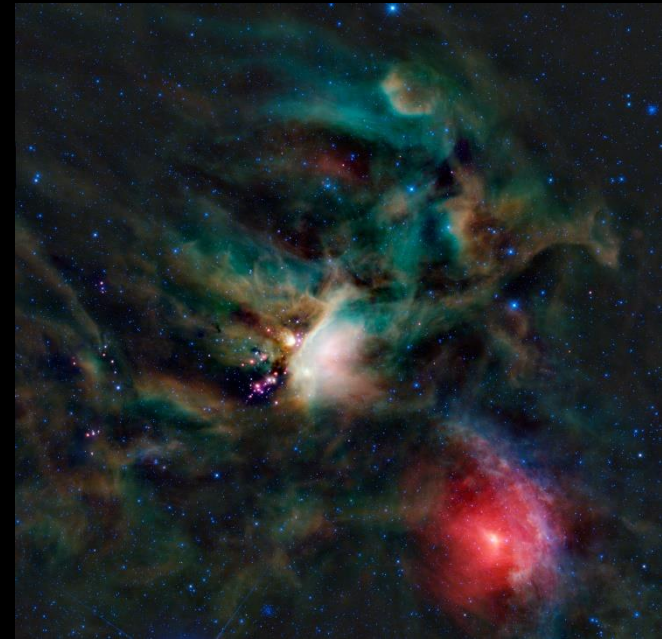
Seeing Through the Pre-Collapse Black Cloud B68
(VLT ANTU + FORS 1 - NTT + SOFI)

ρ Ophiuchi cloud complex

Visible



Infrared



WISE

Interstellar Medium (ISM)

- ISM very sparse --- gas and dust (solid)

[star-star distance] / [stellar diameter] *Parsec (pc): a unit of distance, about 3.26 ly or 3×10^{16} m*
 $\sim 1 \text{ pc} / 10^{11} \text{ cm} \sim 3 \times 10^7 : 1$; in terms of volume (space) $\sim 10^{22}$

(What about galaxies?)

➔ Stars truly tiny compared to space in between

- Mass: [gas + dust] / total $\sim 10\%$, but density very low

(What is the number density of air in this room?

Of the solar atmosphere?)

- **Milky Way galaxy**: stars/planets, gas, dust, radiation, magnetic fields, cosmic rays (i.e., charged particles)
- ISM mass = 10% of the total visible matter of the MW galaxy
- Of the ISM: 99% mass in gas, 1% in dust
- Of the gas: 90% H; 10% He
- Hydrogen: **mainly H I (atomic), H II (ionized), and H₂ (molecular)**
- Studies of ISM ---
 - Beginning of evolution of baryonic matter “recombination”
 - Stars form out of ISM
 - Important ingredient of a galaxy

*“gas-to-dust ratio” ≈ 100
nominally, but ...*

H⁰, neutral

H⁺, singly ionized

e.g., He III, Fe XXVI

Table 1.2 Mass of H II, H I, and H₂ in the Milky Way ($R < 20$ kpc)

Phase	$M(10^9 M_{\odot})$	fraction	Note
Total H II (not including He)	1.12	23%	see Chapter 11
Total H I (not including He)	2.9	60%	see Chapter 29
Total H ₂ (not including He)	0.84	17%	see Chapter 32
Total H II, H I and H₂ (not including He)	4.9		
Total gas (including He)	6.7		

Material Constituents of the ISM

Name	T (K)	n (cm ⁻³)	Properties
Hot, intercloud and “coronal” gas	10^6	10^{-4}	
Warm intercloud gas	10^4	10^{-1}	
Diffuse cloud (H I)	10^2	$10^{-1} - 1$	Mostly H I; $n_e/n_0 \approx 10^{-4}$
H II regions	10^4	>10	
Dark Molecular Clouds	10	$> 10^3$	Mostly H ₂ and dust
Supernova Remnants	$10^4 \sim 10^7$	>1	
Planetary Nebulae			

Energy Density in the Local ISM

Component	u (eV/cm ⁻³)	Properties
Cosmic microwave background	0.265	$T_{\text{CMB}} = 2.725$ K
FIR radiation from dust	0.31	
Starlight	0.54	$h\nu < 13.6$ eV
Thermal kinetic energy	0.49	
Turbulent kinetic energy	0.22	$\langle n_H \rangle = 1$ cm ⁻³
Magnetic field	0.89	$B^2/8\pi$; $\langle B \rangle = \mu\text{G}$
Cosmic rays	1.39	

There seems to be equipartition between these energies. Why?

A SMALL CLOUD

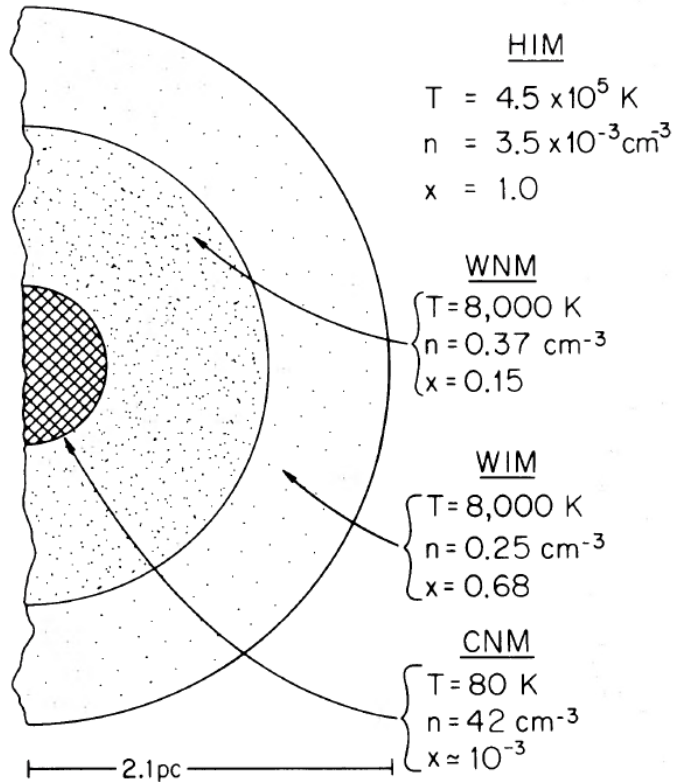
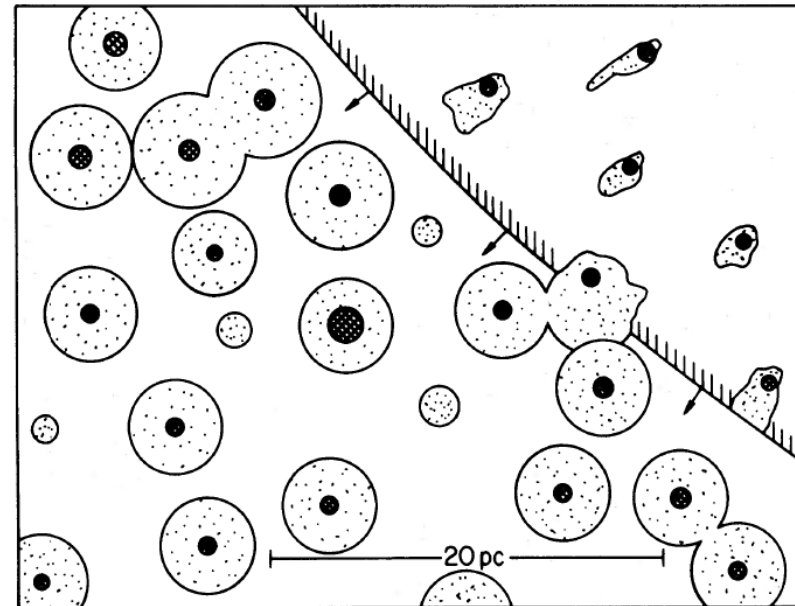


FIG. 1

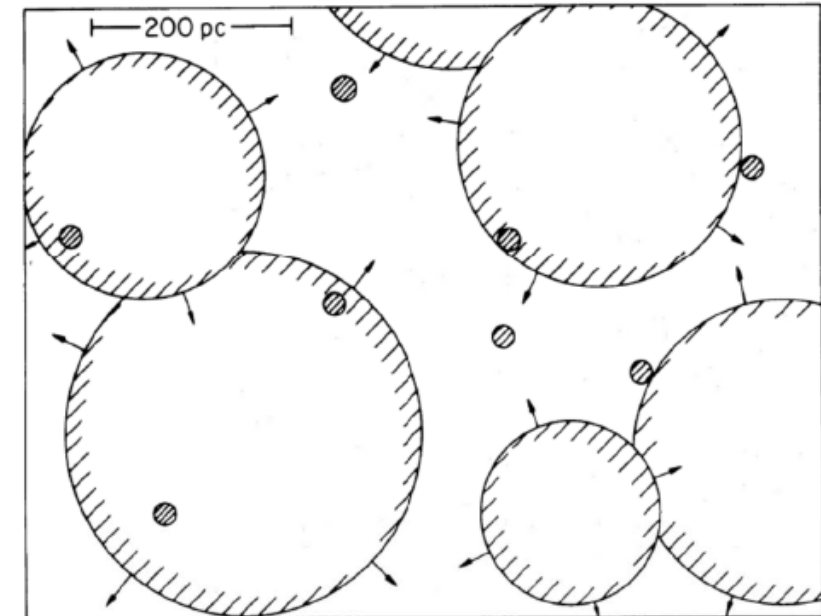
Zooming out from Fig. 1



A CLOSE UP VIEW

FIG. 2

Zooming out further from Fig. 2



A LARGE SCALE VIEW

$600 \times 800 \text{ pc}$

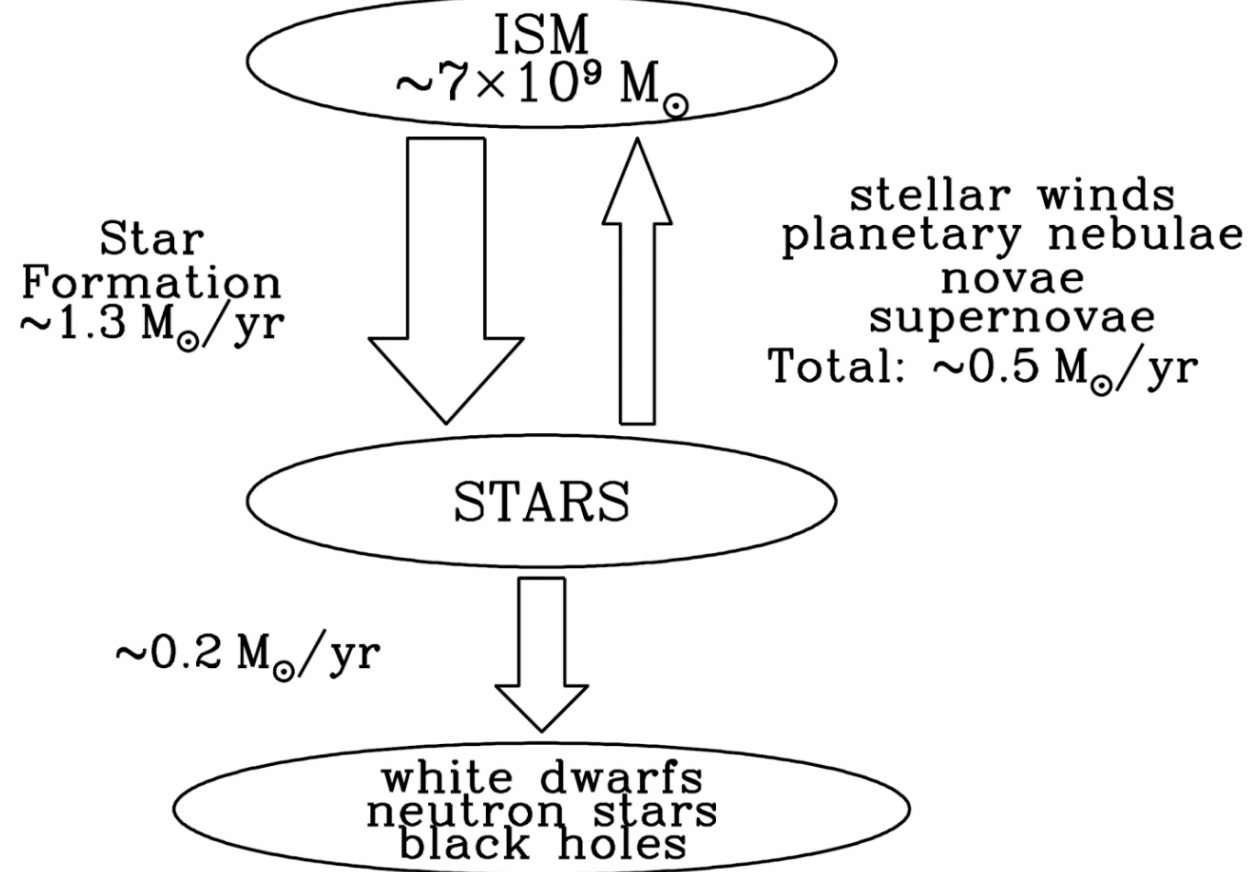
FIG. 1.—Cross section of a characteristic small cloud. The crosshatched region shows the cold core, which gives the usual optical absorption lines. Next is the warm neutral medium (WNM) with ionization produced by soft X-ray background. The outer layer (WIM) is gas largely ionized by stellar UV background. Typical values of hydrogen density n , temperature T , and ionization $x = n_e/n$ are shown for each component, except that a higher than average value of the soft X-ray flux has been assumed in order to produce a significant amount of WNM at this pressure.

FIG. 2.—Small-scale structure of the interstellar medium. A cross section of a representative region $30 \text{ pc} \times 40 \text{ pc}$ in extent is shown, with the area of the features being approximately proportional to their filling factors. A supernova blast wave is expanding into the region from the upper right. The radius of the neutral cores of the clouds (represented by crosshatching) ranges from about 0.4 to 1 pc in this small region; all the clouds with cores have warm envelopes (dotted regions) of radius $a_w \sim 2.1 \text{ pc}$. A few clouds are too small to have cores. The envelopes of clouds inside the SNR are compressed and distorted.

From the intergalactic medium

Infall
 $\sim 0.5 M_{\odot}/\text{yr}$

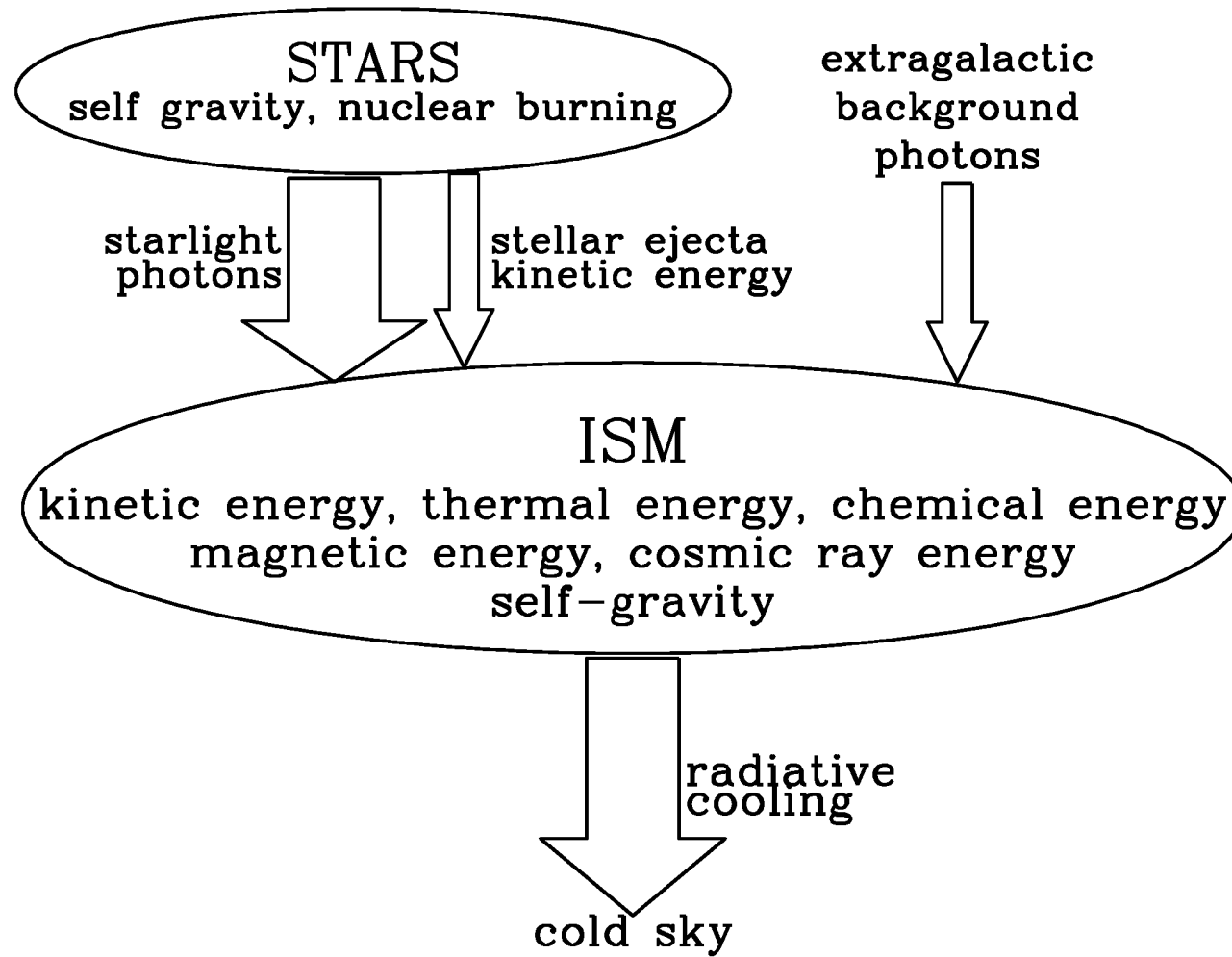
To the intergalactic medium;
galactic winds; tidal stripping



Flow of baryons in the Milky Way galaxy

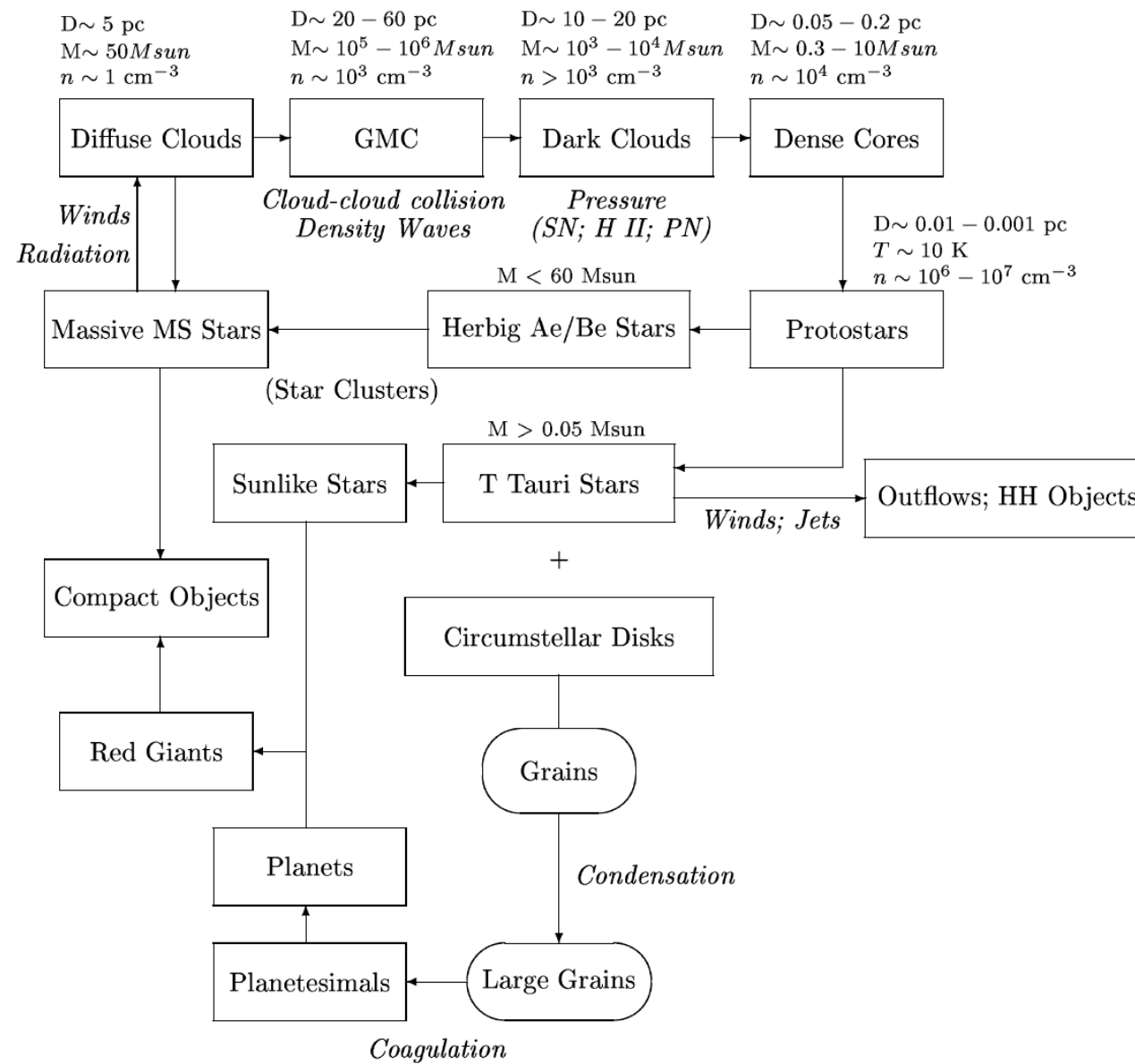
Draine

The ISM is far from thermodynamic equilibrium.

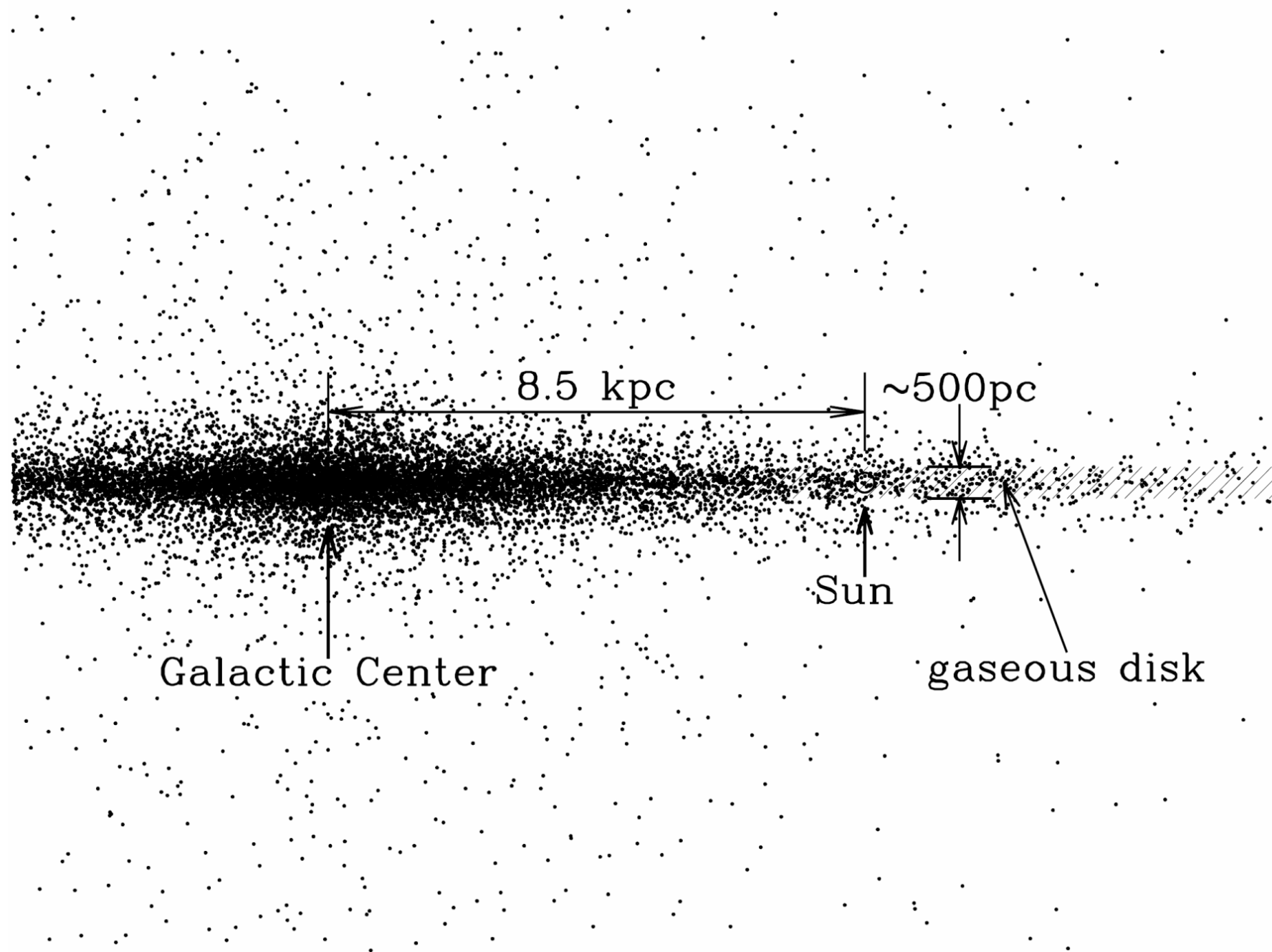


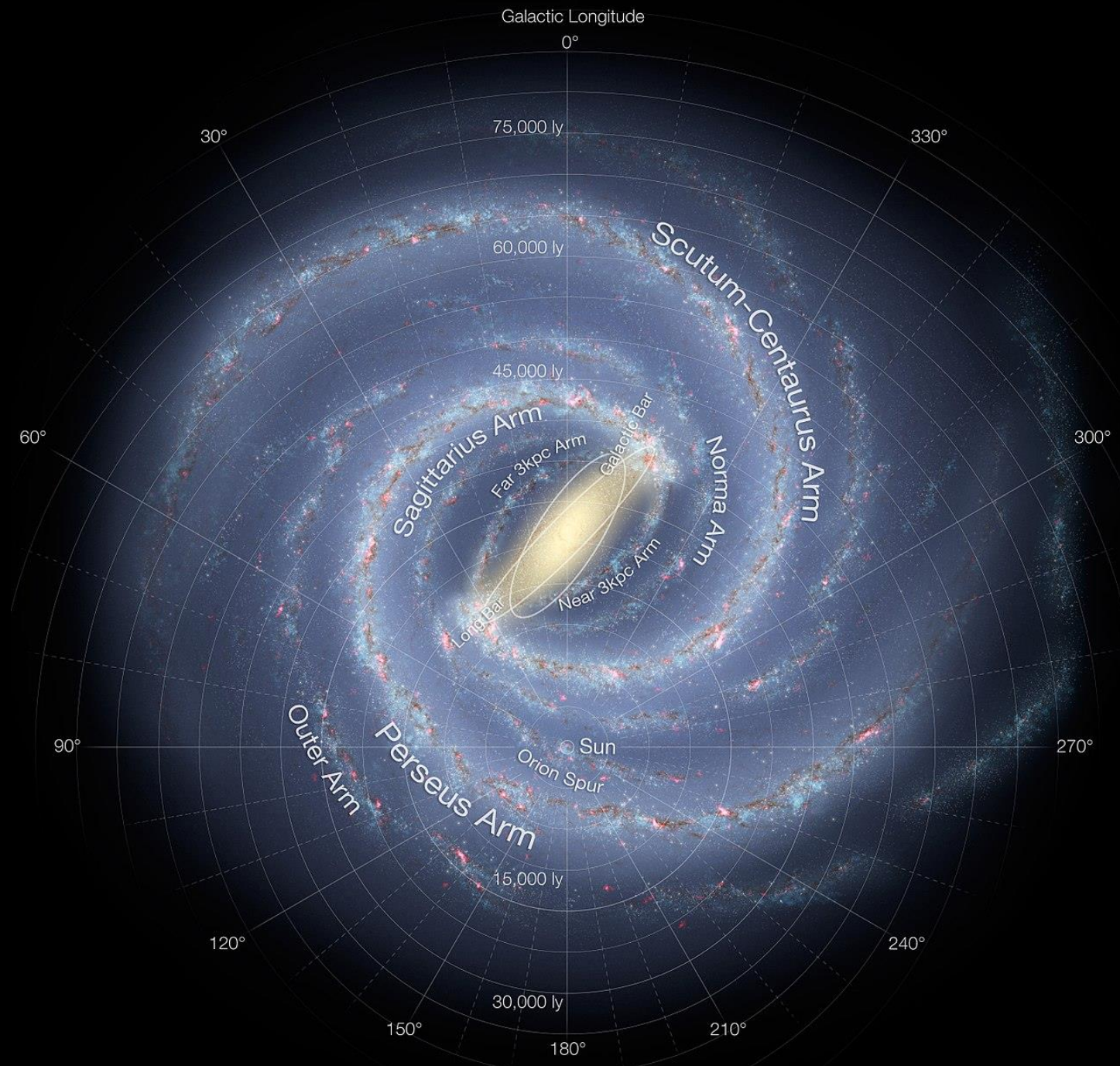
Flow of energy in the Milky Way

Draine

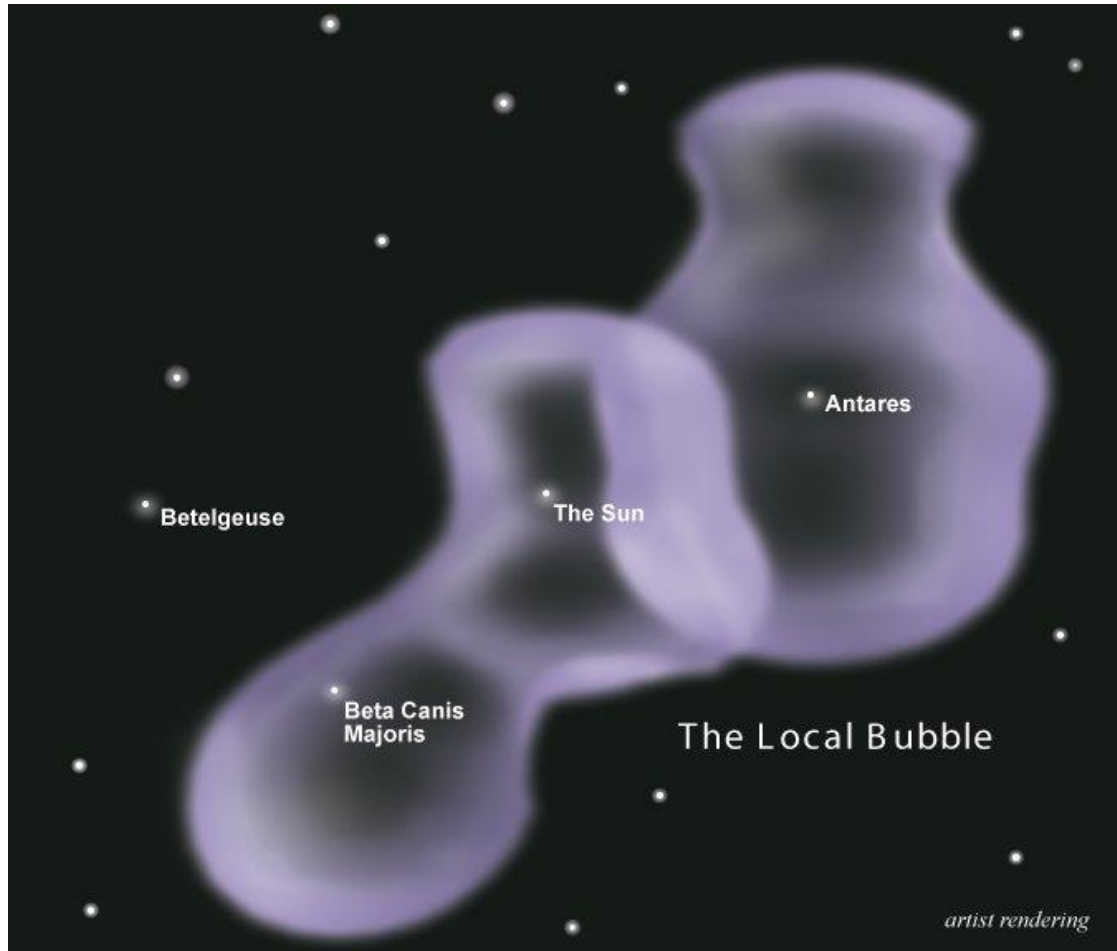


Galactic Ecology

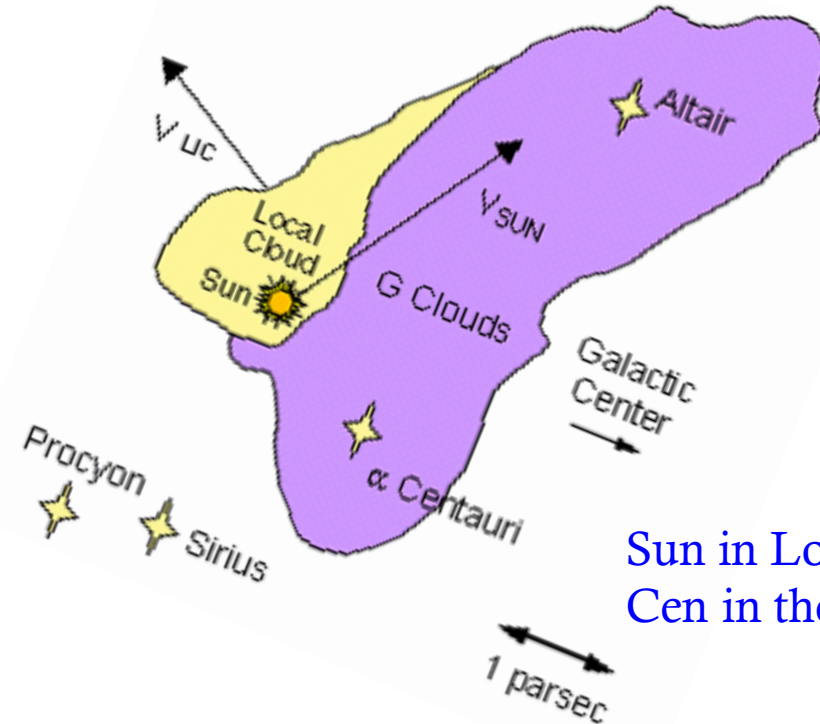




The Local Bubble A cavity of sparse, hot gas in the Orion Arm; ~ 100 pc across; $n \sim 0.05 \text{ cm}^{-3} \sim 0.1$ of ISM; likely by SN explosions 10--30 Myr ago?



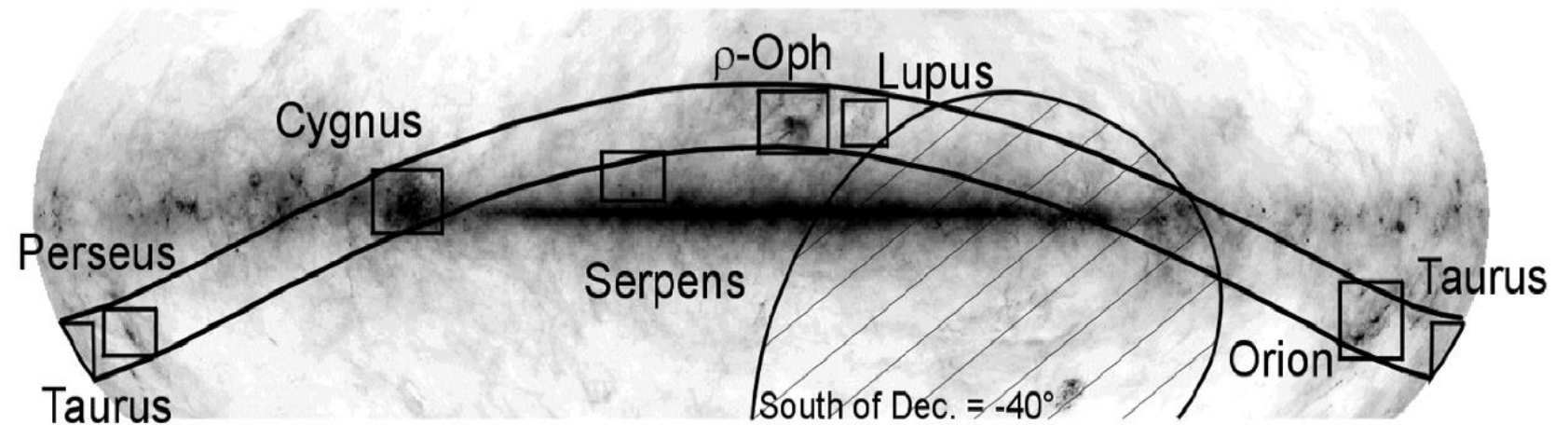
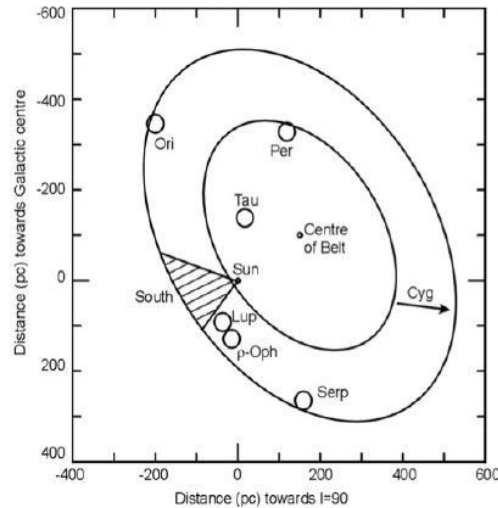
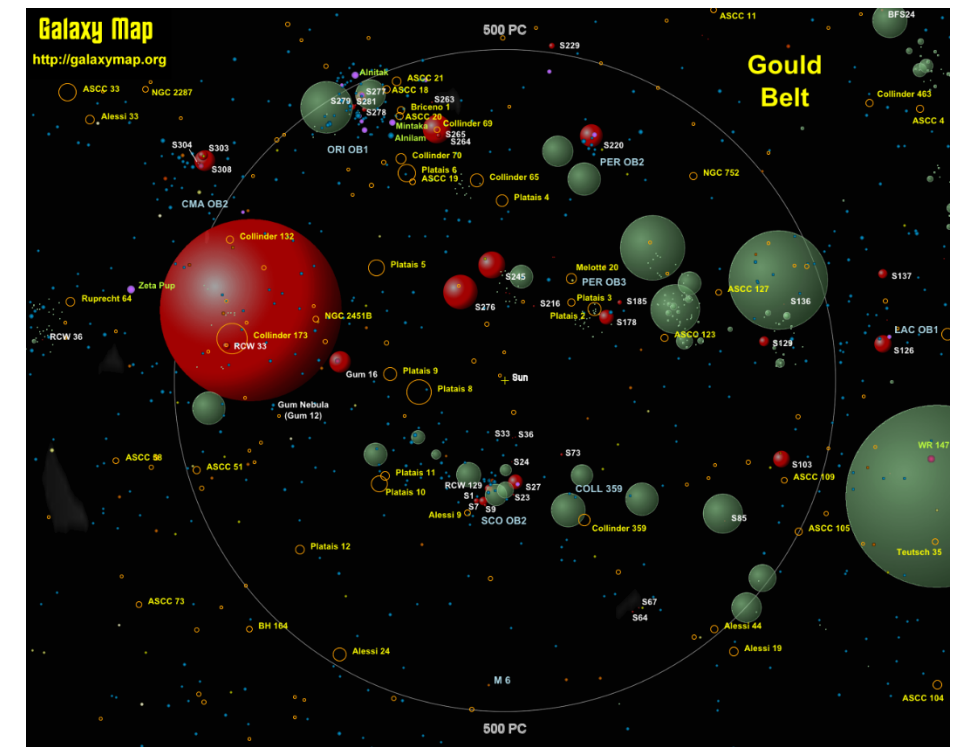
Where is the supernova (remnant)?
Check out the Orion-Eridanus [Superbubble](#)



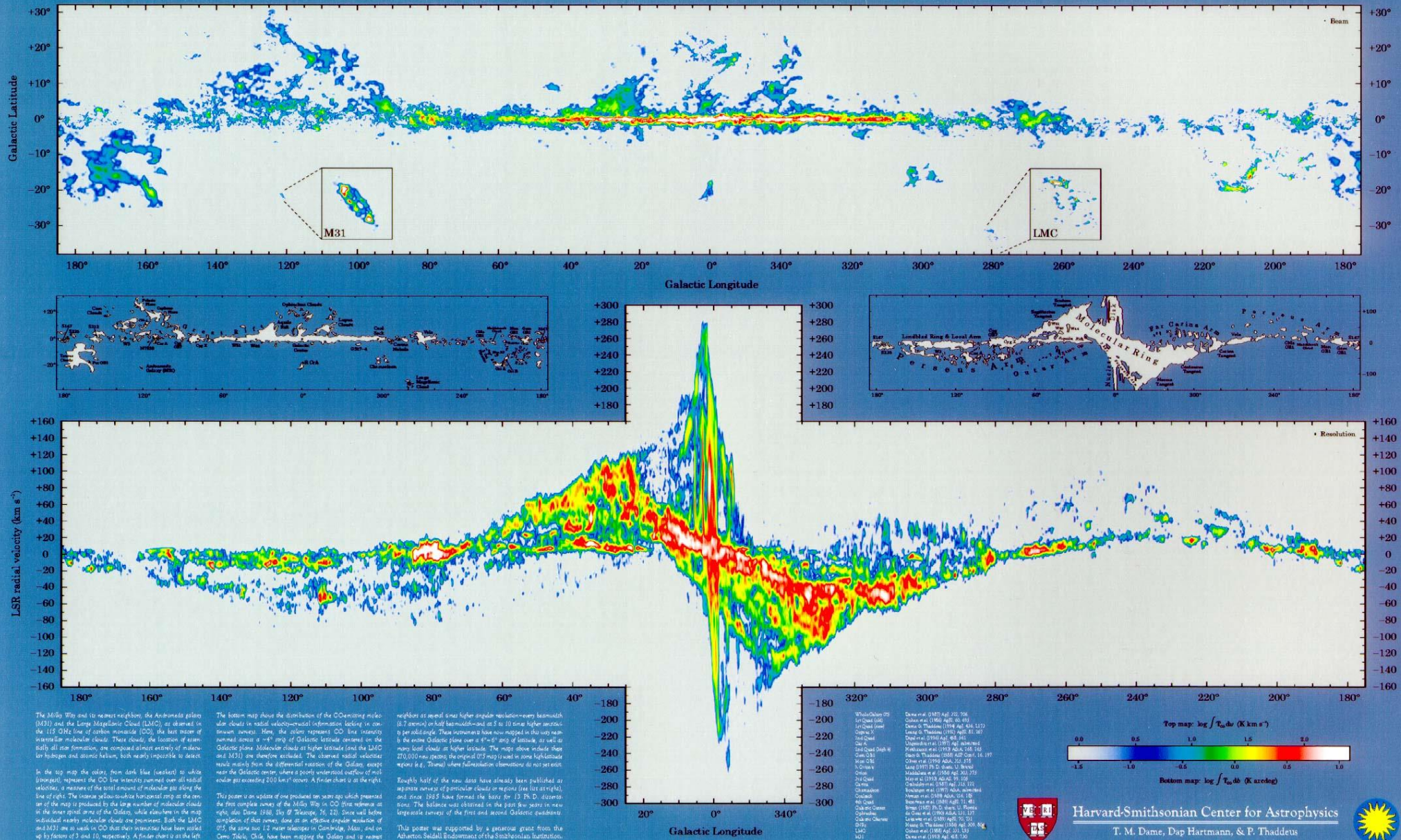
Sun in Local Cloud; Alpha Cen in the G-cloud complex

The **Gould Belt**, a (partial) ring in the sky, ~ 1 kpc across, centered on a point 100 pc from the Sun and tilted about 20 deg to the Galactic plane, containing star-forming molecular clouds and OB stars = local spiral arm

Origin unknown (dark matter induced star formation?)



The Milky Way in Molecular Clouds

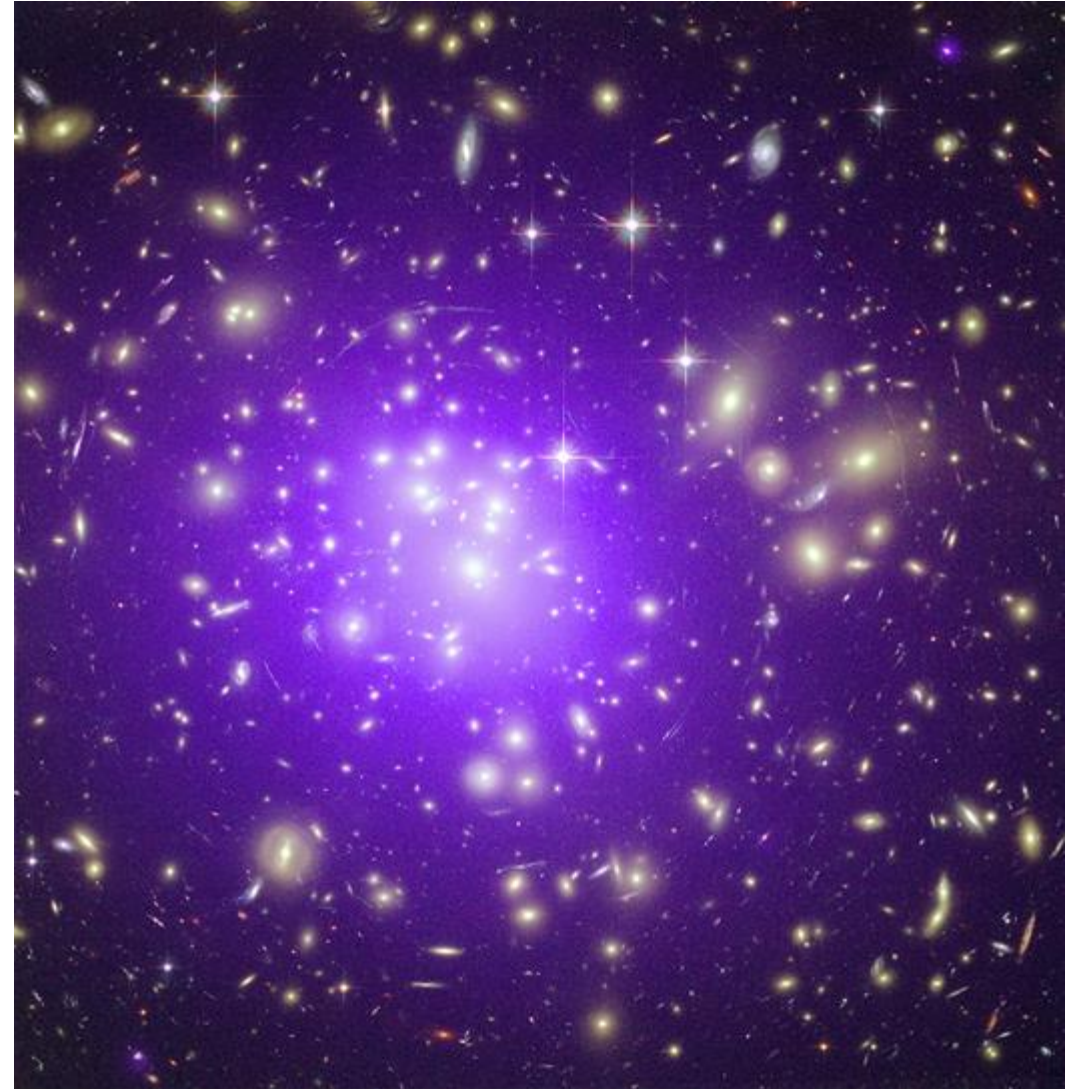


Intergalactic medium

Warm to hot (10^5 to 10^7 K)
sparse ($1/\text{m}^3$)

Intracluster medium

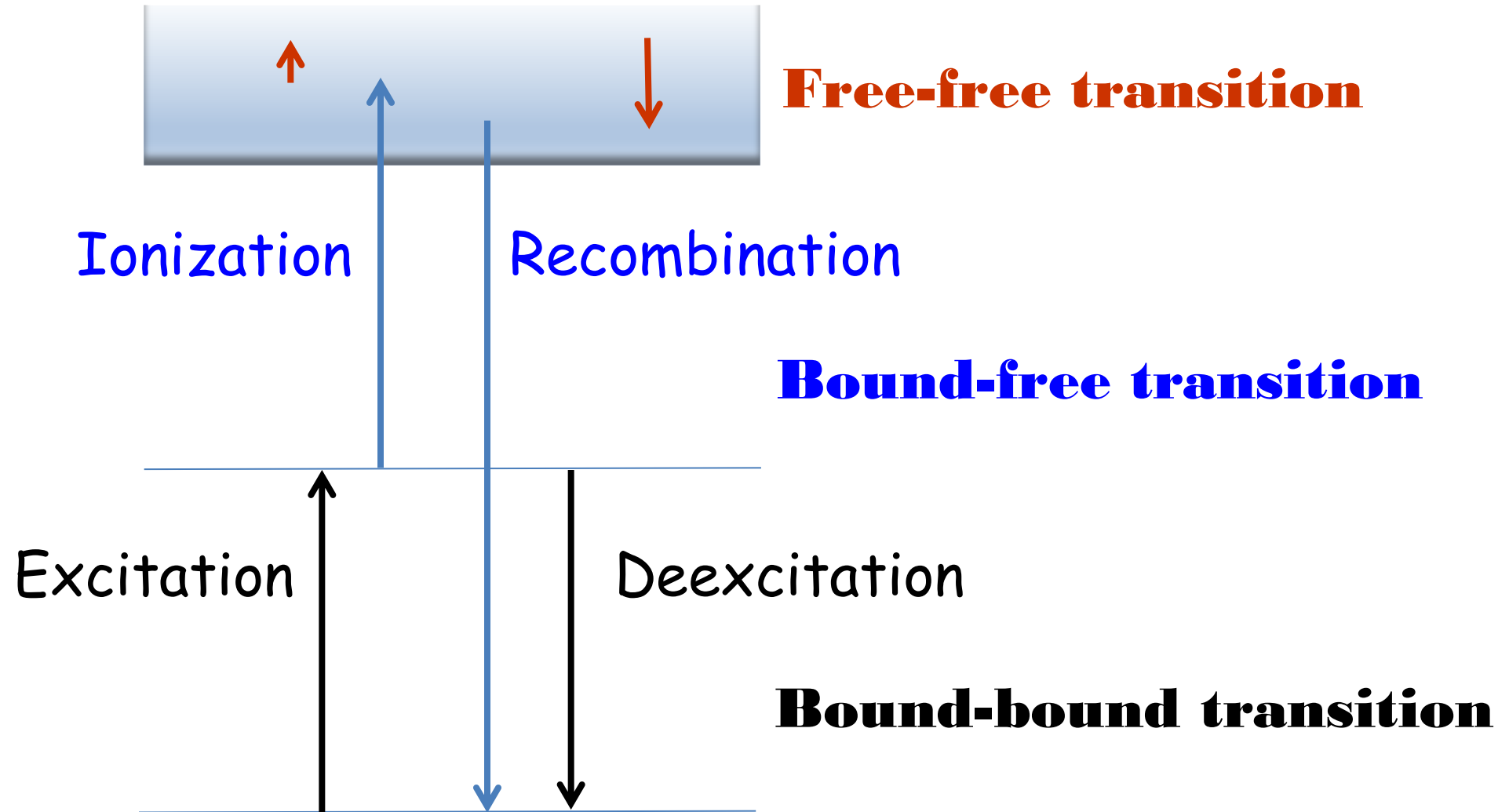
Hot (10^7 to 10^8 K)
sparse ($1000/\text{m}^3$)



Chandra image (100 MK) of Abell1689

Radiation and Matter

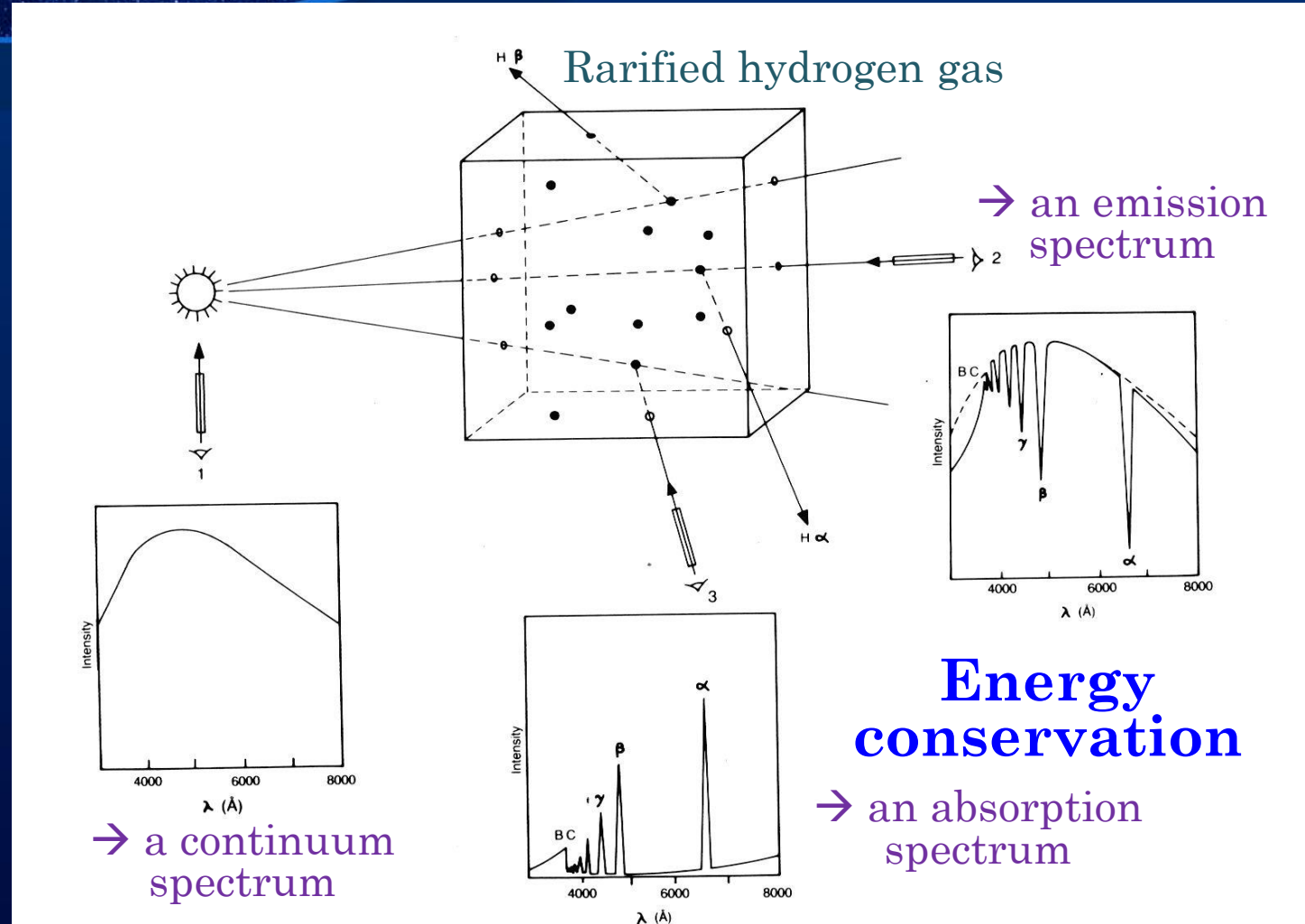
Electronic transitions Matter \leftrightarrow matter; matter \leftrightarrow photons



Rotational transition, vibrational transition, ...

Line Formation: Kirchhoff's Laws of Spectroscopy

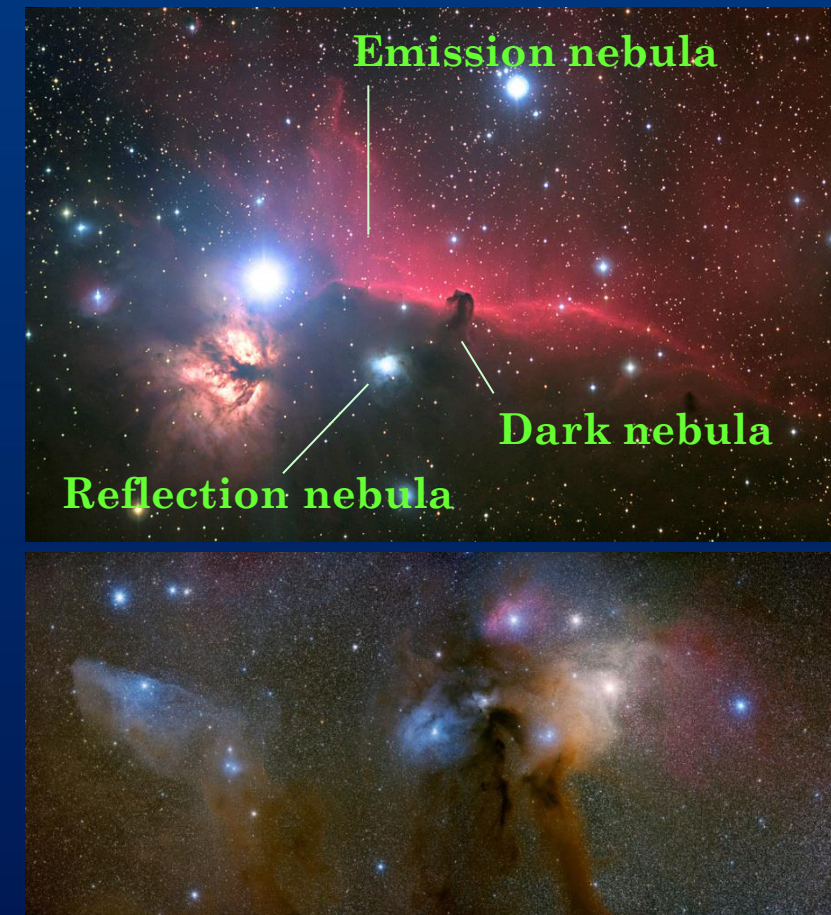
cf. circuit/current law



Kaler

Interstellar Clouds

- **Emission nebula**
Gas itself emits light
(excited by starlight, collision, etc.)
e.g., Balmer alpha → reddish
- **Reflection nebula**
Gas reflects/scatters light
→ bluish
- **Dark nebula**
Dust blocks background light
(stars, emission/reflection nebulae)
→ dark/black



A photograph may be a false-color composite. How to display a radio or X-ray image?



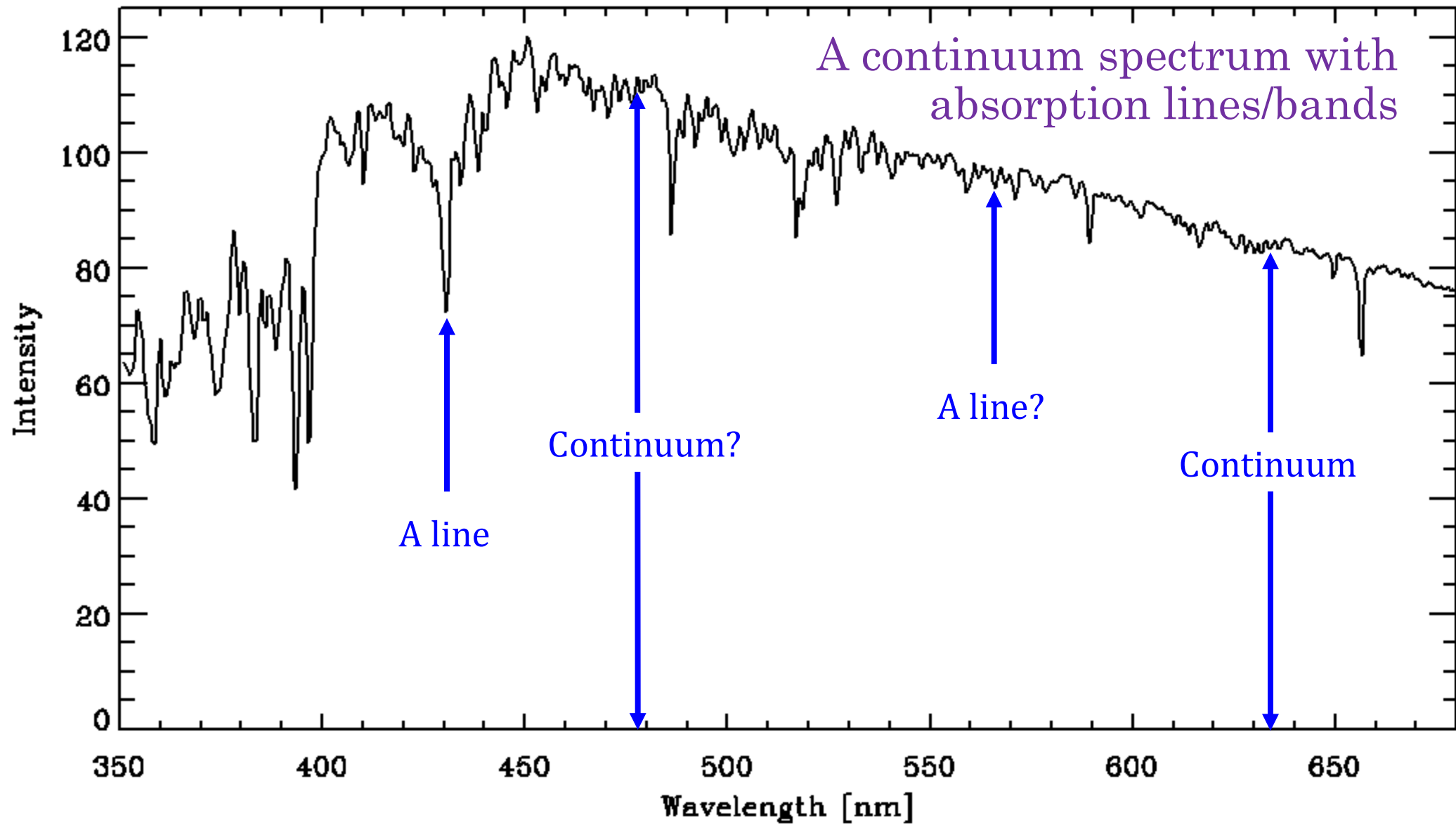
Star Shadows Remote Observatory

- Electromagnetic (EM) radiation (from gamma rays to radio waves) + cosmic rays + neutrinos + gravitational waves ...

Interactions between matter, between matter and energies/photons. We detect photons.

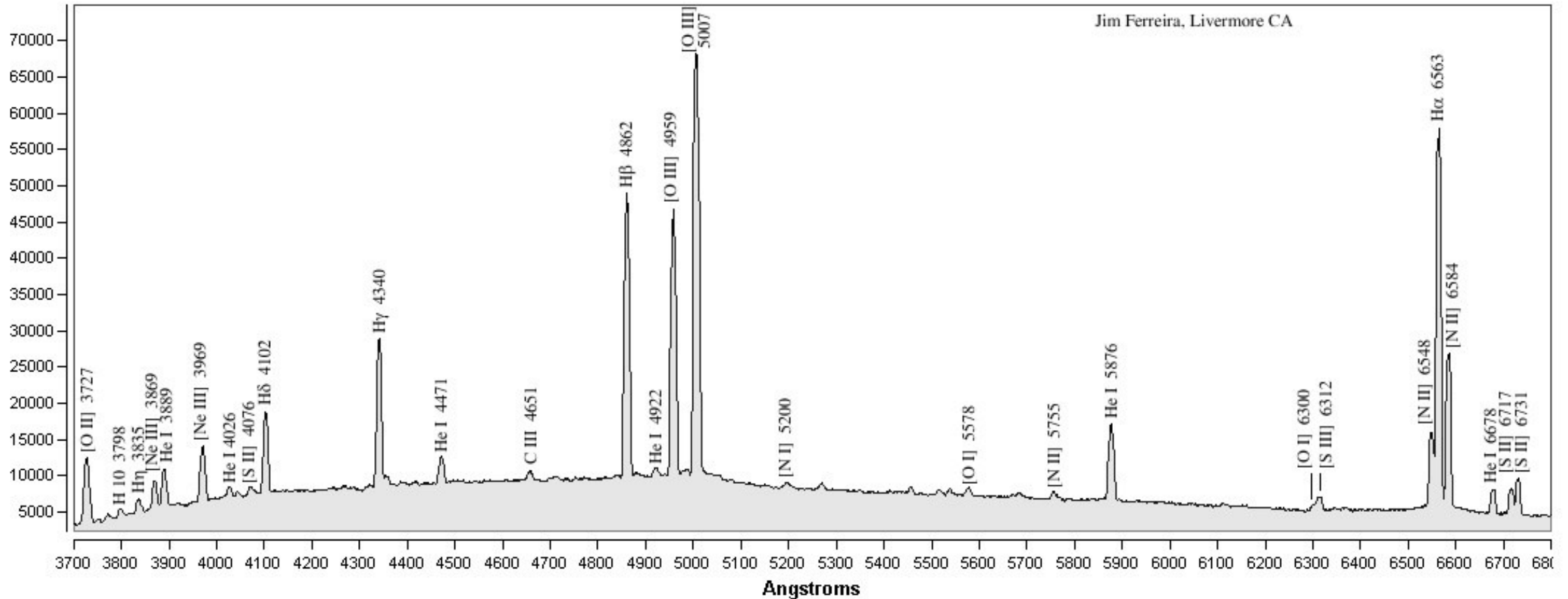
- Diagnosed by photometry, spectroscopy, polarization, etc.
 - **line** (absorption, emission) in a narrow range of frequency
e.g., $h\nu + \text{H}(^1\text{S}) \rightarrow \text{H}(^2\text{P})$ ($h\nu = 10.2 \text{ eV}$ or $\lambda = 121.6 \text{ nm}$)
 - **continuum** (absorption, emission) over a continuous range of ν
e.g., $h\nu + \text{H}(^1\text{S}) \rightarrow \text{H}^+ + \text{e}^-$ ($h\nu \geq 13.6 \text{ eV}$ or $\lambda \leq 91.2 \text{ nm}$)

Spectrum of a star $G1/2$ V



A weak continuum with prominent emission lines

Orion Nebula - M42 20141110UT Alpy 600 / C9@f/6.3



- **Photometry**

measurement of brightness of radiation (of a source, or a position in sky)

Astronomers use “magnitude” \leftrightarrow flux density

At the V band ($\lambda_{\text{eff}} = 550 \text{ nm}$; $\Delta\lambda = 86 \text{ nm}$), $F_{\nu}^{\text{V}=0} = 3.64 \times 10^{-23} [\text{W m}^{-2} \text{ Hz}^{-1}]$

$F_{\lambda}^{\text{V}=0} = 3.61 \times 10^{-11} [\text{W m}^{-2} \text{ nm}^{-1}]$; $N_{\lambda} = 1000 [\text{photons s}^{-1} \text{ cm}^{-2} \text{ \AA}^{-1}]$

- **Spectroscopy**

measurements of brightness distribution with wavelength or frequency

Spectrophotometry; Integral Field Unit (IFU); IF Spectrograph

- **Polarimetry**

*measurements of the polarization level (polarized intensity/total intensity)
and polarization angle*

Observations of the ISM

- Difficult: typical temps either too **low** or too **high**, so observable usually only outside visible wavelengths.

Planck function (1901) to describe a blackbody radiation

$$B_\nu d\nu = \frac{2h\nu^3}{c^2} \frac{n_\nu^2}{e^{h\nu/k_B T} - 1} d\nu \text{ [erg s}^{-1} \text{ cm}^{-2} \text{ sr}^{-1} \text{ Hz}^{-1}\text{]}$$

$$B_\lambda d\lambda = \frac{2hc^2}{\lambda^5} \frac{n_\nu^2}{e^{hc/\lambda k_B T} - 1} d\lambda \text{ [erg s}^{-1} \text{ cm}^{-2} \text{ sr}^{-1} \text{ \AA}^{-1}\text{]}$$

$$\lambda_{\text{max}} T \approx 2900 \text{ [\mu m} \cdot \text{K]} \dots \text{Wien's displacement law}$$

Not possible until the second half of the 20th century (detector technology, from space, etc.)

Blackbody radiation
(prescribed by the
Planck function) is a
continuum radiation.

$$B_\nu d\nu = \frac{2h\nu^3}{c^2} \frac{n_\nu^2}{e^{h\nu/k_B T} - 1} d\nu$$

$$\nu^3 \Leftrightarrow e^{-\nu}$$

Low ν

High ν

Short λ

Long λ

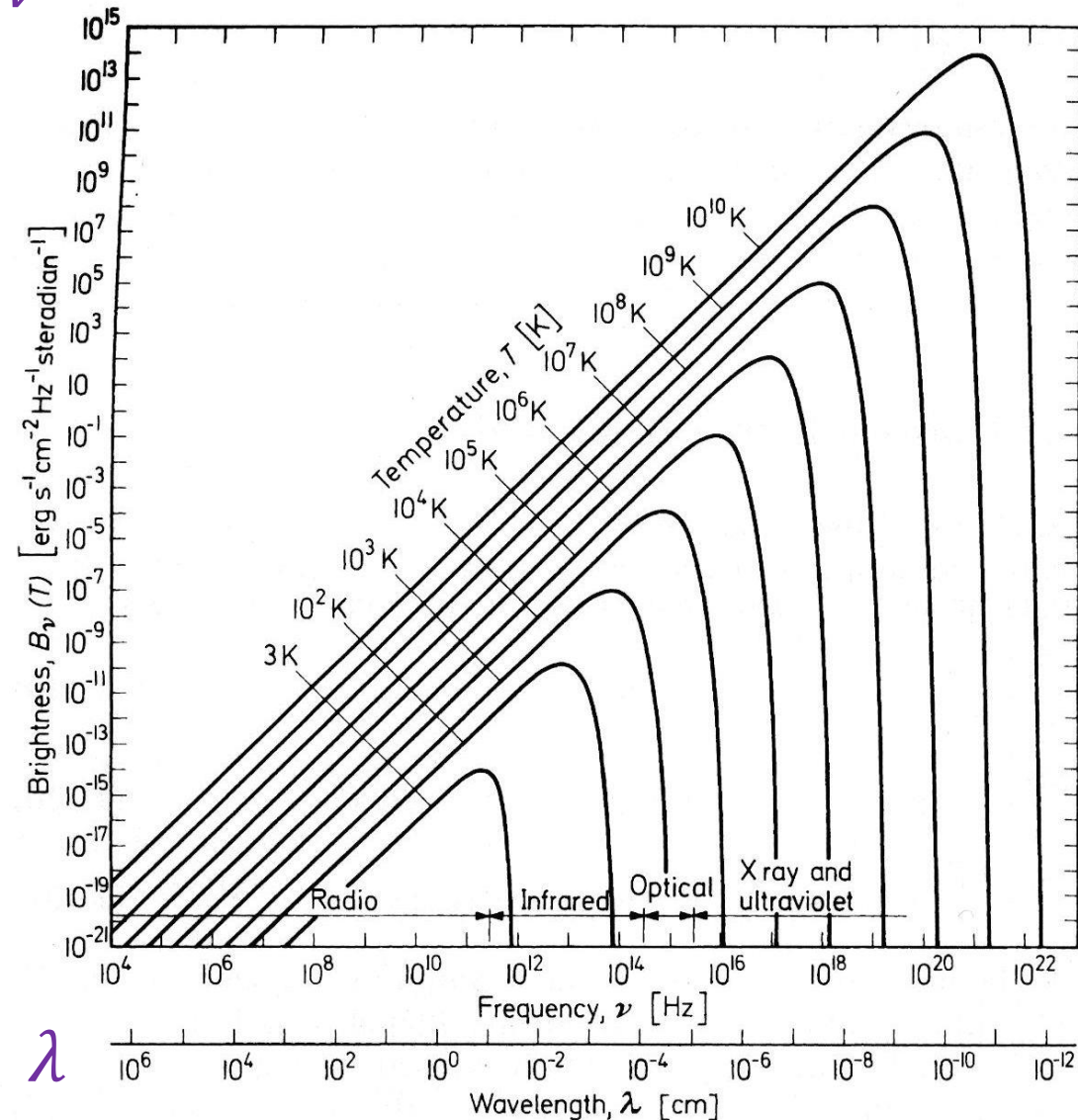
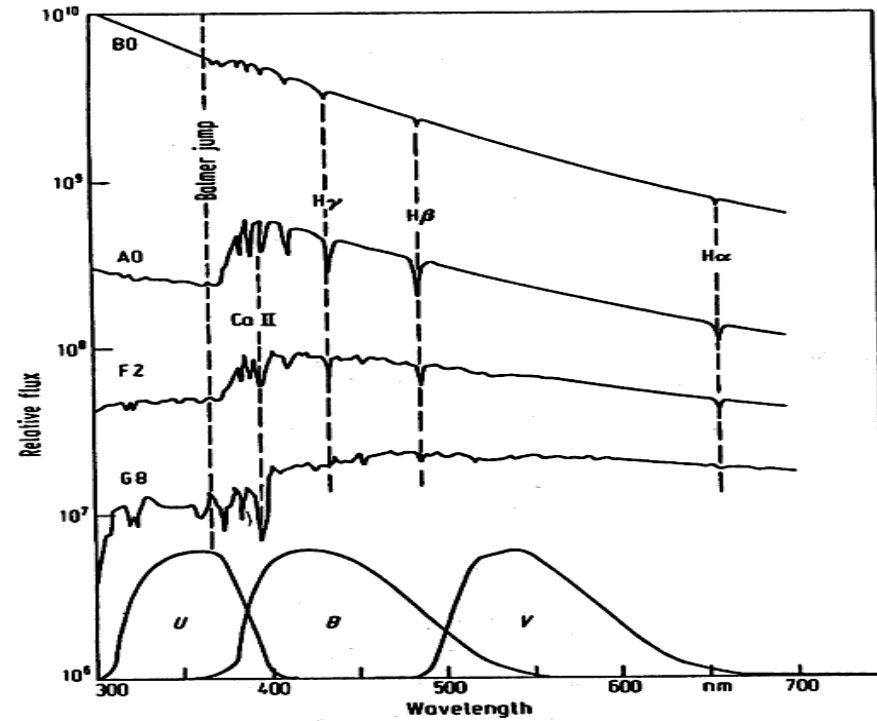
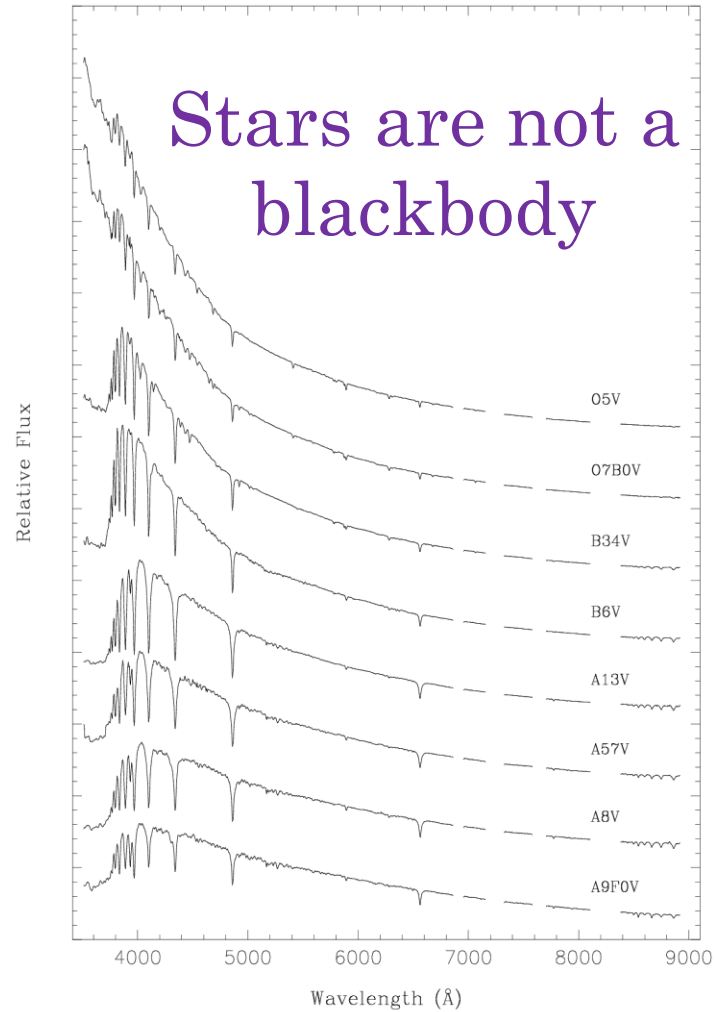
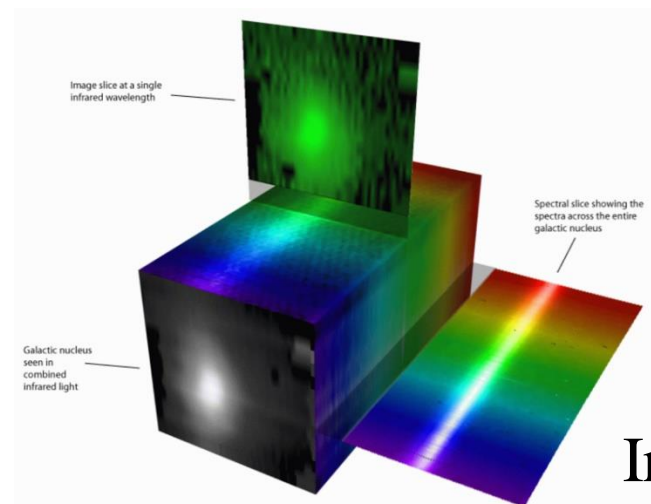


Fig. 1.1. The brightness, $B_\nu(T)$, of a black-body radiator at frequency, ν , and temperature, T . The Planck function $B_\nu(T)$, is given by Eq. (1.119)

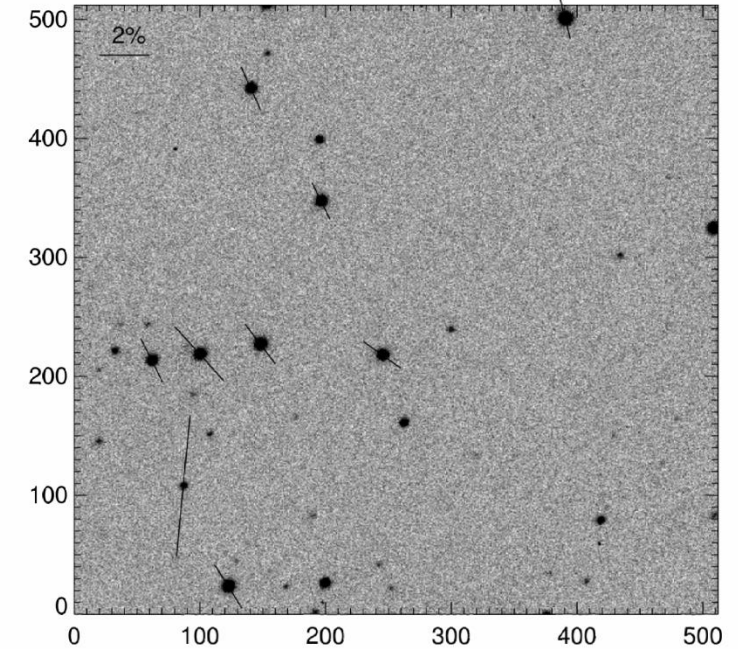
Spectra of hot stars



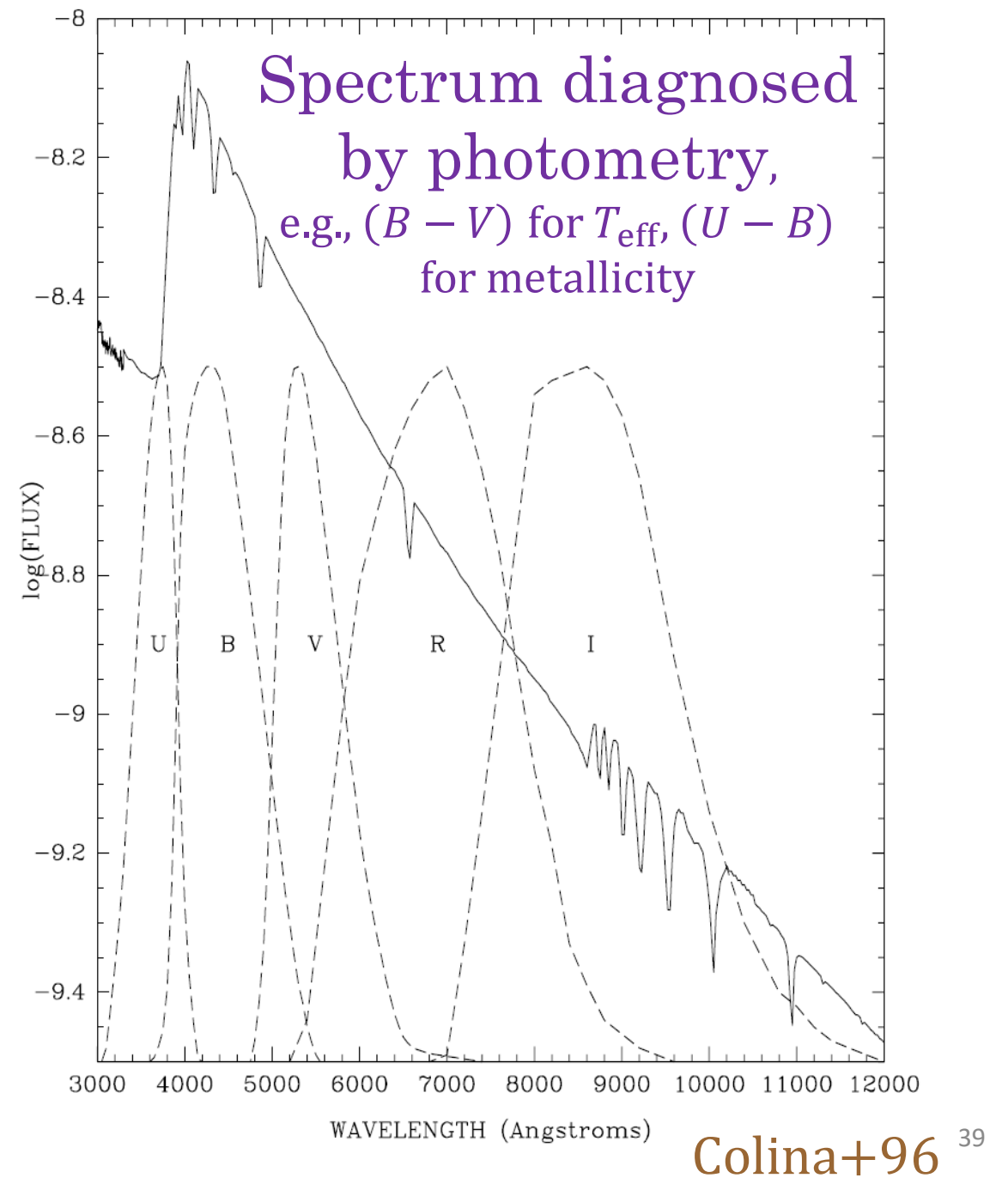
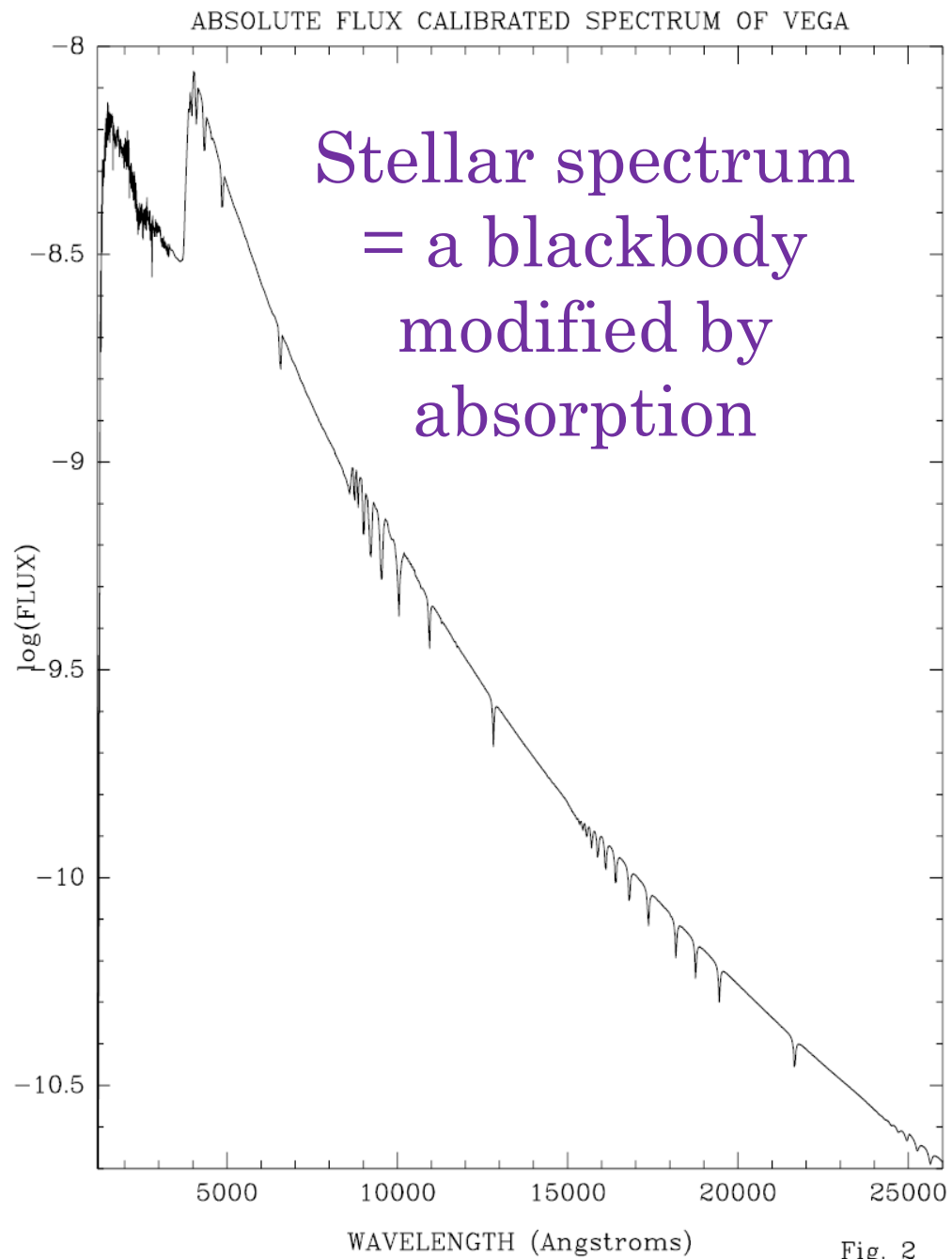
Imaging photometry



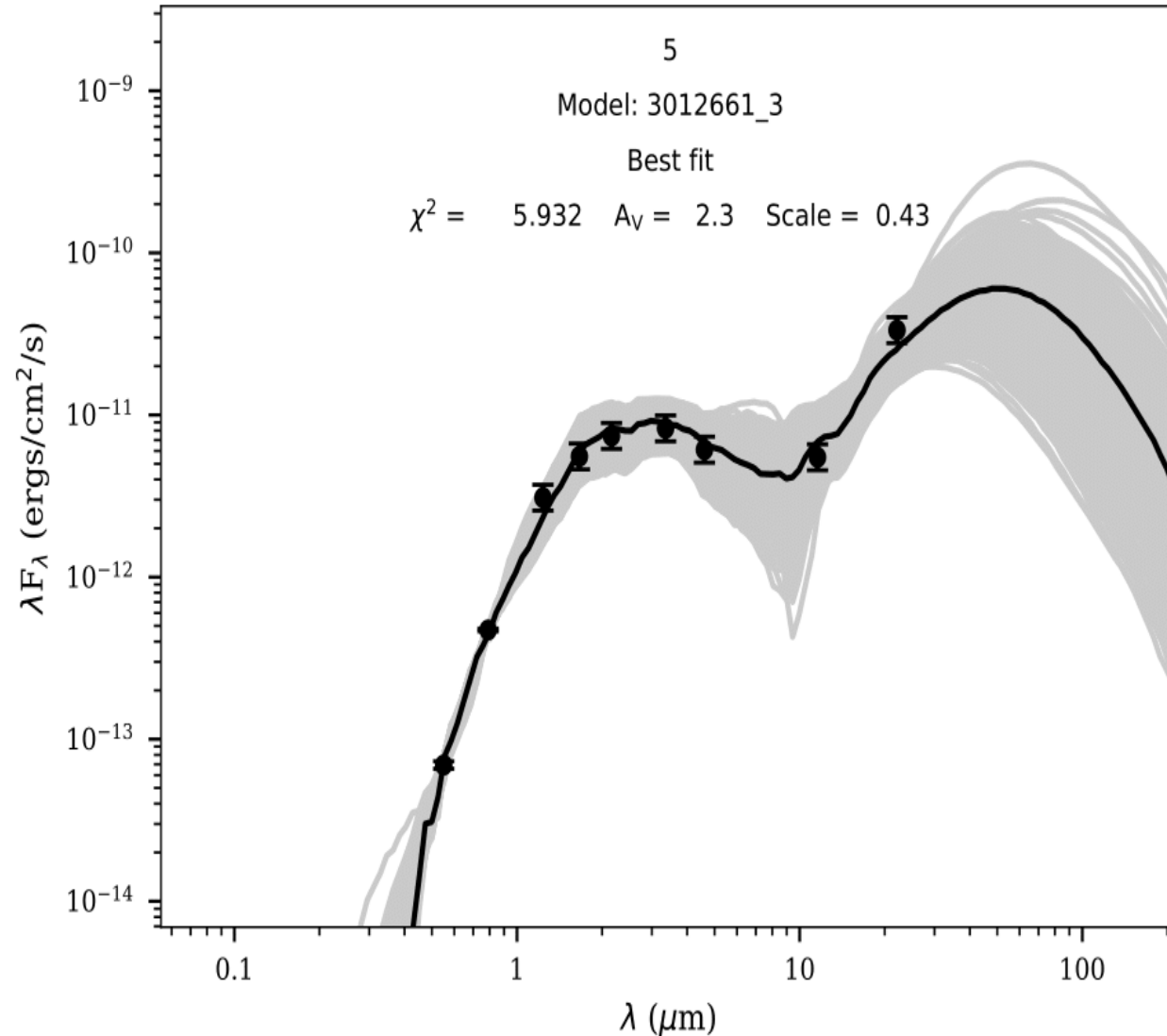
Photometry and polarization of background stars of a globule



Integral field spectroscopy



The Spectral Energy Distribution: photometry as a proxy of (a very low-dispersion) spectroscopy



Continuum

Absorption --- bound-free (ionization); free-free

Emission --- (thermal) blackbody; bremsstrahlung
(non-thermal) synchrotron; Čerenkov Cherenkov

Matter \Leftrightarrow energy \rightarrow what we observe

Thermodynamics (ISM cooling, heating, physical interactions;
chemical reactions ...)

Line

- Emission --- atom/ion/molecule already excited (by collisions or absorption of a photon from, e.g., a star)
- Absorption --- atom initially in a lower state and absorbs an incoming photon

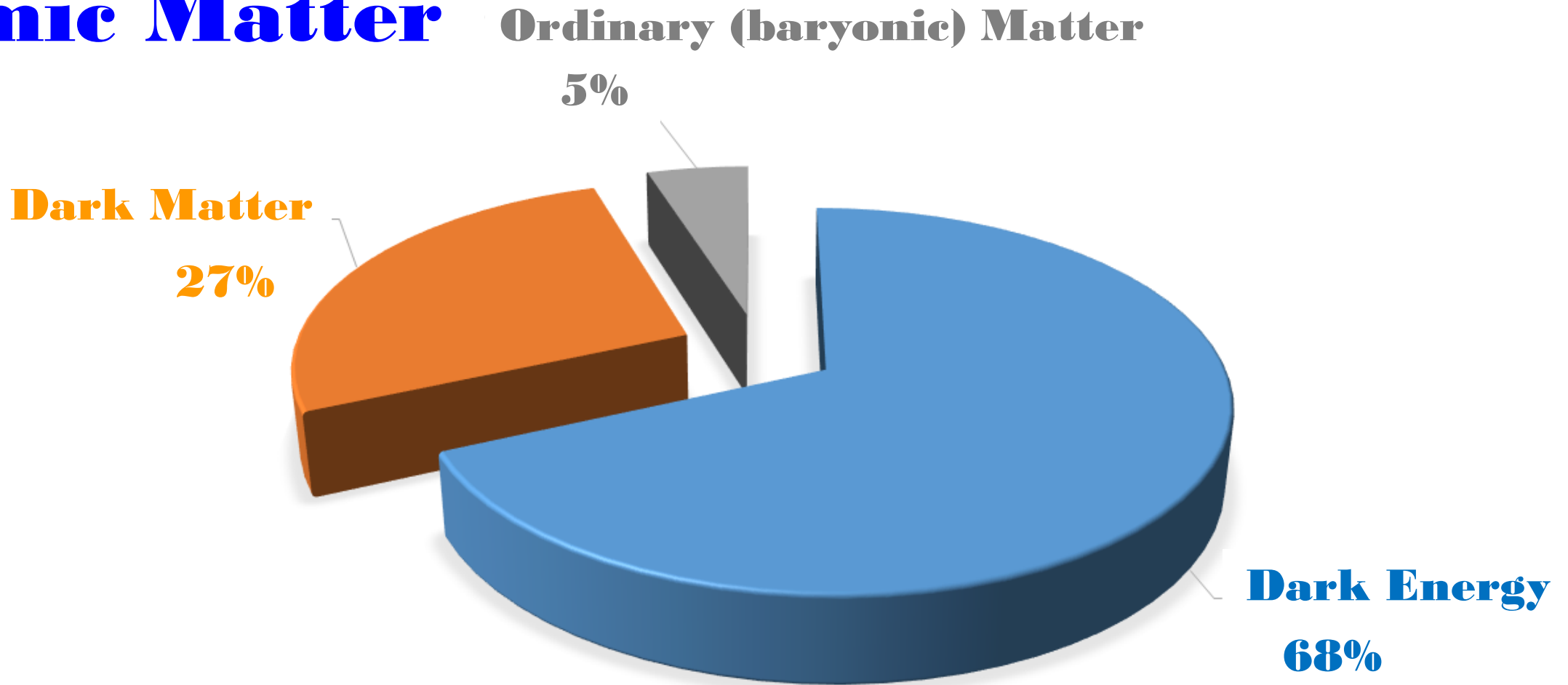
Transition between 2 quantum levels

(electronic, rotational, vibrational, stretching...)

- Collision ($u \rightarrow l$) or ($l \rightarrow u$) (upwards or downwards)
spontaneous emission ($u \rightarrow l$) (only downwards)
absorption ($l \rightarrow u$) (only upwards)
- Diagnosis: line strength, central wavelength, shape, ...

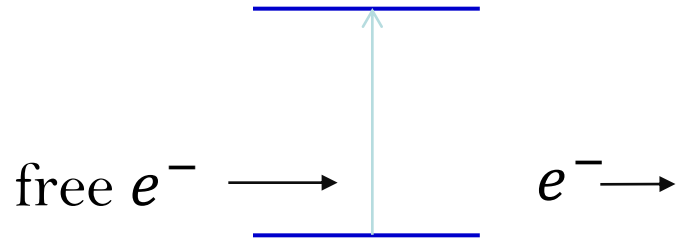
ISM in Gaseous and Solid States

Cosmic Matter

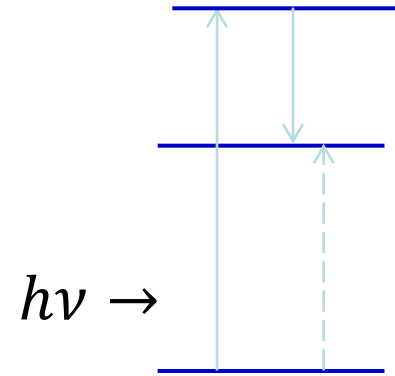


Early Universe: Energy \rightarrow Matter condensed + Energy
 \rightarrow ISM being gaseous \rightarrow Stars (light + complex elements)
 \rightarrow ISM of gas and dust (planets \rightarrow life) \rightarrow summer school⁴⁵

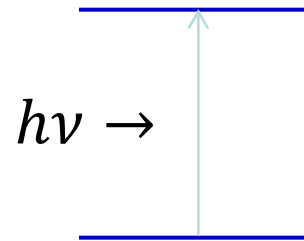
Excitation



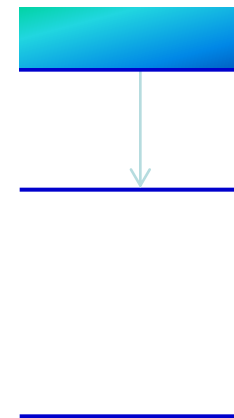
Collision



Photon Pumping



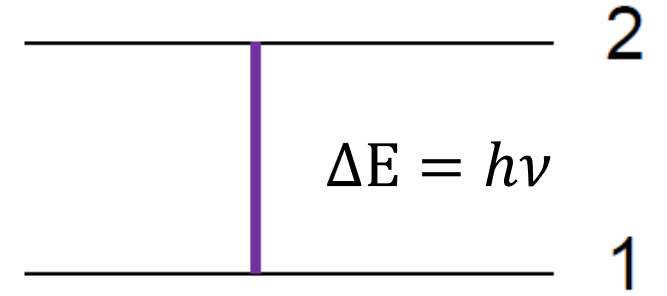
Radiation



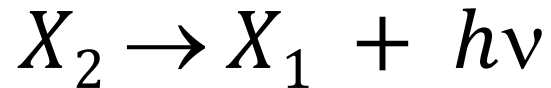
Recombination

Emission and Absorption

Two ways to jump down from an excited state



- **Spontaneous emission**



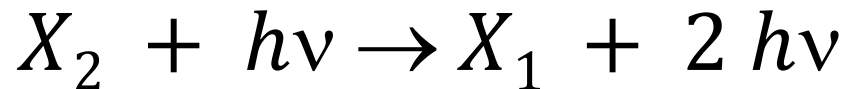
occurrence rate \leftrightarrow atomic properties

Colliding up

✓ colliding down, or

✓ jumping down

- **Stimulated emission**



occurrence rate \leftrightarrow density of incoming photons of the same ν , polarization, and direction of propagation

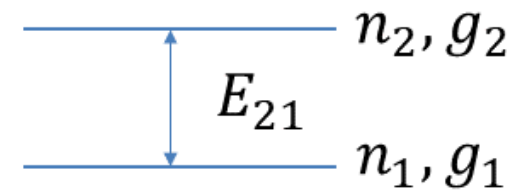
- **Collisional deexcitation** \rightarrow no emission of photons

Boltzmann Excitation Equation

$e^{-E_{21}/kT}$: Boltzmann factor

Population ratio between two excited states (of the same r -times ionized species)

$$\frac{n_2}{n_1} = \frac{g_2}{g_1} e^{-E_{21}/kT}$$

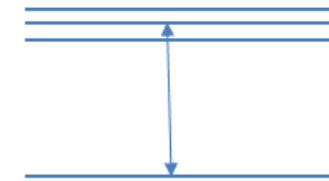


n_i : number density of the particles in the i -th energy state

g_i : **statistical weight** of the i -th energy state

= degeneracy of the level

= number of states with different quantum numbers but with the same energy



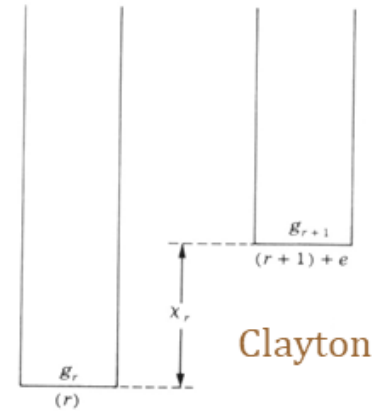
E_{21} : difference in excitation energies (wrt to ground state) = $h\nu$

It really should have been n_i^r or g_i^r for the same r -times ionization.

Saha Ionization Equation

Population ratio between two ionization stages

$$\frac{n_{r+1} n_e}{n_r} = \frac{G_{r+1} g_e}{G_r} \frac{(2\pi m_e kT)^{3/2}}{h^3} e^{-\chi_r/kT}$$



n_r : number density of the particles in the r -th ionized state

n_e : number density of free electrons

G_r, g_e : **partition functions** of the ionized species, and of the electron = sum of the statistical weights of all bound states, each weighted by the Boltzmann factor

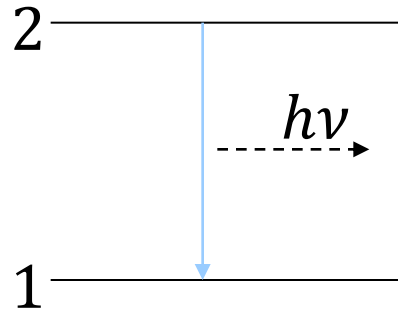
$G_r = \sum_i g_{r,i} e^{-\frac{E_i}{kT}}$, very often G_1 dominates; $g_e = 2$

χ_r : ionization potential from the ionization stage r to $r + 1$

Einstein Coefficients

Einstein (1917)

Spontaneous emission



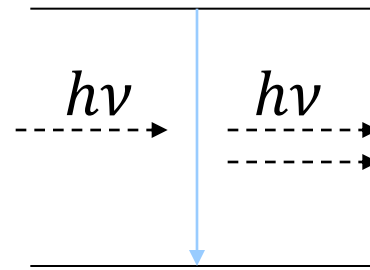
$$X_2 \longrightarrow X_1 + h\nu$$

$$\nu = (E_2 - E_1)/h$$

A_{21} --- probability [s^{-1}]

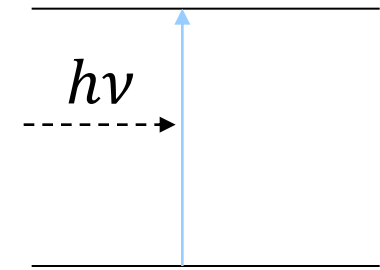
$n_2 A_{21} dt$: # of spontaneous radiative transitions during dt

Stimulated
(induced) emission (Stimulated) absorption



$$X_2 + h\nu \longrightarrow X_1 + 2 h\nu$$

B_{21}



$$X_1 + h\nu \longrightarrow X_2$$

B_{12}

$B I_\nu$ --- probability or $B u_\nu$ then unit different

$n_2 B_{21} I_\nu dt$ or $n_1 B_{12} I_\nu dt$: # of (stimulated) or radiative transitions during dt when irradiated with I_ν

Einstein

Separat-Abdruck aus:
Mitteilungen der Physikalischen Gesellschaft Zürich - Nr. 18, 1916.

112 4
Zur Quantentheorie der Strahlung
von A. Einstein.

Die formale Ähnlichkeit der Kurve der chromatischen Verteilung der Temperaturstrahlung mit dem Maxwell'schen Geschwindigkeits-Verteilungsgesetz ist zu frappant, als daß sie lange hätte verborgen bleiben können. In der Tat wurde bereits W. Wien in der wichtigen theoretischen Arbeit, in welcher er sein Verschiebungsgesetz

$$\varrho = \nu^3 f\left(\frac{\nu}{T}\right) \quad (1)$$

ableitete, durch diese Ähnlichkeit auf eine weitergehende Bestimmung der Strahlungsformel geführt. Er fand hiebei bekanntlich die Formel

$$\varrho = \alpha \nu^3 e^{-\frac{h\nu}{kT}} \quad (2)$$

welche als Grenzgesetz für große Werte von $\frac{\nu}{T}$ auch heute als richtig anerkannt wird (Wien'sche Strahlungsformel). Heute wissen wir, daß keine Betrachtung, welche auf die klassische Mechanik und Elektrodynamik aufgebaut ist, eine brauchbare Strahlungsformel liefern kann, sondern daß die klassische Theorie notwendig auf die Reileigh'sche Formel

$$\varrho = \frac{k}{h} \alpha \nu^2 T \quad (3)$$

führt. Als dann Planck in seiner grundlegenden Untersuchung seine Strahlungsformel

$$\varrho = \alpha \nu^3 \frac{1}{e^{\frac{h\nu}{kT}} - 1} \quad (4)$$

auf die Voraussetzung von diskreten Energie-Elementen gegründet hatte, aus welcher sich in rascher Folge die Quantentheorie entwickelte, geriet jene Wien'sche Überlegung, welche zur Gleichung (2) geführt hatte, naturgemäß wieder in Vergessenheit.

Vor kurzem nun fand ich eine der ursprünglichen Wien'schen Betrachtung¹⁾ verwandte, auf die Grundvoraussetzung der Quanten-

¹⁾ Verb. d. deutschen physikal. Gesellschaft, Nr. 13/14, 1916, S. 318. In der vorliegenden Untersuchung sind die in der eben zitierten Abhandlung gegebenen Überlegungen wiederholt.

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"On the Quantum Theory of Radiation" by A. Einstein

Einstein relations

$$g_1 B_{12} = g_2 B_{21}$$

$$A_{21} = \frac{2h\nu^3}{c^2} B_{21}$$

These relate to the intrinsic properties of an atom.

<https://einstein.manhattanrarebooks.com/pages/books/17/albert-einstein/zur-quantentheorie-der-strahlung-on-the-quantum-theory-of-radiation>

Define the **excitation rate coefficient** γ_{01} , so that

of excitation $\text{s}^{-1} \text{cm}^{-3}$ ($= n_e n_1 v \sigma$) $\equiv n_e n_1 \gamma_{12}$,
where both n_e and n_1 have units of $[\text{cm}^{-3}]$

$$\gamma_{12} \equiv \langle \sigma v \rangle = \int_{\chi=\frac{1}{2}mv^2}^{\infty} \sigma_{01}(v) v f(\vec{v}) d^3 \vec{v}$$

Here σ_{12} is the excitation cross section, and $f(\vec{v})$ is the Maxwellian distribution function,

$$f(\vec{v}) dv = 4\pi \left(\frac{m}{2\pi kT} \right)^{3/2} v^2 e^{-\frac{mv^2}{2kT}} dv$$

So

$$\gamma_{12} = \frac{4}{\sqrt{\pi}} \left(\frac{1}{2kT} \right)^{1/2} \int_{\chi=\frac{1}{2}mv^2}^{\infty} v^3 \sigma_{12}(v) e^{-\frac{mv^2}{2kT}} dv$$

This is the upward transition $1 \rightarrow 2$.

For the downward transition $2 \rightarrow 1$,
the spontaneous emission rate $= n_2 A_{21}$,
and the deexcitation rate by collisions $= n_2 n_e \gamma_{21}$,
where $\gamma_{21} = \int_0^\infty \nu \sigma_{21}(\nu) f(\vec{\nu}) d^3 \vec{\nu} = \gamma_{21}(T)$

In a steady state, [upward rate]=[downward rate],
i.e., in **detailed balancing**,

$$n_1 n_e \gamma_{12}(T) = n_2 [A_{21} + n_e \gamma_{21}(T)]$$

The competition for downward transition between the two terms
in the bracket \rightarrow **critical density** (radiative deexcitation = collisional deexcitation)

$$n_{\text{crit}} = A_{10}/\gamma_{10}$$

When $n_e > n_{\text{crit}}$, collisions dominate the deexcitation process
 \rightarrow LTE, populations governed by the Boltzmann equation

For example, NH_3 (ammonia) is a good tracer of clumps of cold dense gas, and has a critical density of $n_{\text{H}_2} \approx 10^4 \text{ cm}^{-3}$

$$A_{21} \Leftrightarrow n_e \gamma_{21} \quad 1/A_{21} : \text{Lifetime in the excited state}$$

If staying up too long (?) $1/A_{21} \rightarrow$ colliding down \rightarrow no emission, unless in a very low-density environment (space)

❑ **Allowed (regular) Lines** (no bracket),

$$A \approx 10^{+8} \text{ s}^{-1}, \text{ e.g., C IV}$$

❑ **Semi-forbidden Lines** (a single bracket),

$$A \approx 10^{+2} \text{ s}^{-1}, \text{ e.g., [OII]}$$

❑ **Forbidden Lines** (a pair of square brackets),

$$A \approx 10^0 \text{ to } 10^{-4} \text{ s}^{-1}, \text{ e.g., [O III], [N II]}$$

- Normally an atom stays in an excited state for 10^{-8} s.
- A forbidden transition occurs for excitation levels $< \text{a few eV}$ (for heavy ions, cf. for H 10^4 eV) ; an electron remains excited for seconds or longer before returning to the ground state.
- On Earth $n \uparrow\uparrow$, both excitation and de-excitation take place frequently, so radiative transition (emitting a photon) is unlikely.
- In ISM, the electrons are not energetic enough to excite the atoms to normal levels (10 to 20 eV) , but enough to excite to metastable levels. In hot, low-density environments, e.g., in H II regions, PNe, solar corona, earth aurora ...

Once (collisionally) excited \rightarrow emission

\rightarrow photons escaped \rightarrow **cooling** *'Metals' are efficient coolants.*

Some examples:

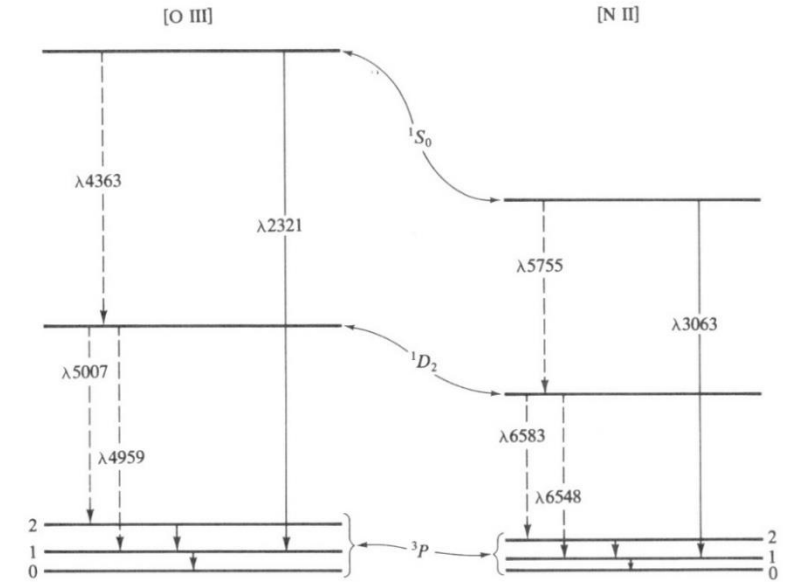
Lyman α ($H, n = 3 \rightarrow 2$), $A_{21} \approx 6.25 \times 10^8 \text{ s}^{-1}$

[O III] $A_{21} = 0.021 \text{ s}^{-1}, \lambda_{21} = 5007 \text{ \AA}$

$A_{21} = 0.0281 \text{ s}^{-1}, \lambda_{21} = 4959 \text{ \AA}$

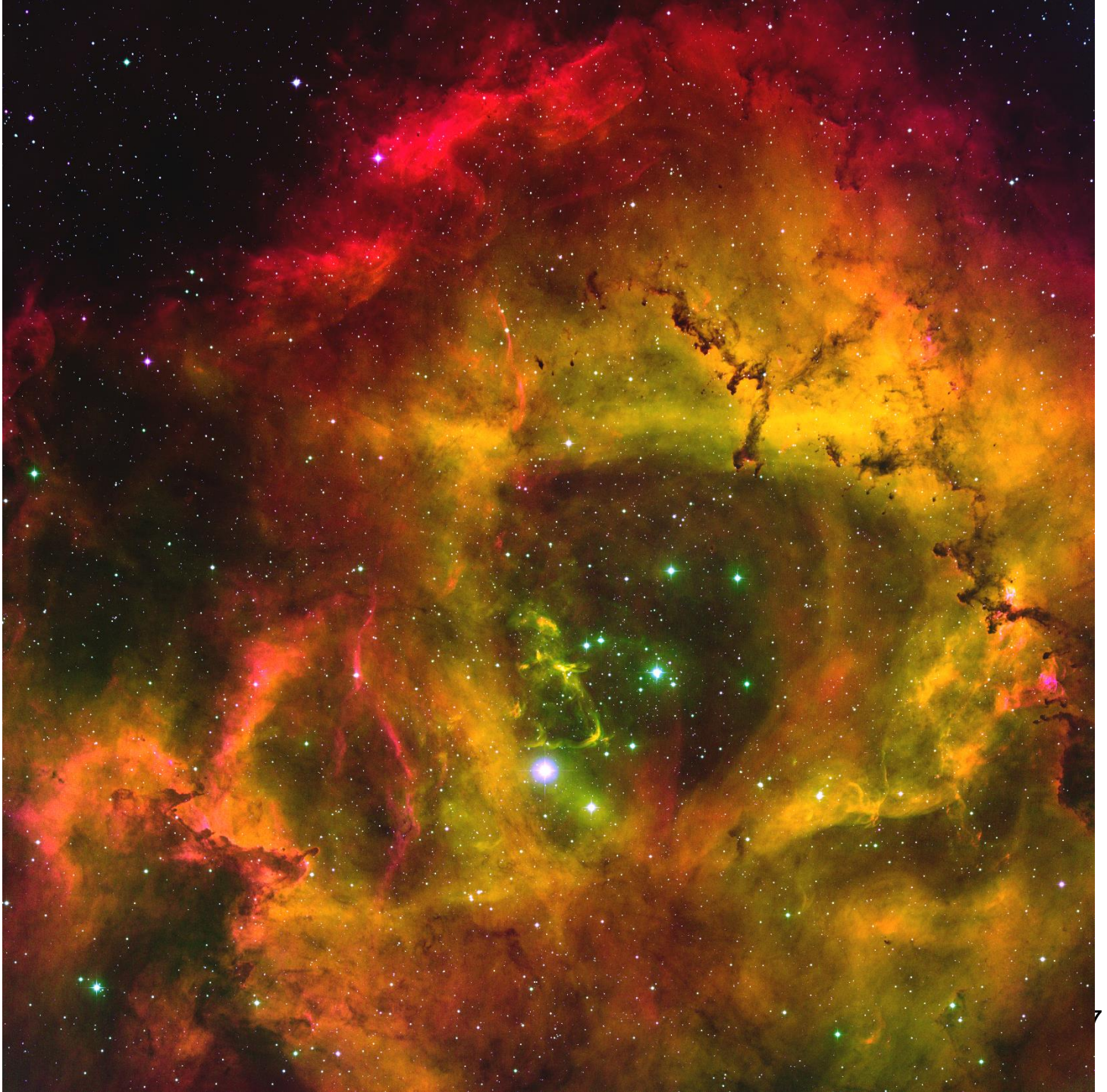
$A_{32} = 1.60 \text{ s}^{-1}, \lambda_{32} = 4364 \text{ \AA}$

[S II] $A_{21} = 4.7 \times 10^{-5} \text{ s}^{-1}, \lambda_{21} = 6716 \text{ \AA}$

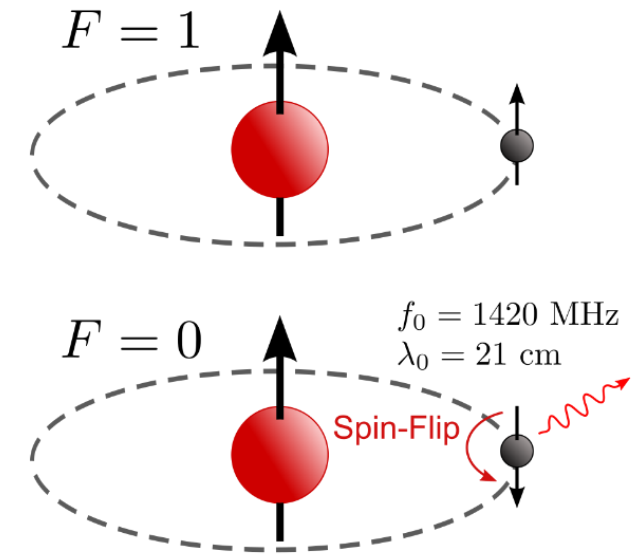


Rosette Nebula and NGC 2244 (H II)

Red: H-alpha
Blue: [S II]
Green: [O III]

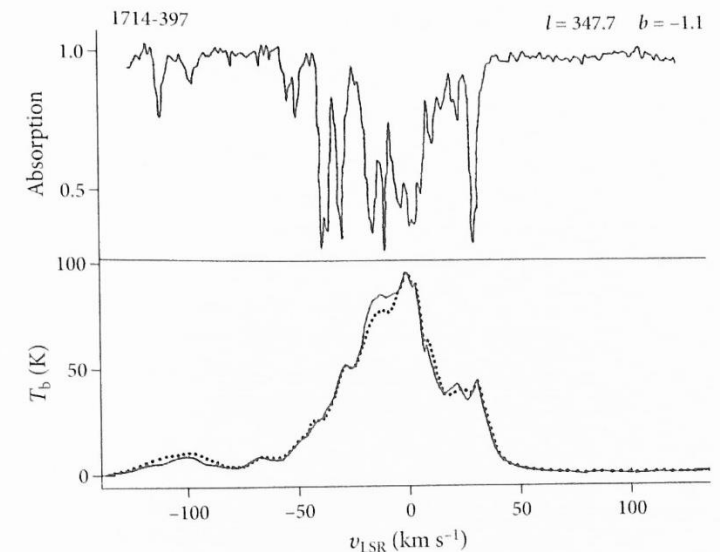


For H, the ground electronic state $1s\ 2S_{1/2}$ has $J = 1/2$, and the proton has $I = 1/2$. The state splits into (total) $F = I + J = 0$ or $F = 1$, $\Delta E = 6.7 \times 10^{-6}$ eV (**hyperfine structure**), $\nu \approx 1420.405751$ MHz, $\lambda \approx 21$ cm.



https://en.wikipedia.org/wiki/Hydrogen_line

The H I **21 cm line** $A_{21} \approx 2.8 \times 10^{-15} \text{ s}^{-1}$; $\tau_{1/2} \approx A_{10}^{-1} \approx 3.5 \times 10^7 \text{ s} \approx 10$ million yrs; transition probability extremely low; useful in detecting atomic hydrogen (amount, motion, etc.) in space.



For $n = 2$, $\ell = 1$, and with spin, a total angular momentum of $\ell(\ell + 1)\hbar^2 = 2\hbar^2$

3 substates, $\hbar, 0, -\hbar$, $m = 1, 0, -1$ (magnetic quantum number)

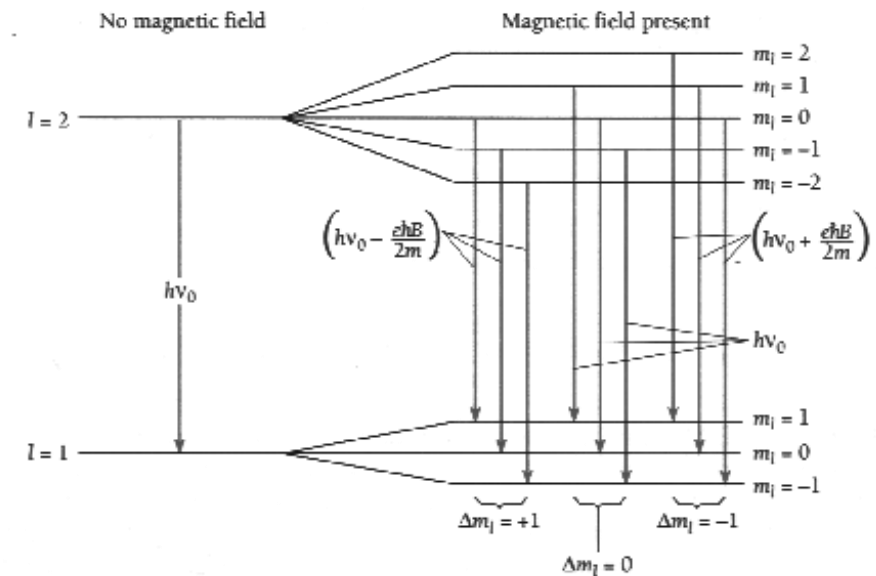
Fine structure, $\Delta\mathcal{E}$ very small, $\sim 10^{-5}$ eV

But with an external **B** field \rightarrow **Zeeman splitting**

With a typical ISM field of $10 \mu\text{G}$, the 21-cm line shifts 10^{-8} , equivalent to an RV of a few km s^{-1} ; very difficult to detect

Detectable by the difference of the two circular polarization signals.

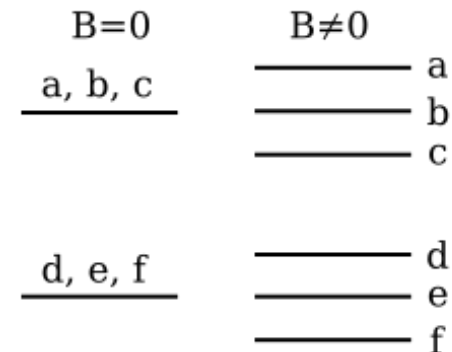
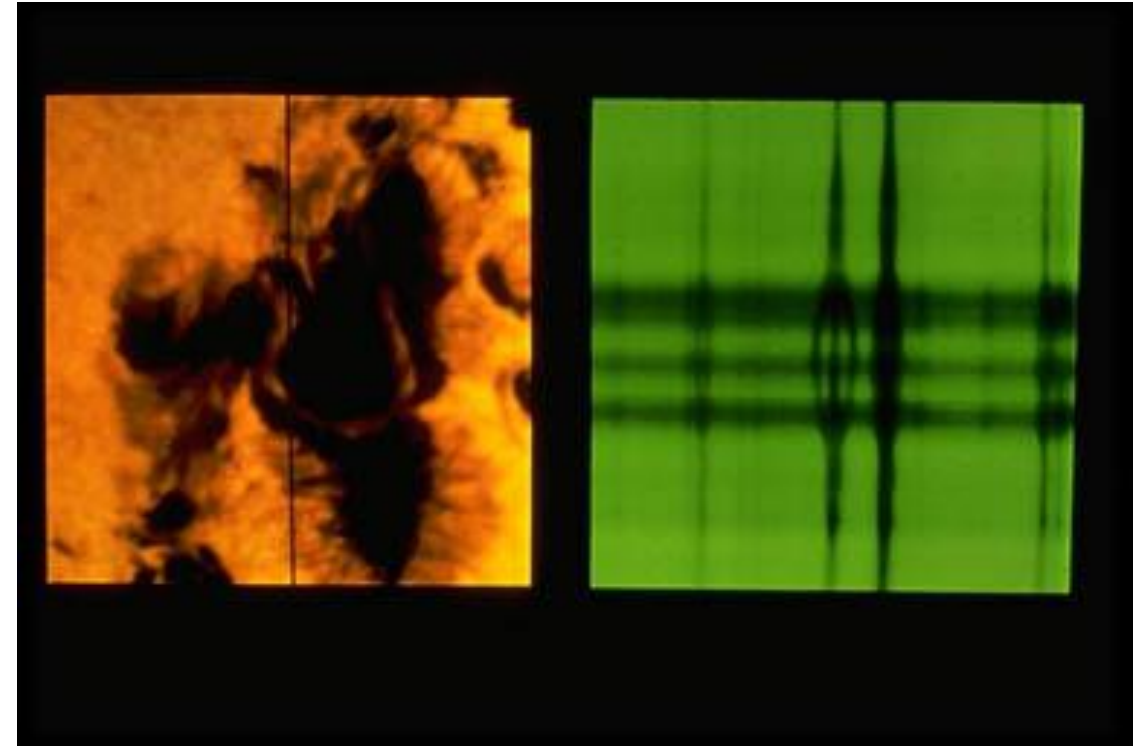
Also in OH 18 cm and 6 cm, H_2CO 6 cm lines \rightarrow to derive B and $n(\text{HI})$



Zeeman Effect

... the split of a spectral line into several components in the presence of a **magnetic field**. It is analogous to the **Stark effect**, the splitting of a spectral line into several components in the presence of an **electric field**.

In (kG) and out (1 G) of sunspots



Ionization Processes

- Photoionization

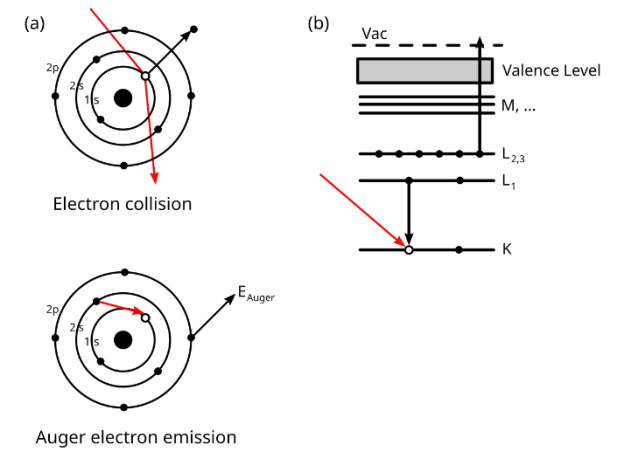
- Auger ionization

an inner-shell electron is photoionized \rightarrow a higher-level electron fills in \rightarrow emitting a photon, or energy transferred to an electron \rightarrow excited or ionized of an Auger electron

- Collisional ionization

- Cosmic Ray Ionization

non-thermal electrons and ions



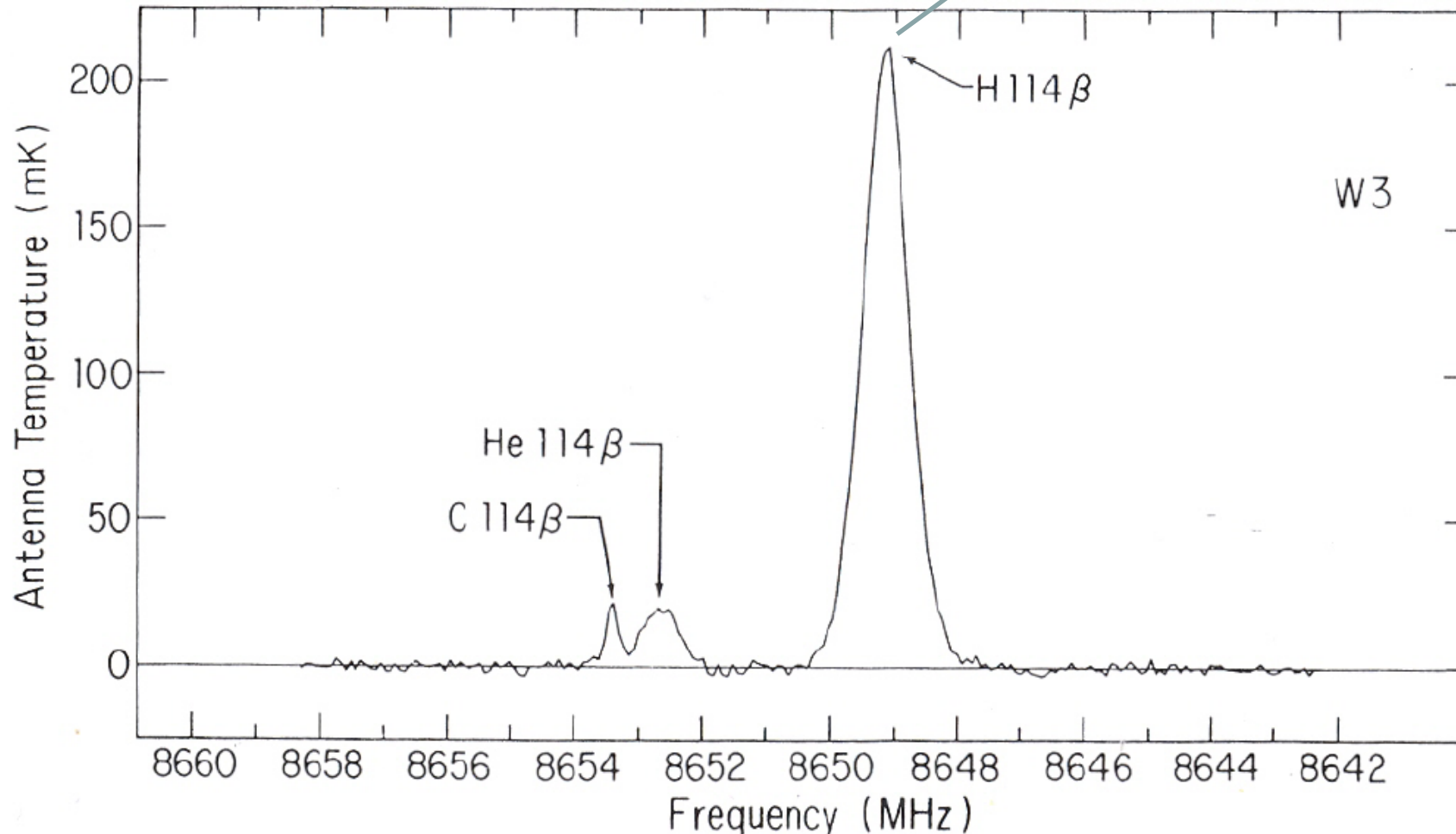
https://en.wikipedia.org/wiki/Auger_effect

Auger-Meitner effect:
1922 by Lise Meitner:
1923 by Pierre Victor Auger

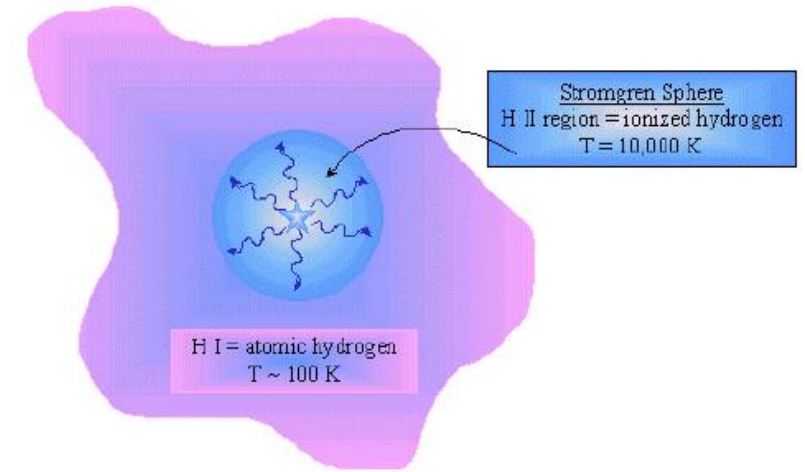
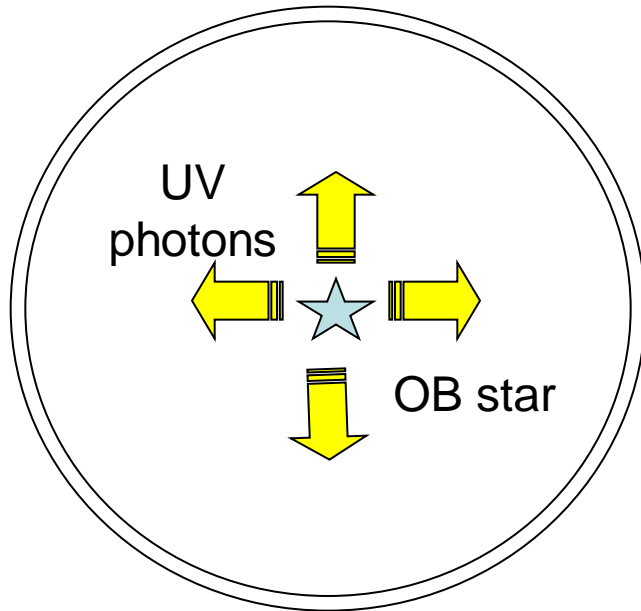
Recombination \rightarrow photons

Some of the photons can also
ionize or excite other species

H 114 β : $n = 116 \rightarrow 114$



H II Regions of Photoionization



Radiation $\lambda < 912 \text{ \AA}$
→ ionization of H from gr state

If e^- already in an excited state, a longer λ will do.

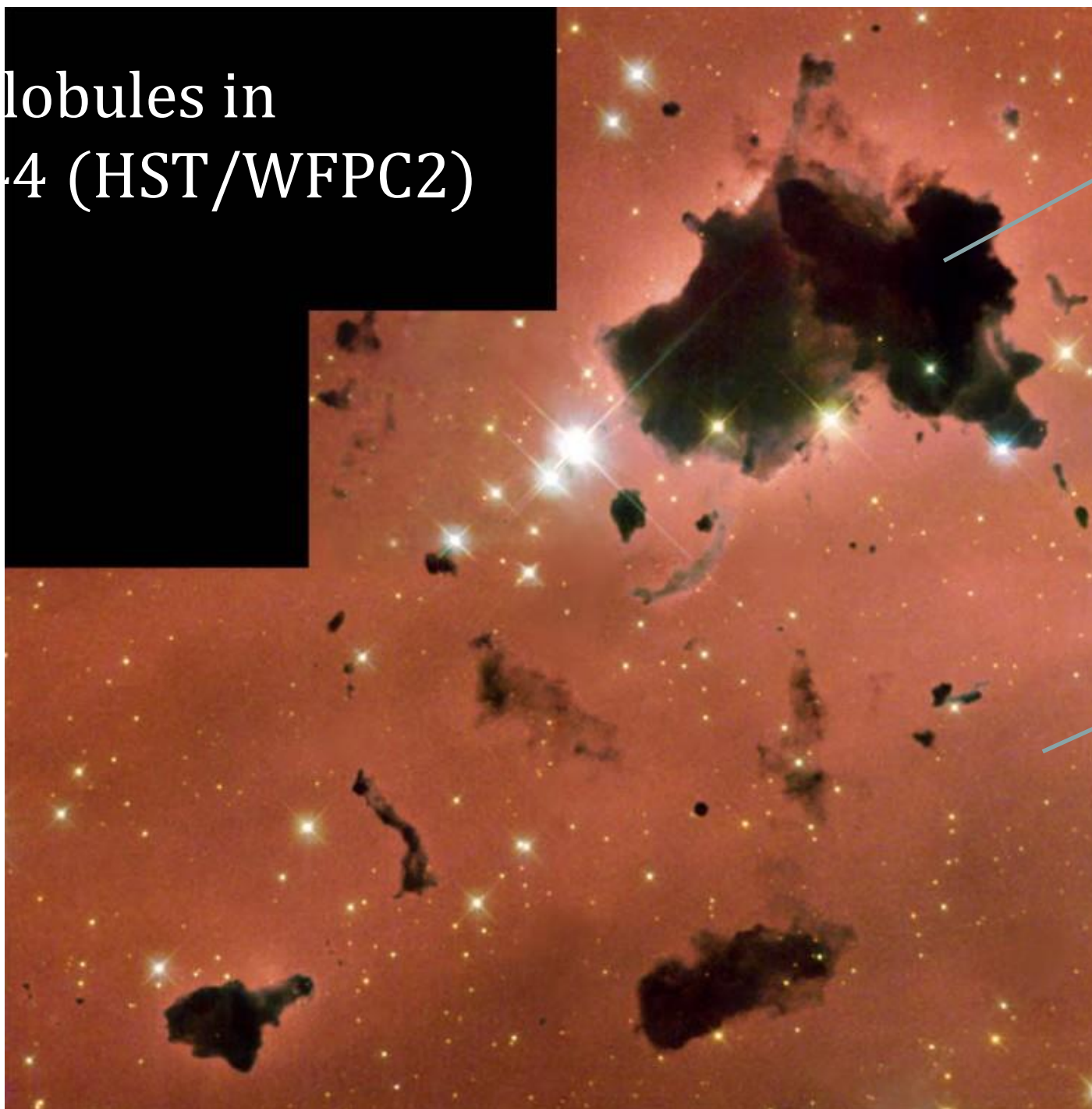
Collisional ionization negligible in HII regions

Once ionized, the e^- recombines with a p^+ , emitting Balmer, Paschen, Pfund lines or continua

→ e^- cascading → we see H α 656.3 nm



lobules in
4 (HST/WFPC2)



Dark cloud

Ionized hydrogen

**Trifid Nebula
(M20)
(H II)**



Ring Nebula (M57) (PN)

Blue: He
Green: O
Red: N
WD 120,000 K

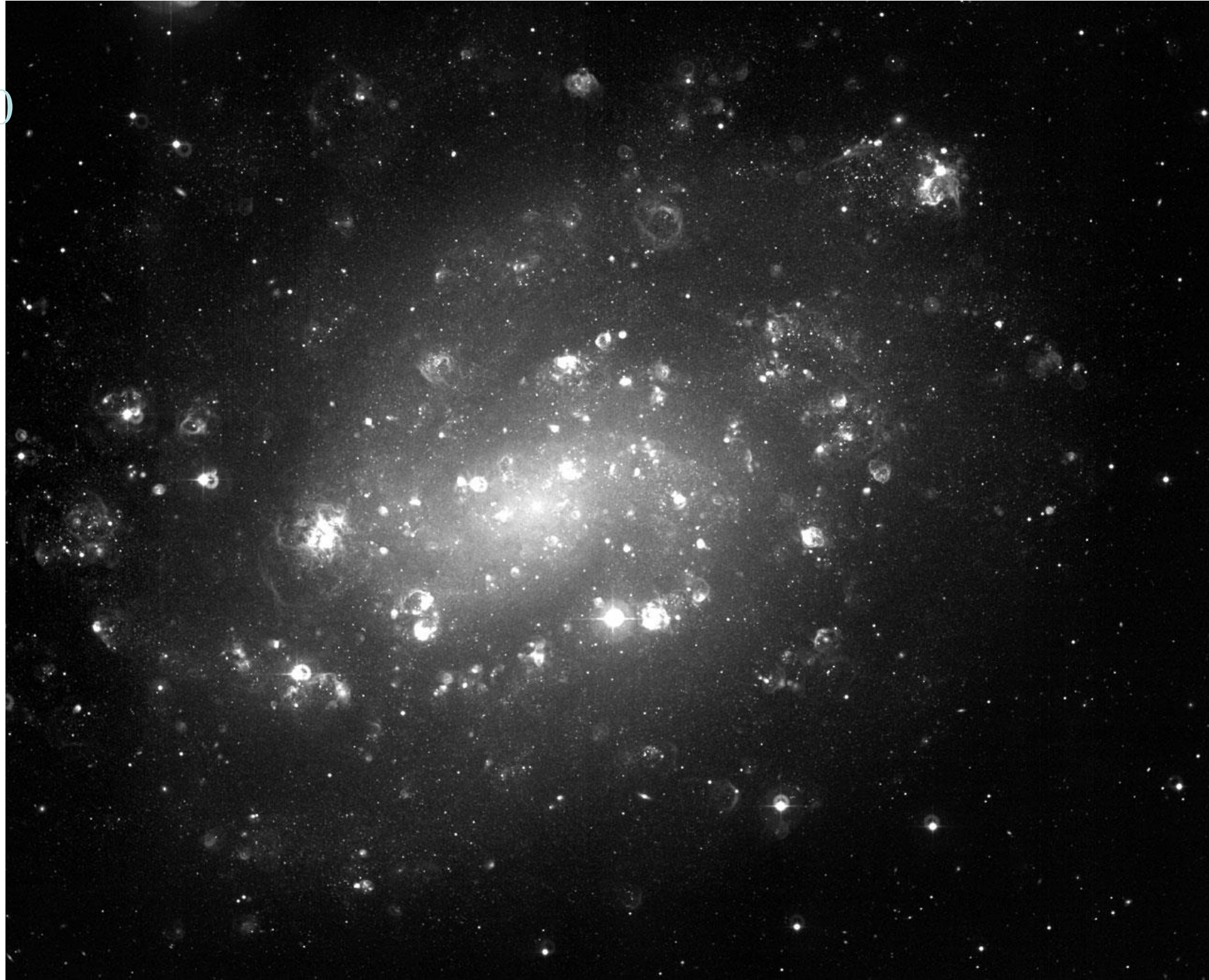


Helix Nebula (NGC 7293) (PN)

Photoionized cometary knots



Spiral galaxy NGC 300
in H-alpha (ESO)



M51 (HST)



Strings of red H II “knots” delineate the arms of the Whirlpool Galaxy: sites of recent star formation

Strömgren Sphere

The region within which every H atom is photoionized by a UV-rich object (e.g., an OB star, a WD),

[*number of ionizing photons per s*] by the star
 = [*Total number of recombinations per s*] of the nebula

$$R_s = \left(\frac{3L_{912}^*}{4\pi\alpha^{(2)}n_H^2} \right)^{1/3}$$

the Strömgren radius

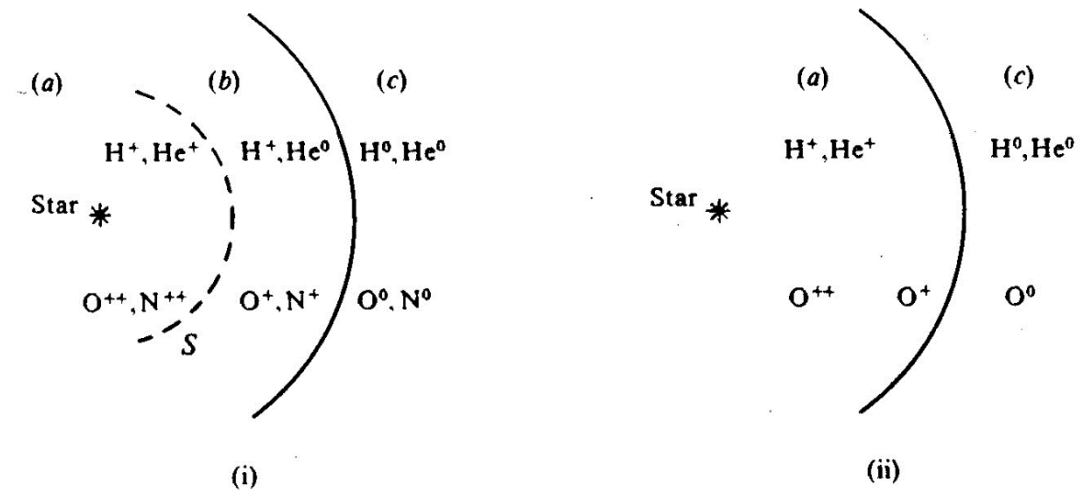


Figure 5.3. Ionization stratification in a nebula. (i) Low stellar temperature ($T_* \leq 40\,000$ K); (ii) High stellar temperature ($T_* \geq 40\,000$ K).

He and C, too

Table 2.3

Calculated Strömgren radii as function of spectral types spheres

Spectral type	T_* (K)	M_V	$\log Q(\text{H}^0)$ (photons/s)	$\log n_e n_p r_1^3$ n in cm^{-3} ; r_1 in pc	$\log n_e n_p r_1^3$ n in cm^{-3} ; r_1 in pc	r_1 (pc) $n_e = n_p$ $= 1 \text{ cm}^{-3}$
O3 V	51,200	−5.78	49.87	49.18	6.26	122
O4 V	48,700	−5.55	49.70	48.99	6.09	107
O4.5 V	47,400	−5.44	49.61	48.90	6.00	100
O5 V	46,100	−5.33	49.53	48.81	5.92	94
O5.5 V	44,800	−5.22	49.43	48.72	5.82	87
O6 V	43,600	−5.11	49.34	48.61	5.73	81
O6.5 V	42,300	−4.99	49.23	48.49	5.62	75
O7 V	41,000	−4.88	49.12	48.34	5.51	69
O7.5 V	39,700	−4.77	49.00	48.16	5.39	63
O8 V	38,400	−4.66	48.87	47.92	5.26	57
O8.5 V	37,200	−4.55	48.72	47.63	5.11	51
O9 V	35,900	−4.43	48.56	47.25	4.95	45
O9.5 V	34,600	−4.32	48.38	46.77	4.77	39
B0 V	33,300	−4.21	48.16	46.23	4.55	33
B0.5 V	32,000	−4.10	47.90	45.69	4.29	27
O3 III	50,960	−6.09	49.99	49.30	6.38	134
B0.5 III	30,200	−5.31	48.27	45.86	4.66	36
O3 Ia	50,700	−6.4	50.11	49.41	6.50	147
O9.5 Ia	31,200	−6.5	49.17	47.17	5.56	71

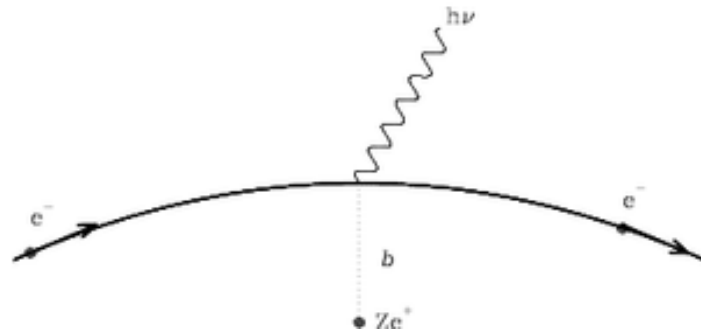
Note: $T = 7,500$ K assumed for calculating α_B .

Evolution of an H II region

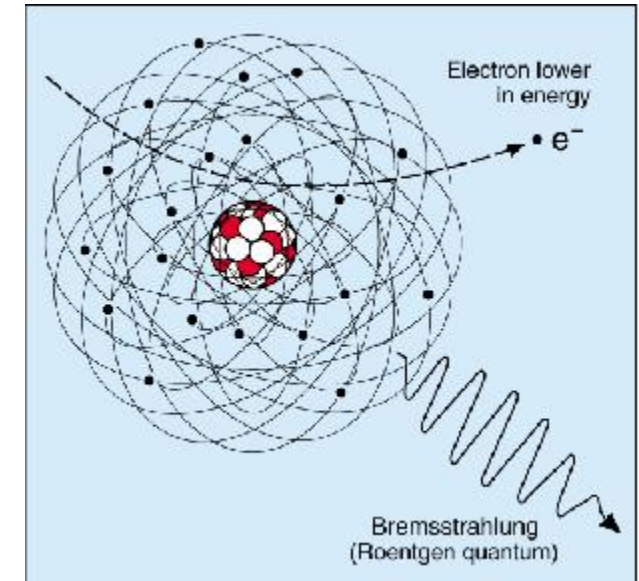
- Original H I, $T \sim 100$ K; now H II, $T \nearrow \nearrow$ ($\sim 10^4$ K), ionization produces free electrons, so $n \nearrow$, hence pressure ($P \propto nT$) $\nearrow \nearrow$
→ H II region expands, $v \sim$ sound speed of the hot gas ~ 10 km/s
- Sound speed in H I ~ 1 km/s → H II expansion highly supersonic
→ a shock (ionization) front
- H II continues to expand ($n \searrow$) until in pressure equilibrium with the H I region. This takes 10^7 to 10^8 years.
But an early O star has a main-sequence lifetime of 10^6 years.
→ H II regions are expanding!
- A **compact** H II region = young; newly formed H II regions = **ultra-compact** H II (UCHII) regions ($D < 0.3$ pc);
hyper-compact H II regions → massive star formation

Thermal (Bremsstrahlung; free-free) Emission

Hot, low-density plasma (e.g., HII regions, PNe, SNRs)
→ thermal radio emission



<http://www.astro.utu.fi/~cflynn/>



c.f. Synchrotron
Radiation



Emission line observations suggest nebula $T_e \approx 10^4$ K, so in radio wavelengths, $h\nu \ll kT$, $e^{-h\nu/kT} \rightarrow 1$ (flat), and $B_\nu \approx 2k T\nu^2/c^2$

For free-free emission or bremsstrahlung (braking radiation)

$$j_\nu \approx \frac{n_e n_i}{T_e^{1/2}} \Rightarrow \kappa_\nu = \frac{j_\nu}{B_\nu} \approx \frac{n_e n_i}{T_e^{3/2} \nu^2}$$

More rigorously, the optical depth

$$\tau = \int \kappa_\nu ds = \frac{8.235 \times 10^{-2}}{T_e^{1.35} \nu_{\text{GHz}}^{2.1}} \text{ EM},$$

Bright HII regions
 $n_e \approx n_p \approx 10^3 \text{ cm}^{-3}$
over $\Delta s \approx 1 \text{ pc}$
 $\rightarrow \text{EM} \approx 10^6 \text{ cm}^{-6} \text{ pc}$

where $\text{EM} = \int n_e n_i ds [\text{cm}^{-6} \text{ pc}]$ is the **emission measure**.

$\tau \searrow$ at higher ν (or long λ)

\rightarrow Plasma is more transparent at higher frequencies.

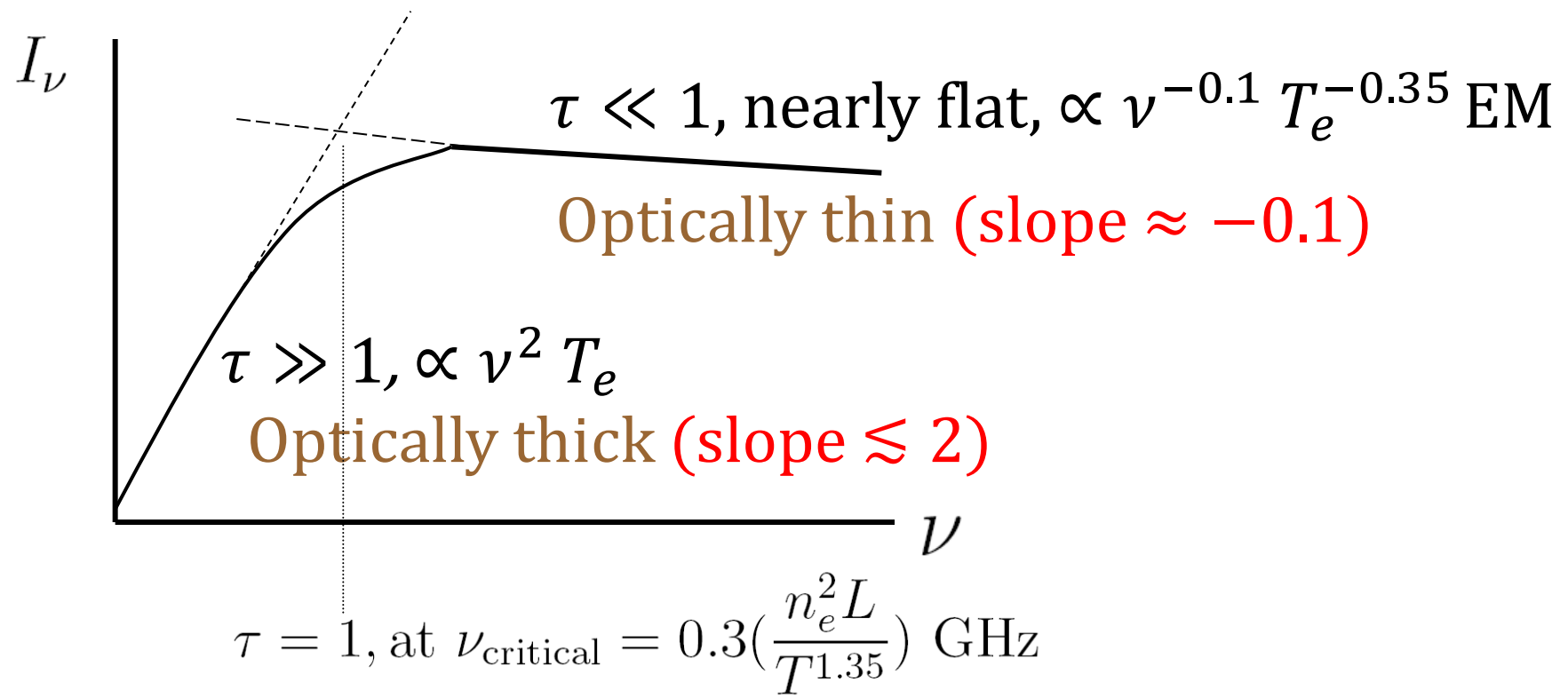
Recall $\tau = \int \kappa_\nu ds \propto \frac{EM}{T_e^{1.5} \nu^2}$

✓ At high frequencies, $\tau \ll 1$,

$$I_\nu = B_\nu \tau \propto \frac{2kT\nu^2}{c^2} \frac{EM}{T^{3/2}\nu^2} \propto \frac{EM}{T^{1/2}} \quad \longleftrightarrow \nu$$

✓ At low frequencies, $\tau \gg 1$,

$$I_\nu = B_\nu = \frac{2kT\nu^2}{c^2} \quad \text{Blackbody} \quad \longleftrightarrow n_e$$



Observations at $\tau \gg 1$, get T
 Observations at $\tau \ll 1$, get n_e

Advantages of radio observations: less extinction;
 measures T directly at low freq.

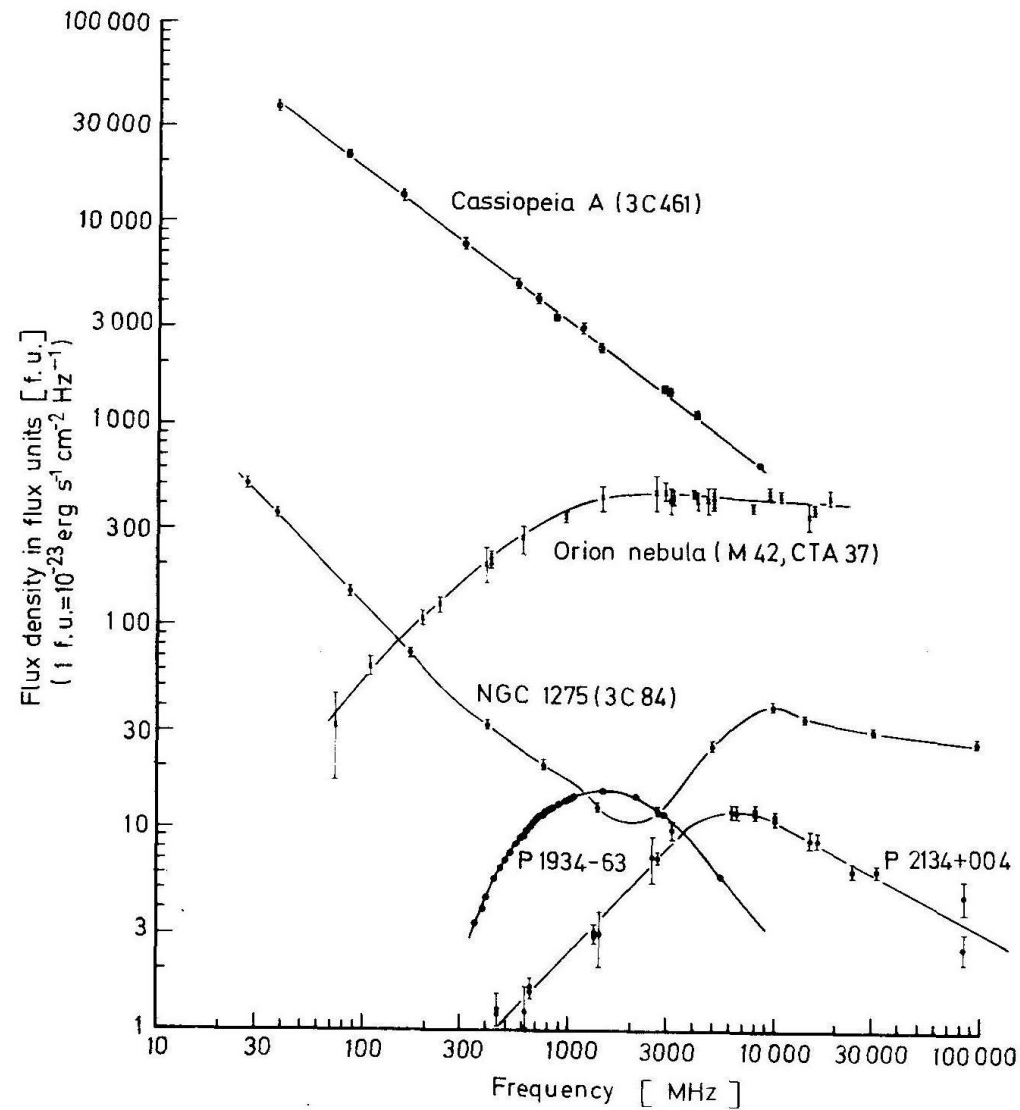
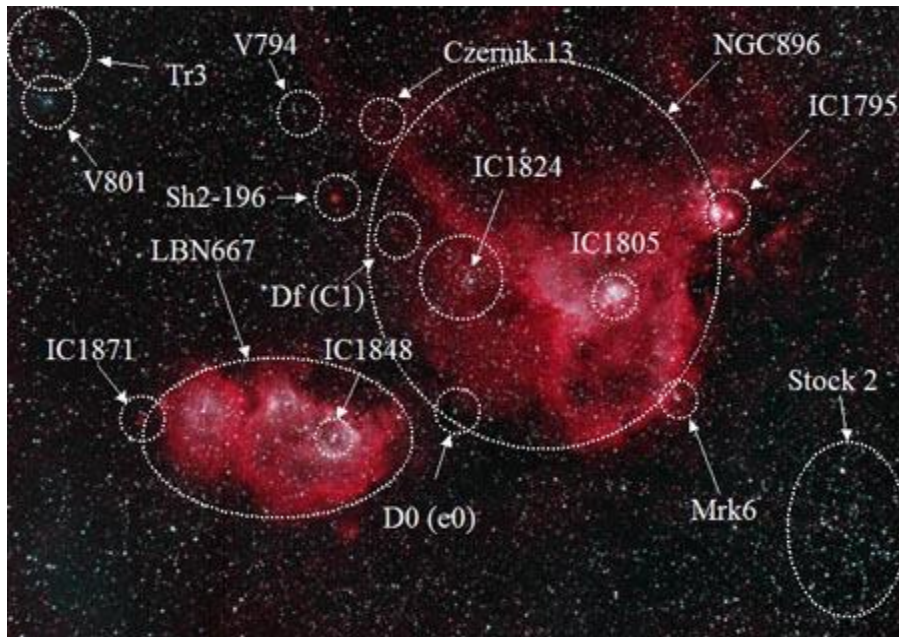
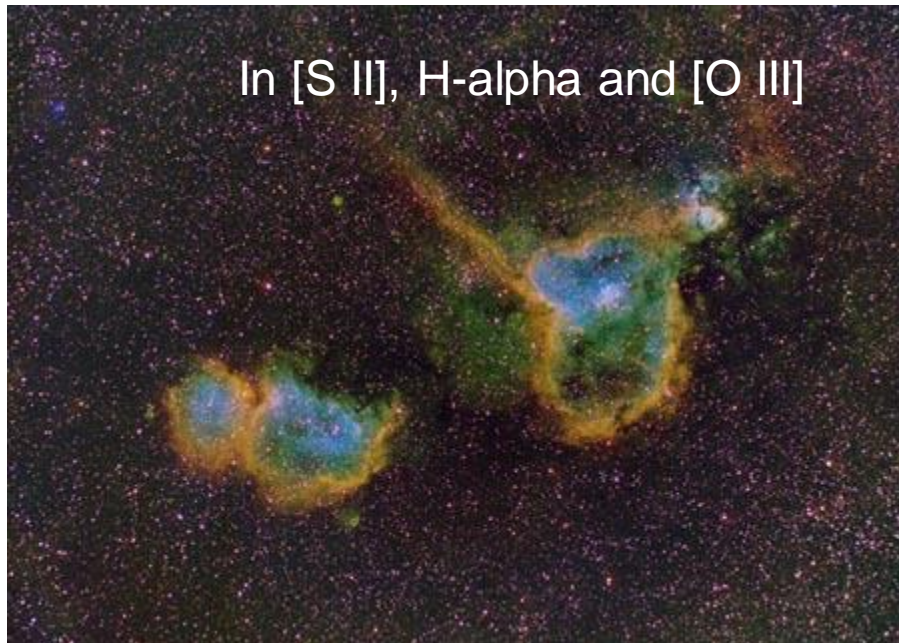
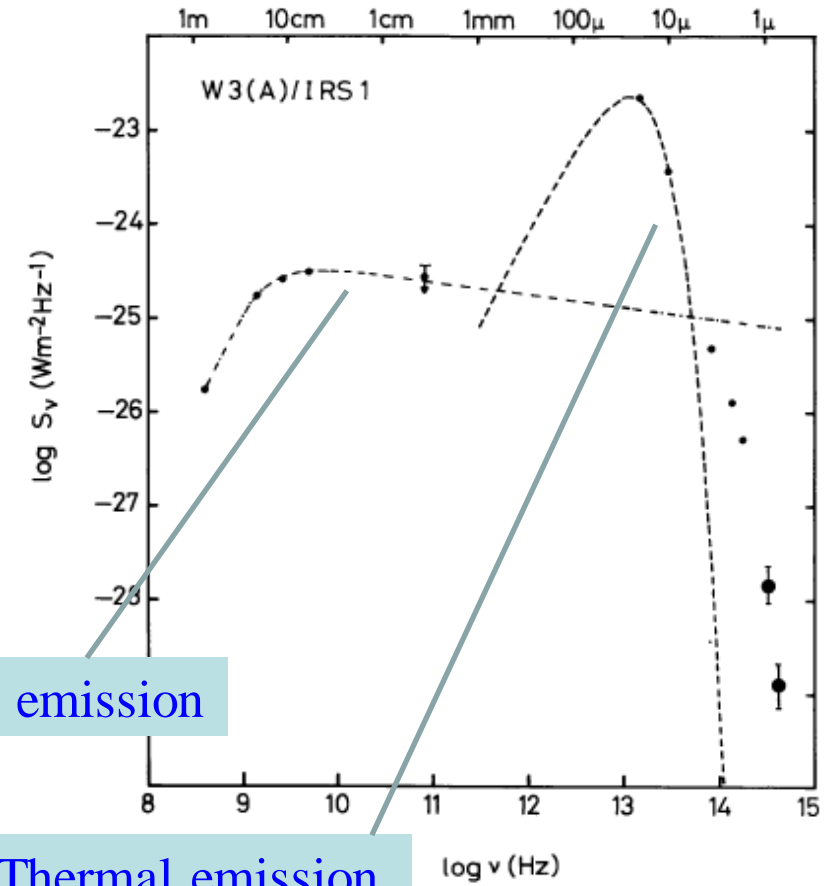


Fig. 4. Radiofrequency spectra of sources exhibiting the power law spectrum of synchrotron radiation (Cassiopeia A), the flat spectrum of thermal bremsstrahlung radiation with low frequency self absorption (Orion Nebula), unusual high frequency radiation (NGC 1275), and low frequency absorption processes (P 1934-63 and P 2134+004). The data for P 2134+004 are from E. K. CONKLIN, and the other data are from KELLERMANN (1966), HJELLMING, and CHURCHWELL (1969), TERZIAN and PARRISH (1970), KELLERMANN, PAULINY-TOTH, and WILLIAMS (1969), and KELLERMANN *et al.* (1971)



W3= IC 1795

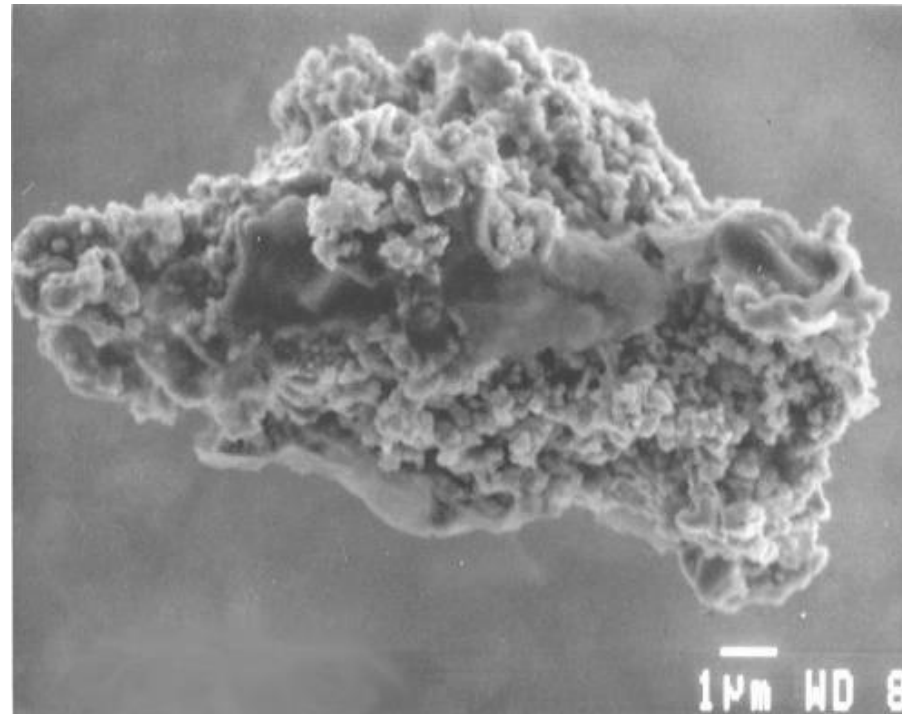
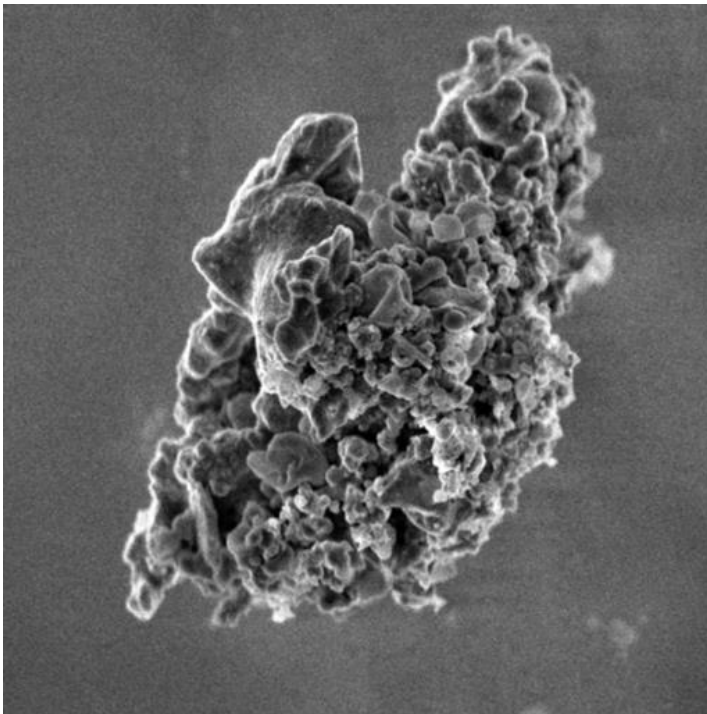


(Gas) Thermal emission

(Dust) Thermal emission

Fig. 2. Energy distribution of IRS 1 according to Wynn-Williams *et al.* (•) together with flux densities in *I* and *R* (●). Dashed lines: Predicted free-free emission from ionized hydrogen and thermal infrared radiation of dust, represented by Planck-curve with temperature $T = 200 \text{ K}$

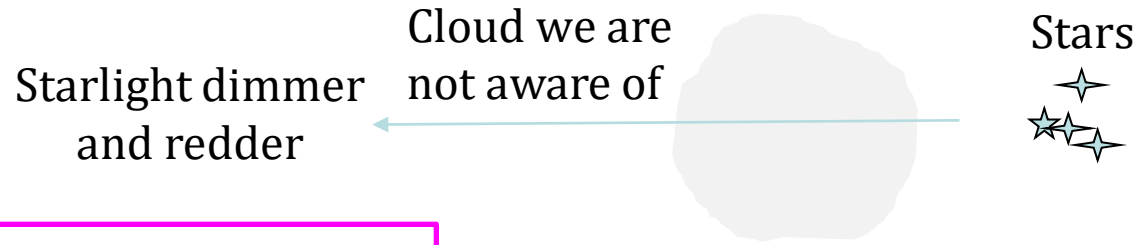
ISM Solid State (dust grains)



Grains appear to be loose (porous) conglomerations of smaller specks of material; stick together to grow in size.

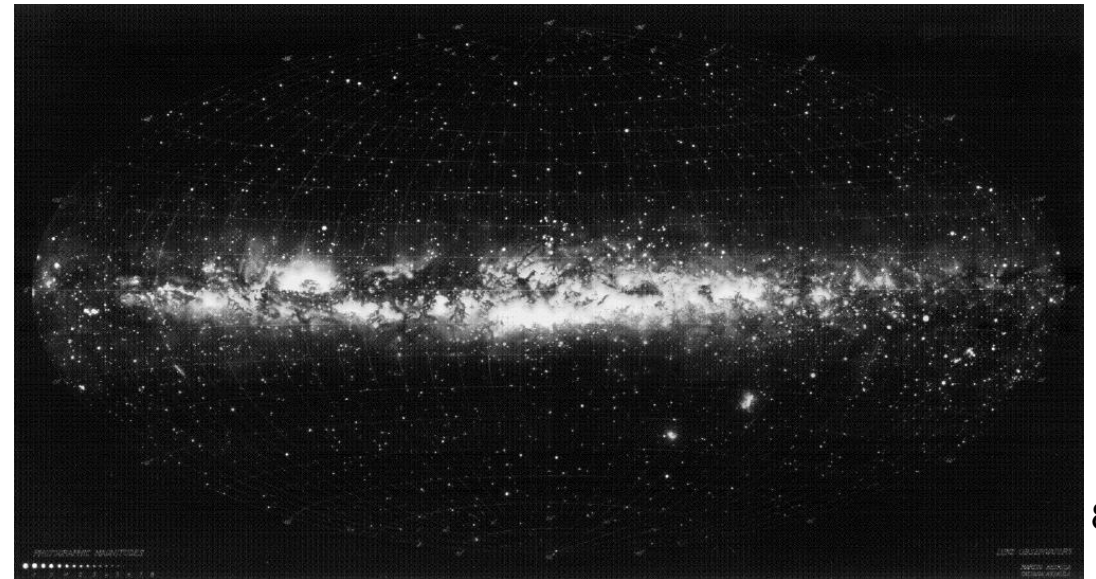
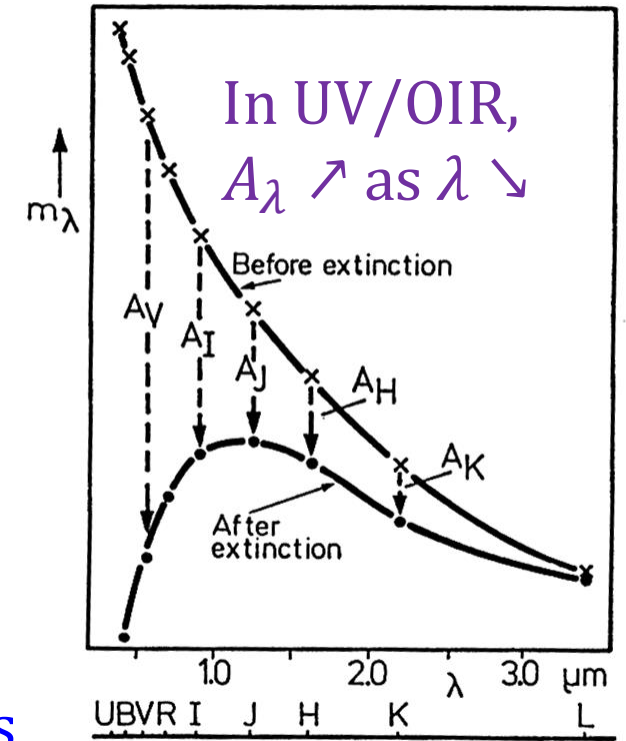
Interstellar Extinction

$$\langle \text{Extinction} \rangle = \langle \text{Absorption} \rangle + \langle \text{Scattering} \rangle$$



$$m_{\lambda} - M_{\lambda} = 5 \log r_{pc} - 5 + A_{\lambda}$$

Extinction severe in UV;
much less in IR and X-rays



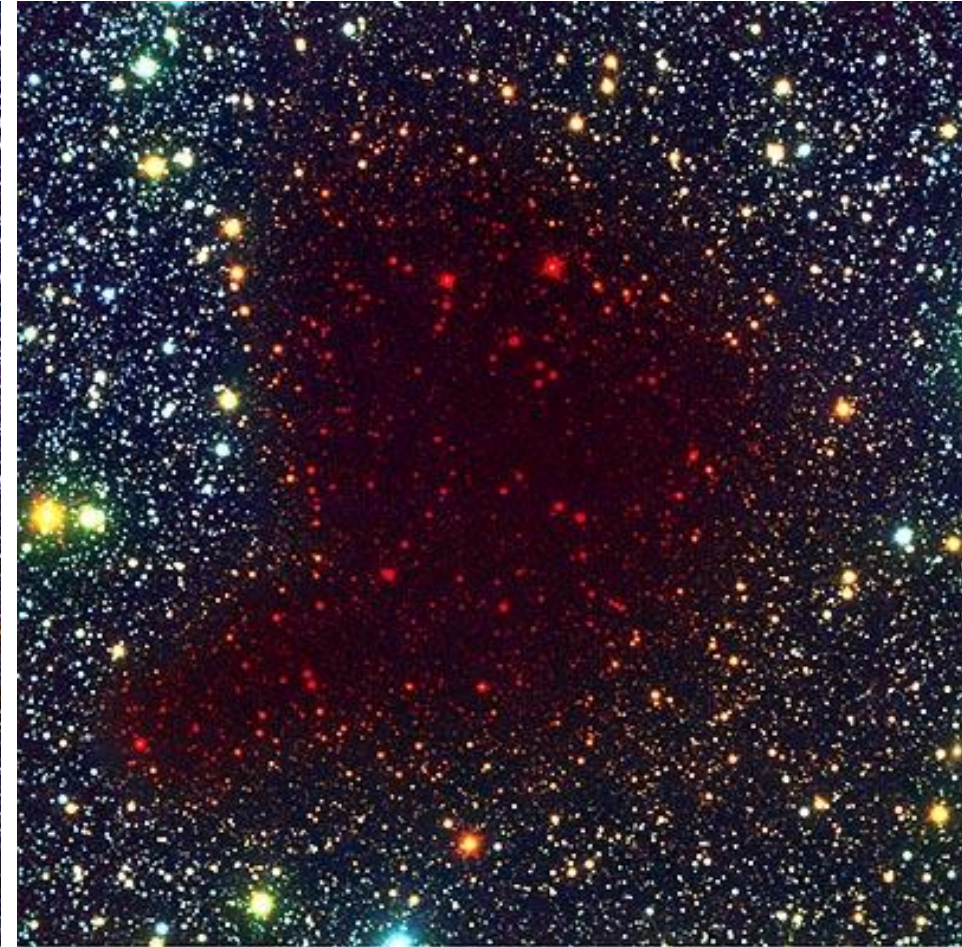
Background IR light shines through ...



Pre-Collapse Black Cloud B68 (visual view)
(VLT ANTU + FORS 1)

ESO PR Photo 02a/01 (10 January 2001)

© European Southern Observatory



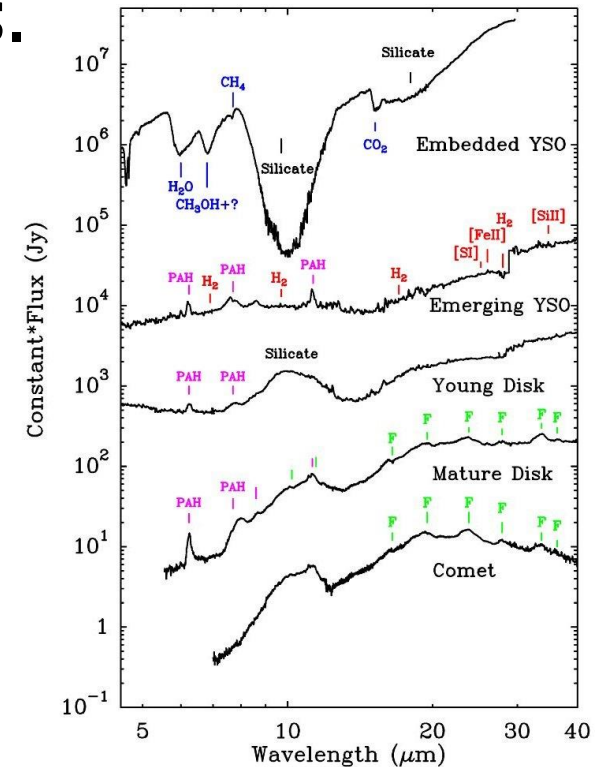
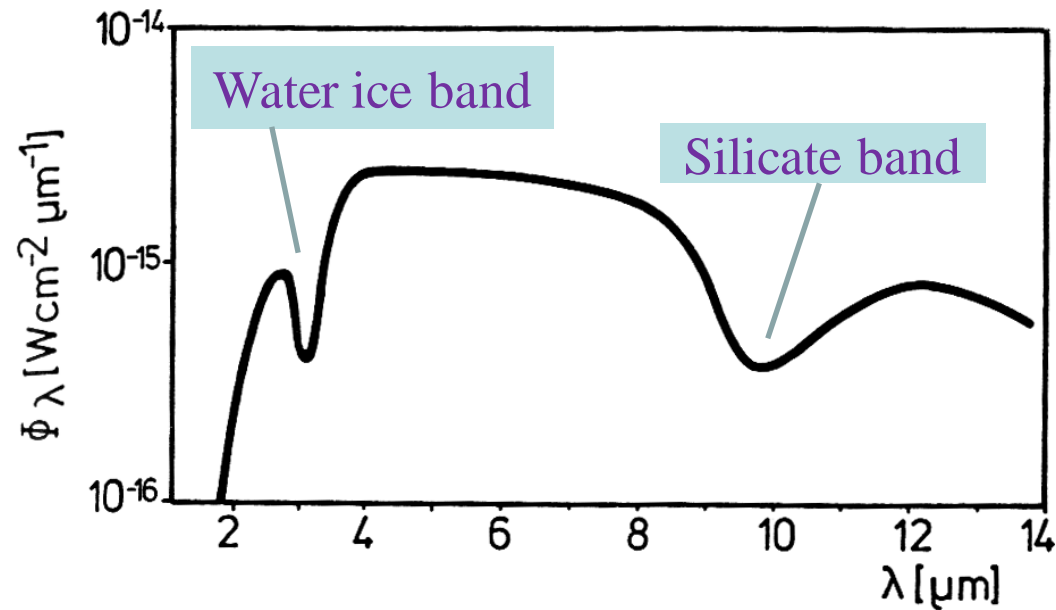
Seeing Through the Pre-Collapse Black Cloud B68
(VLT ANTU + FORS 1 - NTT + SOFI)

ESO PR Photo 02b/01 (10 January 2001)

© European Southern Observatory



- ❑ Dust affects our view therefore our study of celestial objects.
- ❑ Dust serves as the seed of grain growth toward planet formation.
- ❑ It is vital in cosmic energy budget (emissions from thermalized dust at long wavelengths easily escape).
- ❑ It exists in ISM (particular in cold clouds), and in cool (stellar, substellar, and planetary) atmospheres.



Scattering

Size of particles a

□ $2\pi a \ll \lambda \Rightarrow \text{scattering} \leftrightarrow \lambda$

$$I_{\text{scattering}} \propto \lambda^{-4} \text{ (Rayleigh scattering)}$$

This is why a clear sky is blue.

□ $2\pi a \gg \lambda \Rightarrow \text{scattering} \nleftrightarrow \lambda$ (cross section \sim geometric)

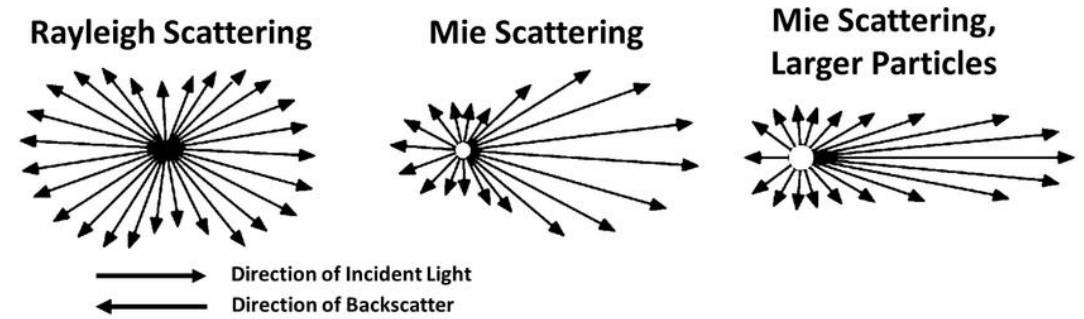
$$I_{\text{scattering}} \propto \lambda^0$$

This is why a cloudy sky is gray.

□ $2\pi a \approx \lambda$ (dust $\bar{a} = 0.3 \mu\text{m}$; λ in UV/visible)

$$I_{\text{scattering}} \propto \lambda^{-1}$$

This is interstellar reddening --- why distant/embedded stars are reddened (interstellar reddening).



Usually a size distribution, e.g., a power law, $n(a) \propto a^{-\beta}$

Gas and dust

In H I regions, $N(x)/N(H)$ depleted relative to atmospheres of Pop I stars $T_c \uparrow \rightarrow \text{condensed first} \rightarrow \text{depletion} \uparrow$

At $T \nearrow \nearrow$, grains evaporated.

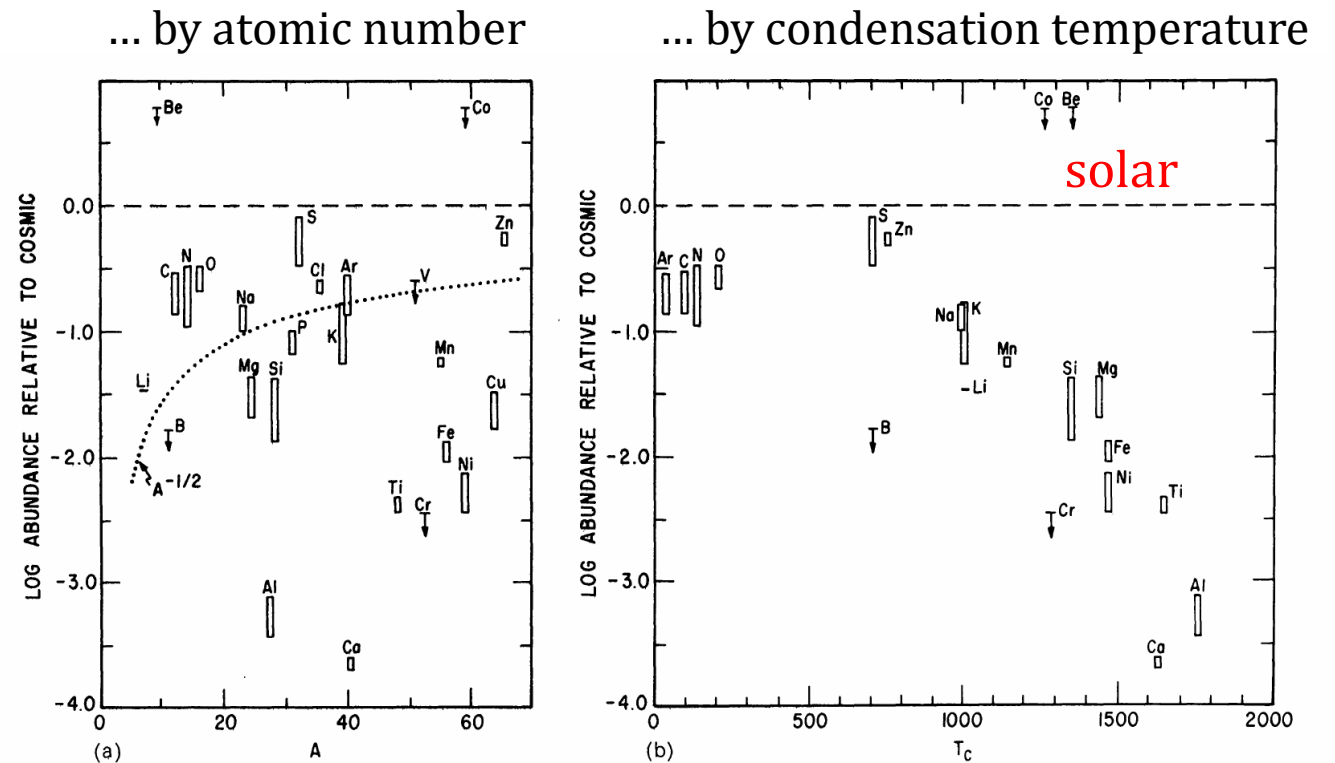


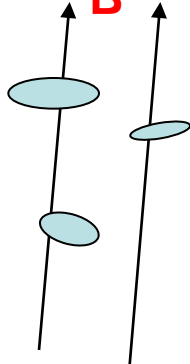
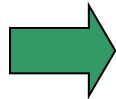
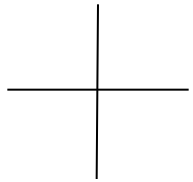
Figure 5 Depletion below solar abundances for elements in their atomic form in the H I gas toward ζ Oph, plotted against atomic mass A in (a) and condensation temperature T_c in (b). The vertical width of each bar represents the experimental error arising from uncertainties in the respective element's curve of growth. For grains and atoms of a given charge, the nonequilibrium accretion rate in cool interstellar clouds should be proportional to $A^{-1/2}$, illustrated by the dotted line in (a). All elements shown here except N, O, and Ar should be predominantly ionized in H I regions.

Polarized Starlight

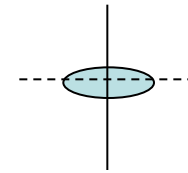
Magnetic field in the ISM first discerned by linearly polarized starlight ($\sim 1\%$) (Hiltner 1949 and Hall 1949)

It is thought that the partial polarization of starlight is produced by elongated dust grains aligned by magnetic fields in the ISM

Unpolarized starlight



Grains preferentially spin with the minor axes $\parallel \vec{B}$

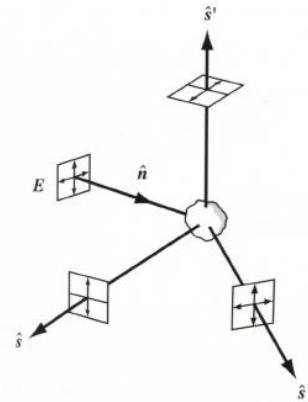


Polarized starlight observed

$$\vec{P} \parallel \vec{B}$$

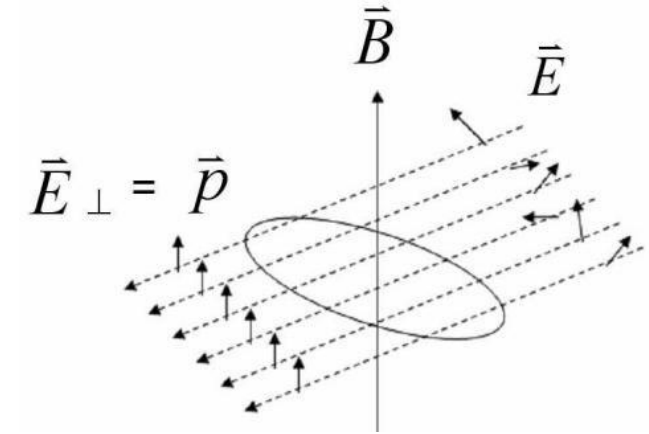
<http://bgandersson.net/grain-alignment>

Observations in FIR to mm

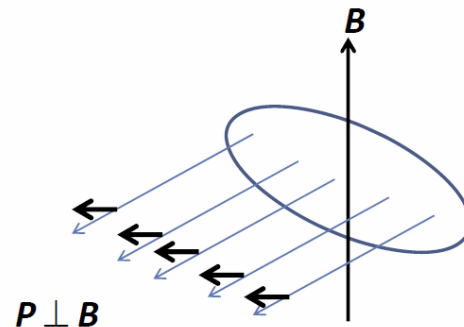


Scattering by dust

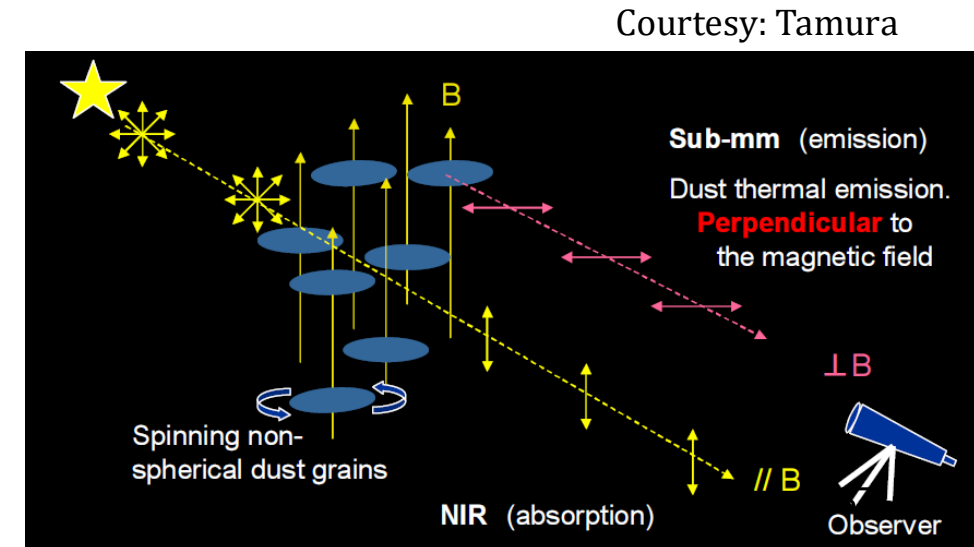
Stahler & Pallo 2004

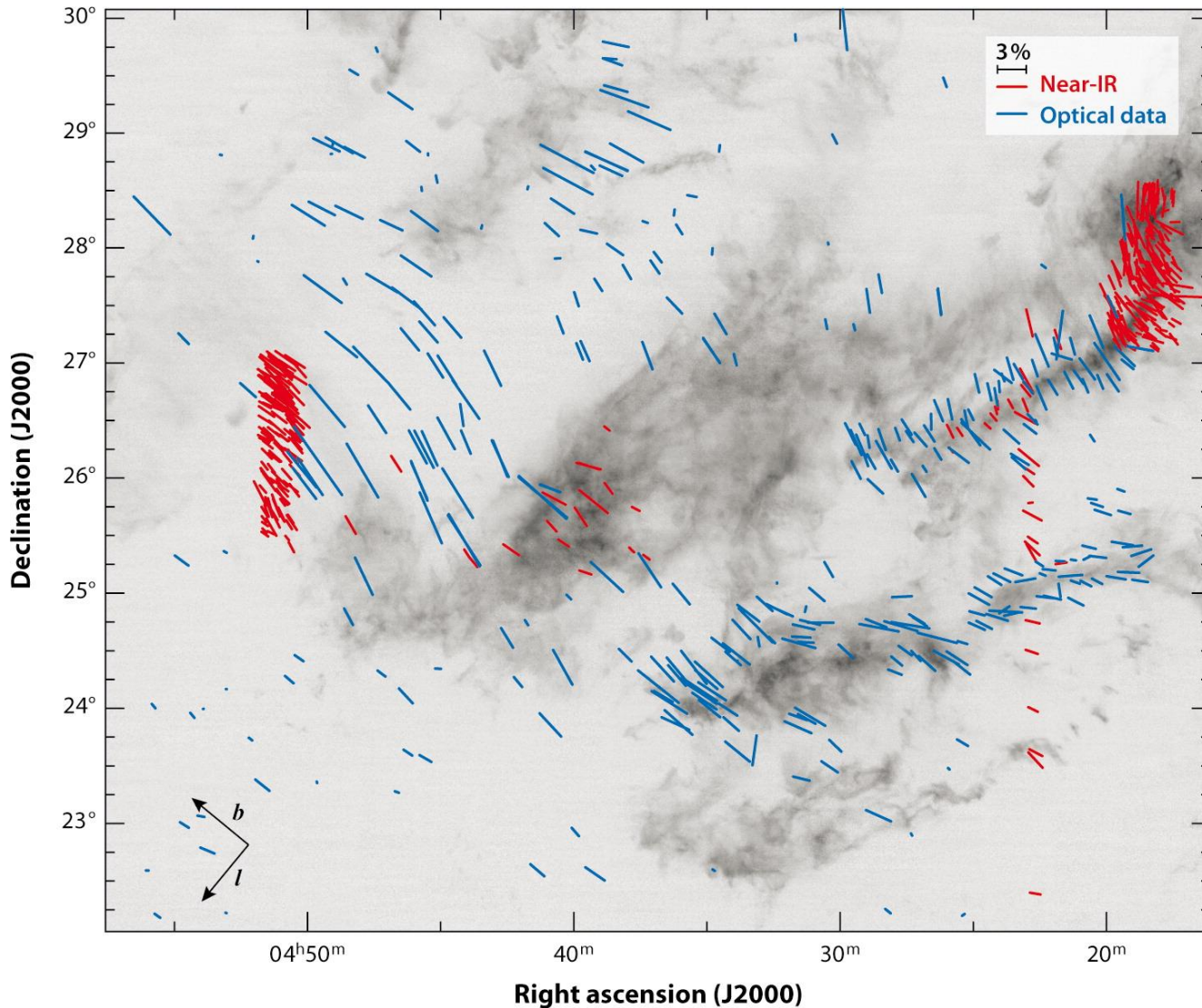


Dichroic extinction by aligned dust



*Polarized thermal emission by
dust aligned by \mathbf{B}*





Organized magnetic field morphology in the Taurus dark-cloud complex superposed on a ^{13}CO map (Chapman et al. 2011). **Blue** lines show polarization measured at optical wavelengths and **red** lines show near-IR (*H*-band and *I*-band) polarization.

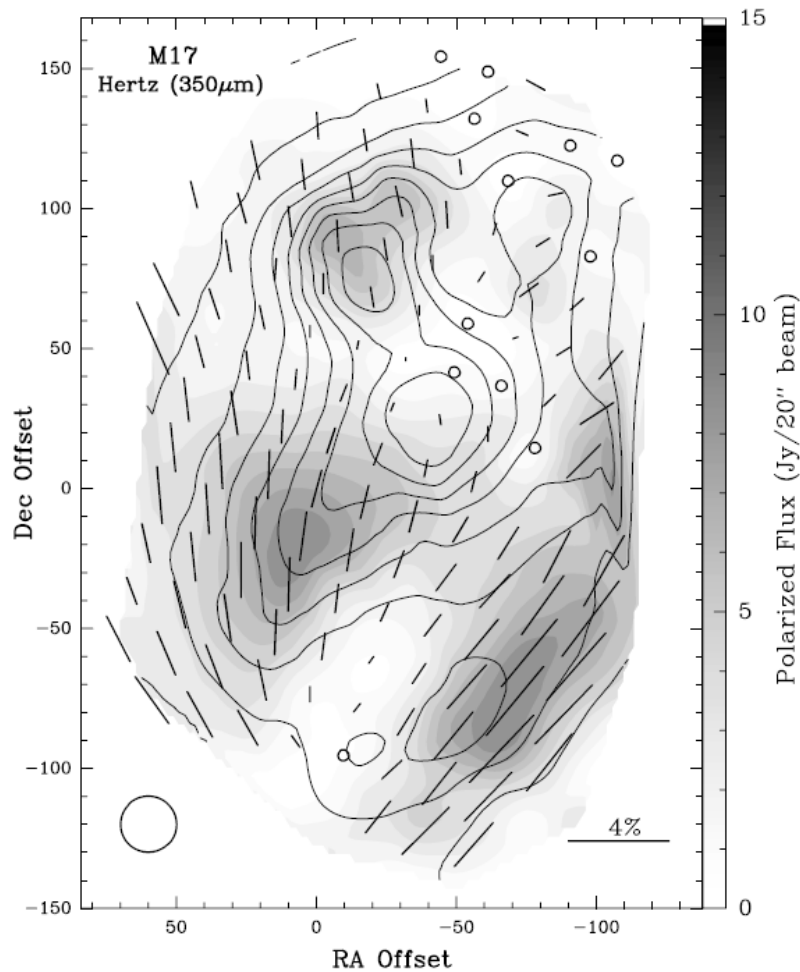


FIG. 6.—HERTZ polarization map of M17 at $350\ \mu\text{m}$. All of the polarization vectors shown have a polarization level and error such that $P > 3\sigma_p$. Circles indicate cases where $P + 2\sigma_p < 1\%$. The contours delineate the total continuum flux (from 10% to 90% with a maximum flux of ≈ 700 Jy), whereas the underlying gray scale gives the polarized flux according to the scale on the right. The beam width ($\approx 20''$) is shown in the lower left corner and the origin of the map is at R.A. = $18^{\text{h}}17^{\text{m}}31^{\text{s}}.4$, decl. = $-16^{\circ}14'25''.0$ (B1950.0).

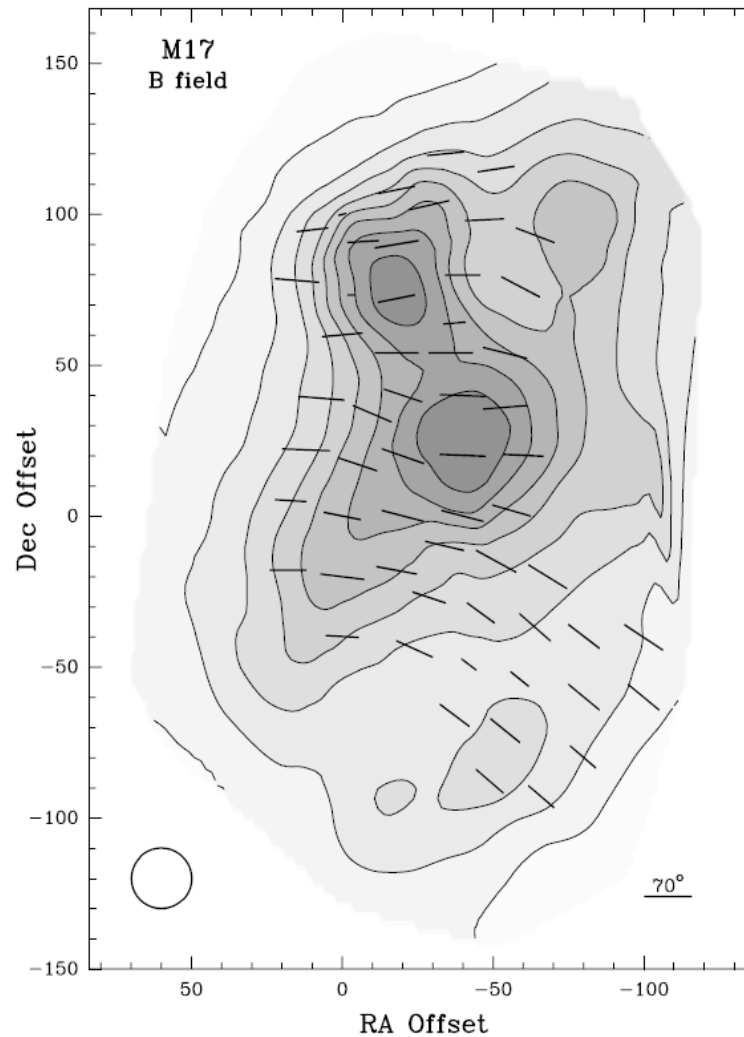


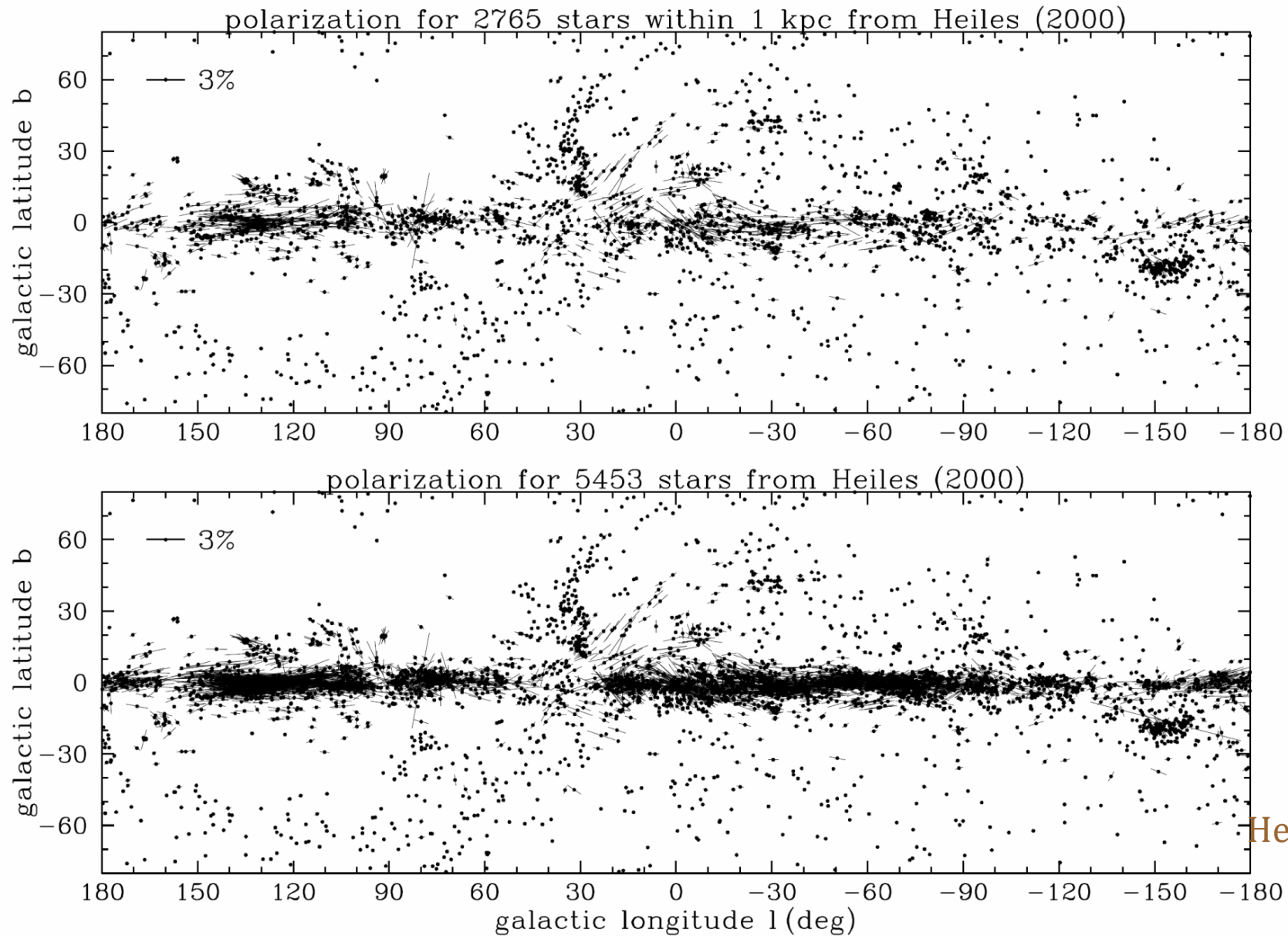
FIG. 11.—Orientation of the magnetic field in M17. The orientation of the projection of the magnetic field in the plane of the sky is shown by the vectors and the viewing angle is given by the length of the vectors (using the scale shown in the bottom right corner). The contours and the gray scale delineate the total continuum flux. The beam width ($\approx 20''$) is shown in the lower left corner, and the origin of the map is at R.A. = $18^{\text{h}}17^{\text{m}}31^{\text{s}}.4$, decl. = $-16^{\circ}14'25''.0$ (B1950.0).

Thermal emission
directly by dust (far-
IR, and smm)

$$\vec{P} \perp \vec{B}$$

Houde et al. (2002)

Polarization



Heiles (2000)

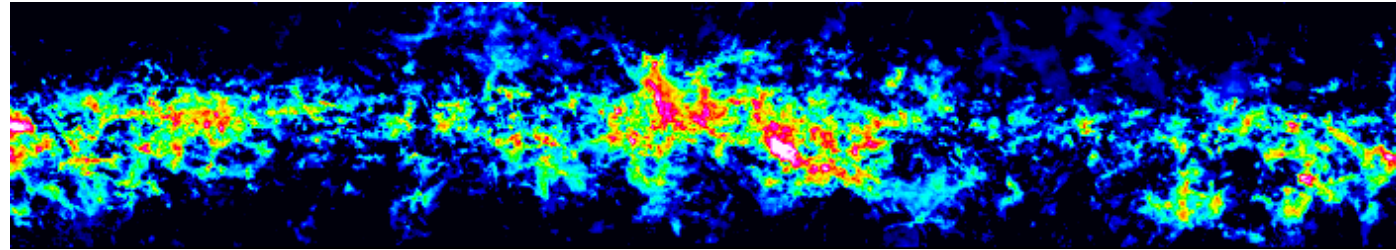
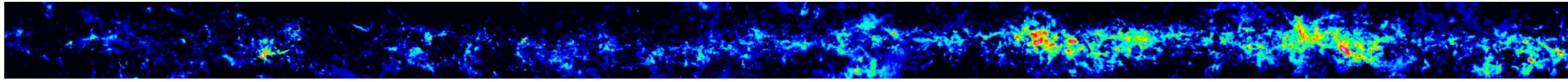
Star Formation

- Stars are formed in dense molecular cloud cores, whereas planets are formed, contemporaneously, in young circumstellar disks.

Compression of gas from a cloud size $\sim 10^{18}$ cm (parsec) down to a stellar size $\sim 10^{11}$ cm, i.e., density increase by a factor of $\sim 10^{21}$.

→ Large dynamical range in size, density, and time

Filamentary Molecular Clouds



Fractal structure

Giant Molecular Clouds

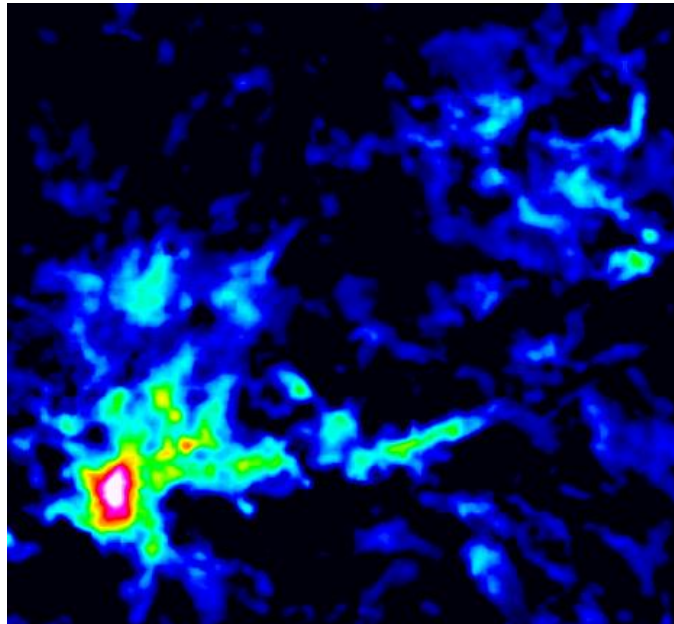
$$D = 20 - 100 \text{ pc}$$

$$\mathcal{M} = 10^5 - 10^6 \mathcal{M}_{\odot}$$

$$n \approx 10 - 300 \text{ cm}^{-3}$$

$$T \approx 10 - 30 \text{ K}$$

$$\Delta v \approx 5 - 15 \text{ km}^{-1}$$



Molecular clumps/ clouds/condensations

$$n \sim 10^3 \text{ cm}^{-3}, D \sim 5 \text{ pc},$$

$$M \sim 10^3 \mathcal{M}_{\odot}$$

Dense molecular cores

$$n \geq 10^4 \text{ cm}^{-3}, D \sim 0.1 \text{ pc},$$

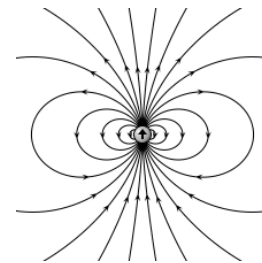
$$M \sim 1 - 2 \mathcal{M}_{\odot}$$

H₂ (dihydrogen, molecular hydrogen)

- It is the main constituent of cold clouds; not important in stars, except in the coolest substellar objects (brown dwarfs or planetary-mass objects)
- Lacking a permanent electric dipole moment, cold H₂ is very difficult to detect. A rotationally excited molecule would radiate through a relatively slow electric quadrupole transition.
- Only in a heated medium (e.g., a photodissociation PDR region between HII and a molecular cloud) where stellar radiation or stellar wind excites vibrational and electronic states which then decay relatively quickly.

$\mathcal{E}_{\text{dissociation}} = 4.48 \text{ eV}$; H – H bond

https://en.wikipedia.org/wiki/Bond-dissociation_energy



Zero electric dipole moment

CO molecules

- Simple and most abundant next to H_2
- Strong $\mathcal{E}_{\text{dissociation}} = 11.16 \text{ eV}$; $C \equiv O$, strongest bond among neutral molecules, self-shielding against stellar UV field
- with a permanent electric dipole moment; radiating strongly at radio frequencies.
- $^{12}C^{16}O$ easiest to detect; isotopes $^{13}C^{16}O$, $^{12}C^{18}O$, $^{12}C^{17}O$, $^{13}C^{18}O$ useful as diagnosing tools
- Low critical density for excitation \rightarrow CO used to study large-scale distribution of clouds, as **a tracer** of H_2 , $n(CO) \approx 10^{-4} n(H_2)$

$$n_{NH_3}^* \approx 10^3 \text{ cm}^{-3}$$

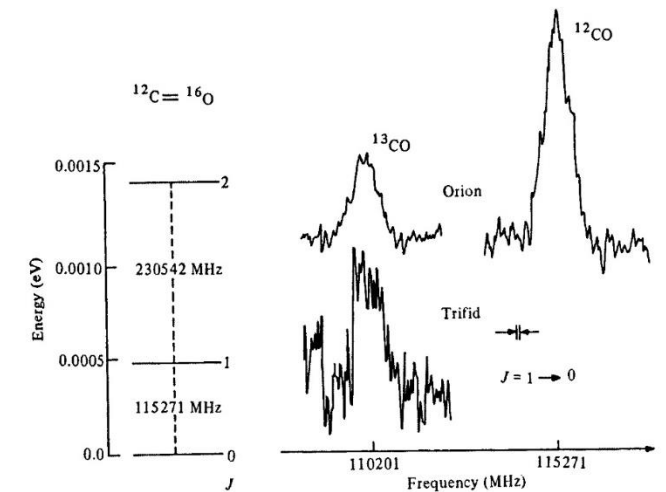
$$n_{HCN}^* \approx 10^5 \text{ cm}^{-3} \text{ (for } J = 1 \rightarrow 0 \text{)}$$

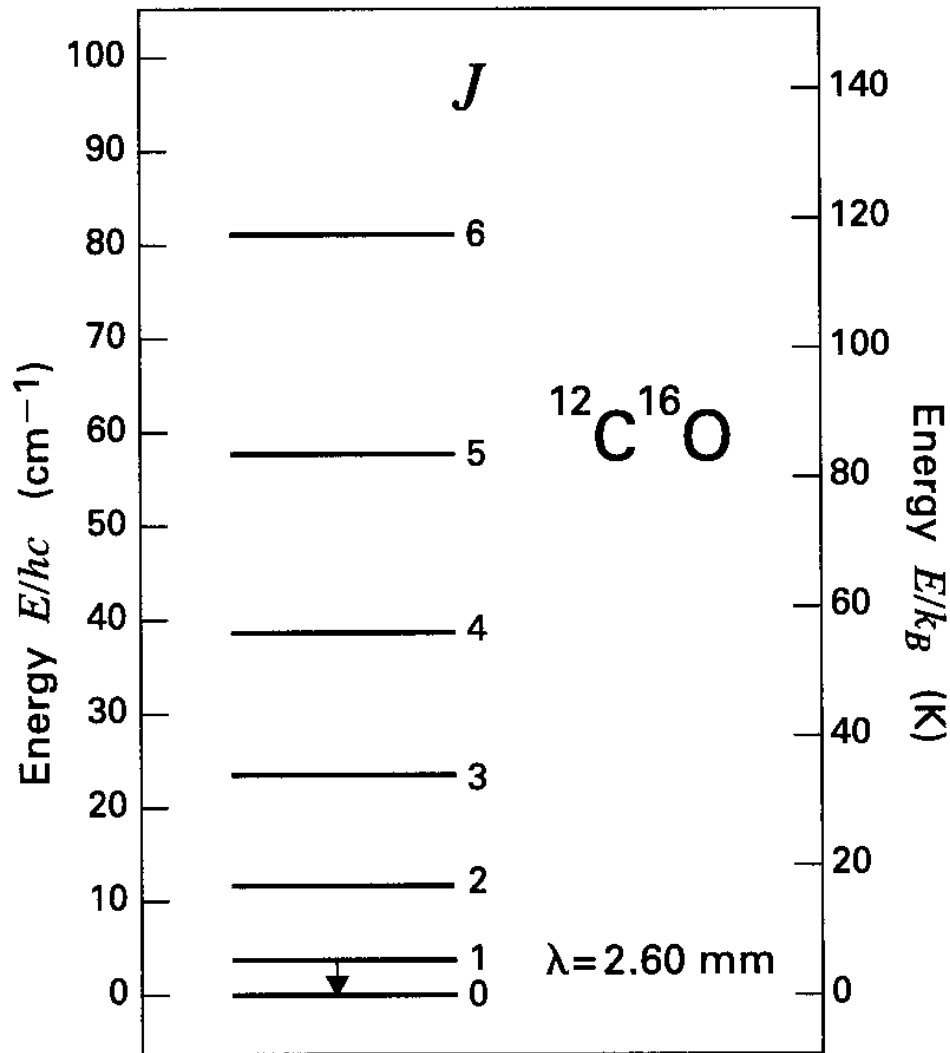
$$n(CO) \approx 10^{-4} n(H_2) \quad n(CO) \approx 10^{-4} n(H_2) \quad n(CO) \approx 10^{-4} n(H_2)$$

- $^{12}\text{C}^{16}\text{O}$ almost always **optically thick**.
so brightness temperature \approx molecular gas kinetic temperature, i.e., little dependence on column density
- Lines from rarer isotopes usually **optically thin**
→ estimate of column density (total mass) of molecular gas

$$N_H = 10^6 N_{^{13}\text{CO}}$$

Intensity ratios of optically thin lines from different J levels → excitation temperature





$$J = 1 - 0, 2.60 \text{ mm} = 115 \text{ GHz}$$

Only 5 K above the ground level ... can be excited by collisions with ambient molecules or CMB photons

$$J = 2 - 1, 1.30 \text{ mm}$$

$$J = 3 - 2, 0.87 \text{ mm}$$

$$J = 1 - 0, 2.67 \text{ mm for } ^{12}\text{C}^{17}\text{O}$$

$$2.72 \text{ mm for } ^{13}\text{C}^{16}\text{O}$$

Figure 5.6 Rotational levels of $^{12}\text{C}^{16}\text{O}$ within the ground ($v = 0$) vibrational state. The astrophysically important $J = 1 \rightarrow 0$ transition at 2.60 mm is shown.

Stars form in groups → seen as a star cluster if the group survives disintegration and remains gravitationally bound. Groups of young stellar objects are found in the dense regions of the molecular clouds (*dense molecular clouds*).

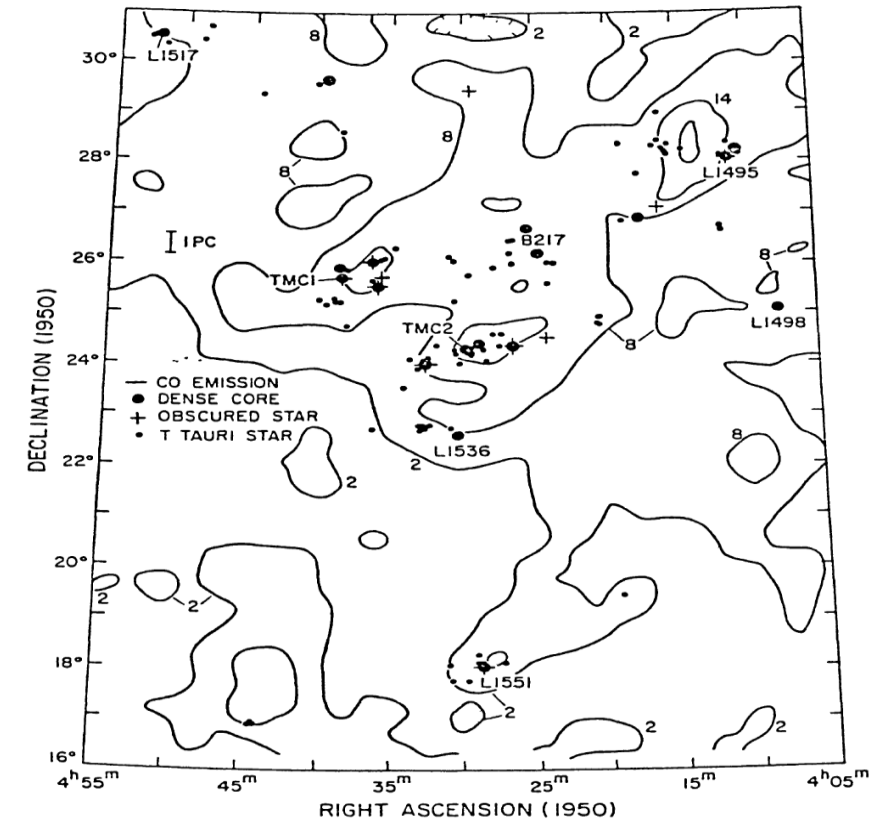
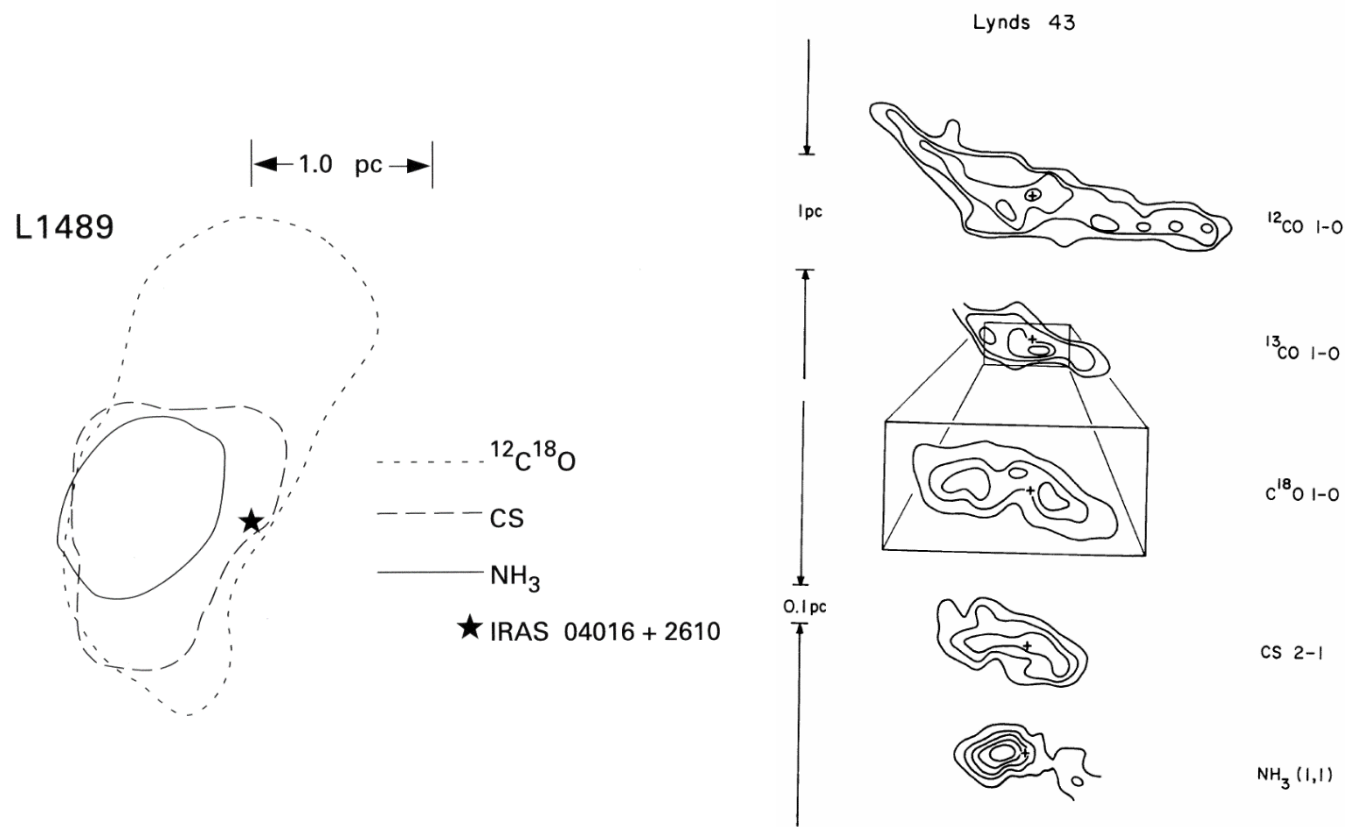


Figure 2 CO contour map of the Taurus molecular cloud with positions of dense NH_3 cores, embedded infrared sources, and visible T Tauri stars (from Myers 1986).

Molecular clouds observed by different tracers ...

Taurus molecular cloud 99

Nearby Examples

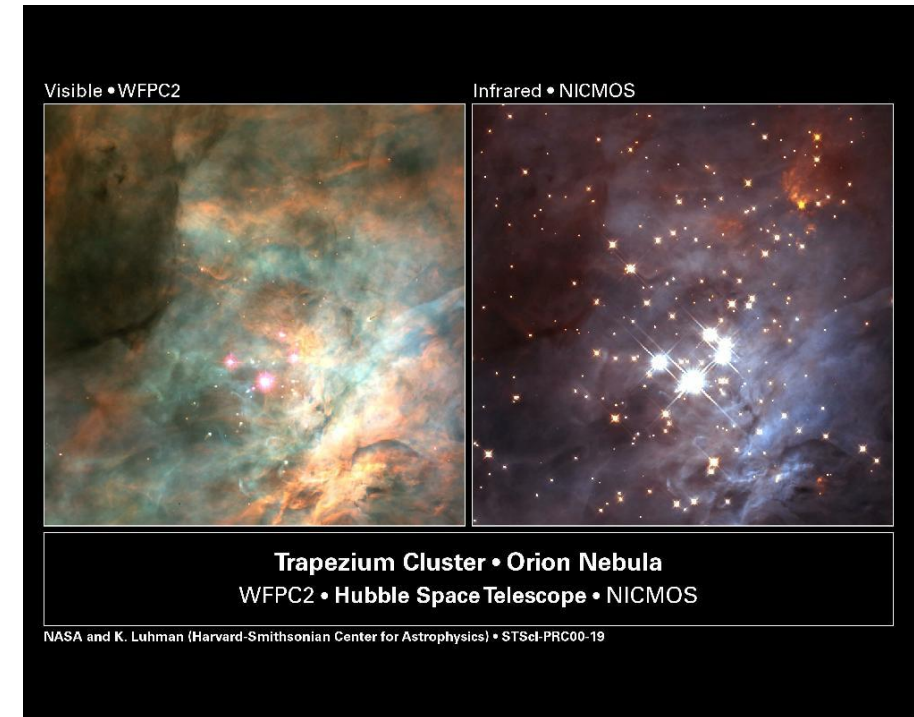
Massive Star-Forming Regions

- *Per OB2* (350 pc)
- *Orion OB Association* (350--400 pc) ... rich

Low-Mass Star-Forming Regions

- *Taurus Molecular Cloud (TMC-1)* (140 pc)
- *Rho Ophiuchi cloud* (130 pc)
- *Lupus* (140 pc)
- *Chamaeleon* (160 pc)
- *Corona Australis* (130 pc)

} 4/5 in the southern sky ... why?



Stability: The Virial Theorem

In a spherically symmetric cloud of temperature T , for each particle, the equation of motion is $\mathbf{F}_i = m_i \ddot{\mathbf{r}}_i = \dot{\mathbf{p}}_i$, the momentum change with time.

Sum up all particles and take time derivative

$$\begin{aligned} \frac{d}{dt} \sum_i \mathbf{p}_i \cdot \mathbf{r}_i &= \sum_i \dot{\mathbf{p}}_i \cdot \mathbf{r}_i + \sum_i \mathbf{p}_i \cdot \dot{\mathbf{r}}_i \\ &= \sum_i \mathbf{F}_i \cdot \mathbf{r}_i + \sum_i m_i \dot{\mathbf{r}}_i \cdot \dot{\mathbf{r}}_i \\ &= E_p + 2E_k \end{aligned}$$

$\frac{d}{dt} \sum_i m_i \dot{\mathbf{r}}_i \cdot \mathbf{r}_i$

$\sum_i \mathbf{F}_i \cdot \mathbf{r}_i = \text{virial of Clausius}$

101

For moment of inertia, $I = \sum_i m_i r_i^2$,

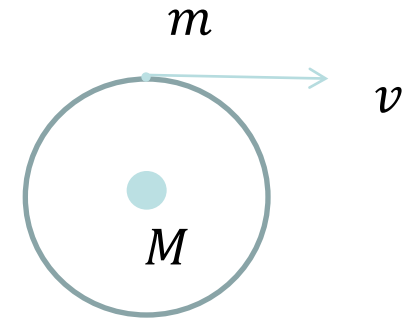
$$\frac{d^2 I}{dt^2} = \frac{d}{dt} \left[\sum_i m_i 2 r_i \dot{r}_i \right]$$

Hence

$$\frac{1}{2} \frac{d^2 I}{dt^2} = 2E_k + E_p$$

To be stable, LHS = 0

$$\boxed{2E_k + E_p = 0}$$



$$\frac{GmM}{r^2} = m \frac{v^2}{r}$$



$$2 \left(\frac{1}{2} \right) m v^2 = GmM/r$$



LHS = 0 \rightarrow stable

LHS < 0 \rightarrow collapsing

LHS > 0 \rightarrow expanding

E_K a variety of kinetic energies

- ✓ Kinetic energy of molecules
- ✓ Bulk motion of clouds
- ✓ Rotation
- ✓ ...

E_P a variety of potential energies

- ✓ Gravitation
- ✓ Magnetic field
- ✓ Electrical field
- ✓ ...

Note:

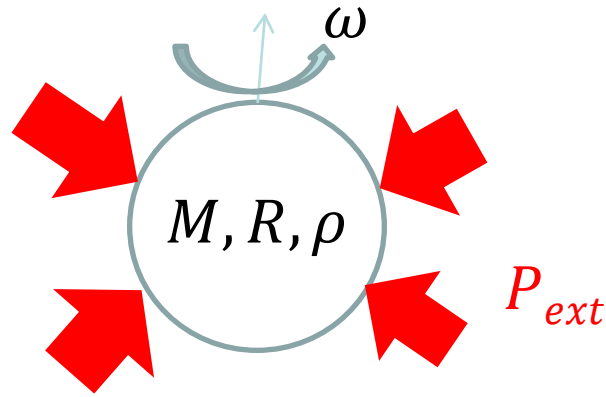
Virial theorem governs the motion status,

whereas the total energy

$$\begin{aligned} E_{\text{total}} &= E_K + E_P \\ &= E_K + \Omega \text{ (mostly)} \end{aligned}$$

governs whether the system is dynamically bound.

A tossed coin (less than the escape velocity) is bound either upward or downward.



Cloud of mass M , radius R , rotating at ω

$$E_{rot} = \frac{1}{2} I \omega^2 \quad I = \frac{2}{5} M R^2 \quad \Omega = -\frac{3}{5} \frac{G M^2}{R}$$

Generalized virial theorem

$$\frac{1}{2} \frac{d^2 I}{dt^2} = 2 \langle E_K \rangle + \int \vec{r} \cdot \vec{F} dm + 3 \int P dV - \oint P \vec{r} \cdot d\vec{s}$$

If $\omega = 0$, and $P_{ext} = 0$

$$2 \cdot \frac{3}{2} \frac{M}{\mu m_H} kT - \frac{3}{5} \frac{G M^2}{R} = 0$$

$$R_J = \frac{1}{5} \frac{G M \mu m_H}{kT}$$

This is the **Jeans length**.

$\mu \approx 2.37$ for solar abundance with H_2

Jeans length = critical spatial wavelength (length scale)

If the perturbation length scale is longer

→ Medium is decoupled from self-gravity → stable

$$M_J = \frac{4}{3}\pi R_J^3 \rho \quad R_J = \left(\frac{15}{4\pi} \frac{kT}{\mu m_H G \rho}\right)^{1/2} \sim \sqrt{\frac{T}{\rho}}$$

$$M_J = \left(\frac{\pi kT}{4\mu m_H G}\right)^{3/2} \sqrt{\frac{1}{\rho}} \sim \frac{T^{3/2}}{\rho^{1/2}}$$

This is the **Jeans mass** ...
the critical mass for onset
of gravitational collapse

If cloud mass $M > M_{\text{Jeans}}$ → cloud collapse

Note the above does not consider external pressure, or other internal supporting mechanisms.

A non-magnetic, isothermal cloud in equilibrium with external pressure → a **Bonnor-Ebert sphere** (Bonnor 1956, Ebert 1955)

$$2E_K + E_P - 3P_{\text{ext}}V = 0$$

The potential term may include, other than the gravity, also rotation, magnetic field, etc.

At first, the cloud is optically thin.

Contraction → density ↑ → collisions more frequent
→ molecules excited and radiating → photons escaped
→ cooling → less resistance to the contraction
→ cloud collapse (free fall)

$$R_f \approx c_s \tau_{\text{ff}} = [\text{isothermal sound speed}] * [\text{free fall time}]$$

To maintain $2E_K + E_P = 0$, the total energy $E_t = E_K + E_P$ must change. The gravitational energy

$$\Omega \sim -\frac{GM^2}{r} \rightarrow d\Omega \sim \frac{dr}{r^2}$$

For contraction, $dr < 0$, so $d\Omega < 0$, then

$$dE_t = dE_K + d\Omega = \frac{1}{2} d\Omega = Ldt$$

This means to maintain quasi-static contraction, half of the gravitation energy from the contraction is radiated away.

Eventually the cloud becomes dense enough (i.e., optically thick) and contraction leads to temperature increase.

The cloud's temperature increases while energy is taken away
→ negative heat capacity

Numerically,

$$M_J = 1.0 \left(\frac{T}{10 \text{ K}} \right)^{3/2} \left(\frac{n_{\text{H}_2}}{10^4 \text{ cm}^{-3}} \right)^{-1/2} [\mathcal{M}_\odot]$$

- H I clouds

$$T \approx 100 \text{ K}, n_H \approx 100, R_J \approx 25 \text{ pc}; M_J \approx 300 \mathcal{M}_\odot > M_{\text{obs}}$$

So H I clouds are not collapsing.

- Dark molecular clouds

$$T \approx 15 \text{ K}, n_H \approx 10^5, M_J \approx 20 \mathcal{M}_\odot < M_{\text{obs}} \approx 100\text{--}1000 \mathcal{M}_\odot$$

So H₂ clouds (dense cores and Bok globules) should be on the verge of collapsing. But observations show that most are not. → Additional support, e.g., thermal pressure, e.g., rotation, magnetic field, turbulence, etc.

Recall $M_J \approx 1.2 \times 10^5 \left(\frac{T}{100 \text{ K}}\right)^{3/2} \left(\frac{\rho_0}{10^{-24} \text{ g cm}^{-3}}\right)^{-1/2} \frac{1}{\mu^{3/2}} [M_\odot]$

$$\propto T^{3/2} / \rho^{1/2}$$

A small/decreasing M_J favors cloud collapse.

During collapse, ρ always \uparrow , so the behavior of M_J depends on T

Optically thin \rightarrow gravitational energy radiated away, isothermal collapse, $T = \text{const}$, so $M_J \propto \rho^{-1/2} \rightarrow$ collapse continues, local $M_J \downarrow \rightarrow$ subregions become unstable and continue to collapse to ever smaller M_J (**fragmentation**)

Until optically thick, adiabatic contraction $\rightarrow T \nearrow \nearrow \rightarrow$ stars

Formation of a cluster of stars $\sim \sim$



Equation of motion for a spherical surface at r is

$$\frac{d^2 r}{dt^2} = -\frac{GM}{r^2}$$

Dimensional analysis yields

$$\frac{R}{t^2} \sim \frac{GM}{R^2} \Rightarrow t_{ff} \sim \frac{1}{\sqrt{G\rho}}$$

More accurately, $t_{ff} = \left(\frac{3\pi}{32 G \rho_0} \right)^{\frac{1}{2}} = \frac{3.4 \times 10^7}{\sqrt{n_0}} \text{ [yr]} = 35 / \sqrt{\rho_{\text{cgs}}} \text{ [min]}$

It takes the Sun ~ 30 minutes to collapse (the **free-fall time scale**)₁₀

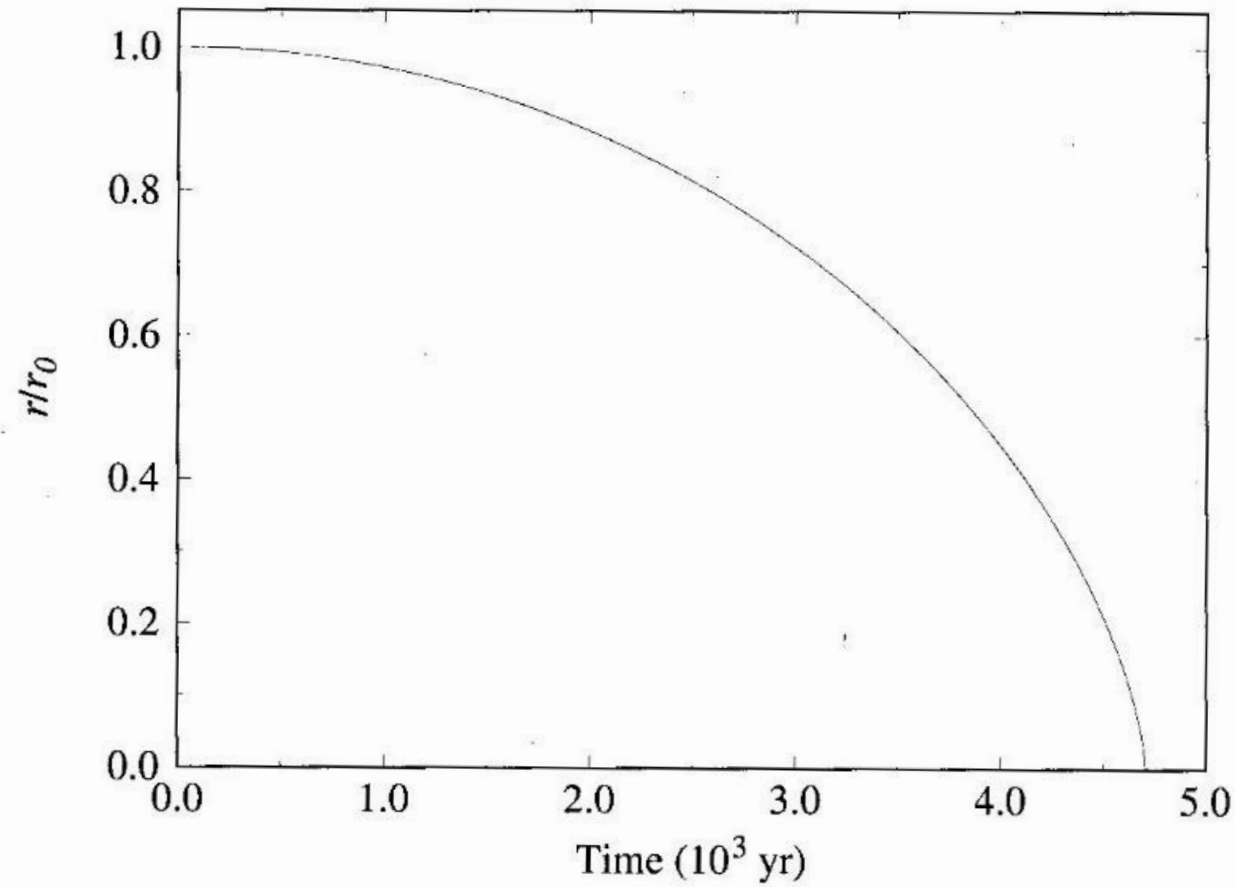


Figure 12.5 The ratio of the radius relative to its initial value as a function of time for the homologous collapse of a molecular cloud. The collapse is assumed to be isothermal, beginning with a density of $\rho_0 = 2 \times 10^{-16} \text{ g cm}^{-3}$.

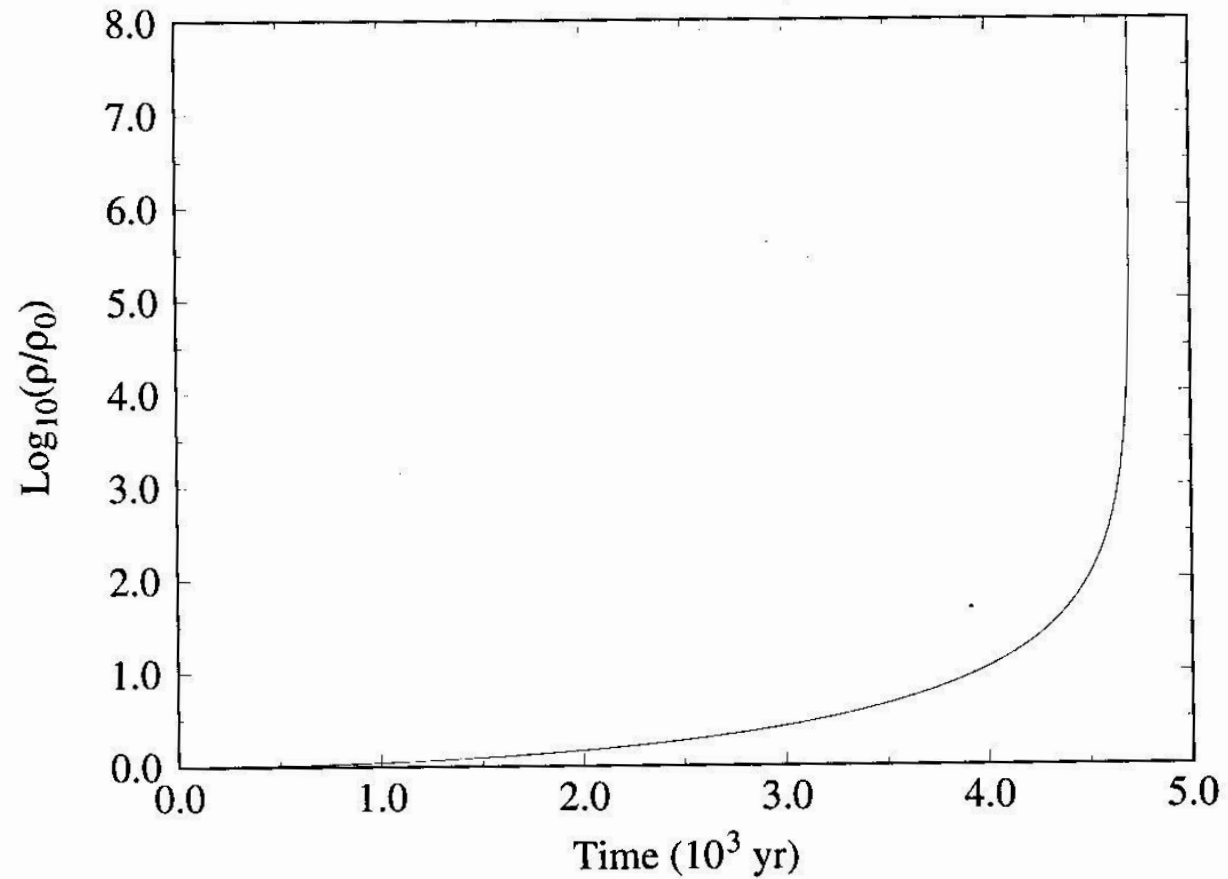


Figure 12.6 The ratio of the cloud's density relative to its initial value as a function of time for the isothermal, homologous collapse of a molecular cloud with an initial density of $\rho_0 = 2 \times 10^{-16} \text{ g cm}^{-3}$.

Note that $t_{\text{ff}} \propto \frac{1}{\sqrt{G\rho_0}}$ has no dependence on r_0 .

If ρ_0 is uniform, all m collapse to the center at the same time

→ **homologous collapse**

In reality, ρ_0 is somewhat centrally condensed, as observed,

e.g., $\rho_0 \propto r^{-1}$ to r^{-2} , inner region (small r), $t_{\text{ff}} \downarrow\downarrow$

→ **inside-out collapse**

A protostellar core is formed, followed by material “raining down” from the envelop → **accretion**

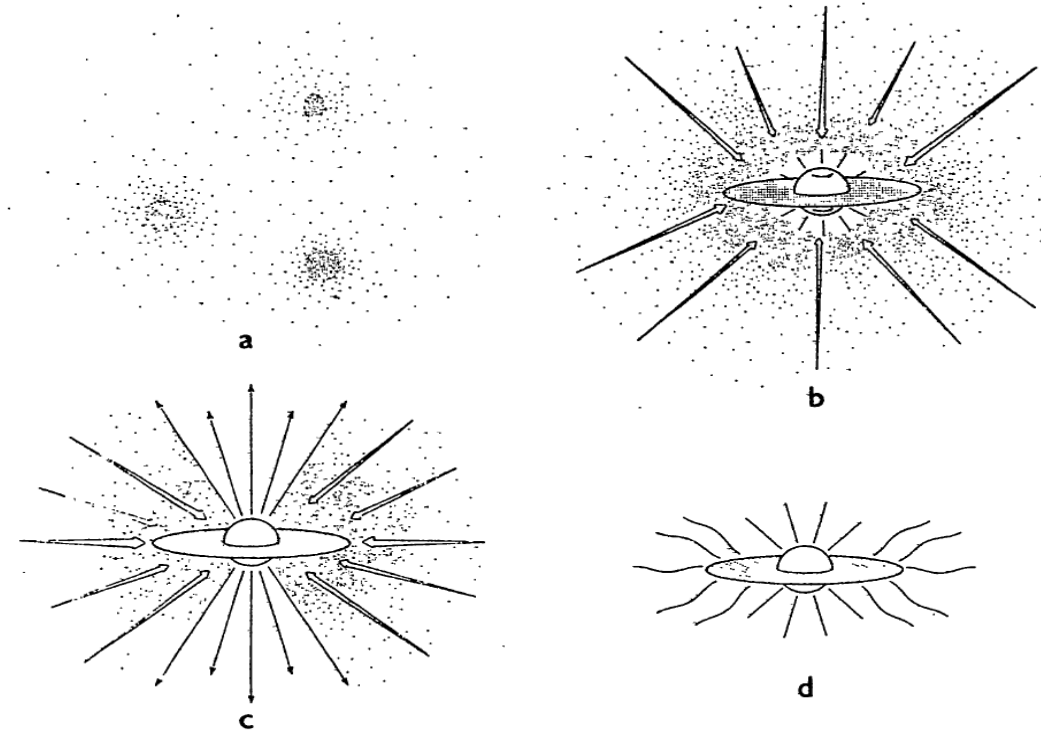
Gravitational energy → kinetic energy → heat $L_{\text{acc}} \sim GM_* \dot{M}/R_*$

*Dense cores form within
molecular clouds → Seeds of
individual stars*

STAR FORMATION IN MOLECULAR CLOUDS: OBSERVATION AND THEORY

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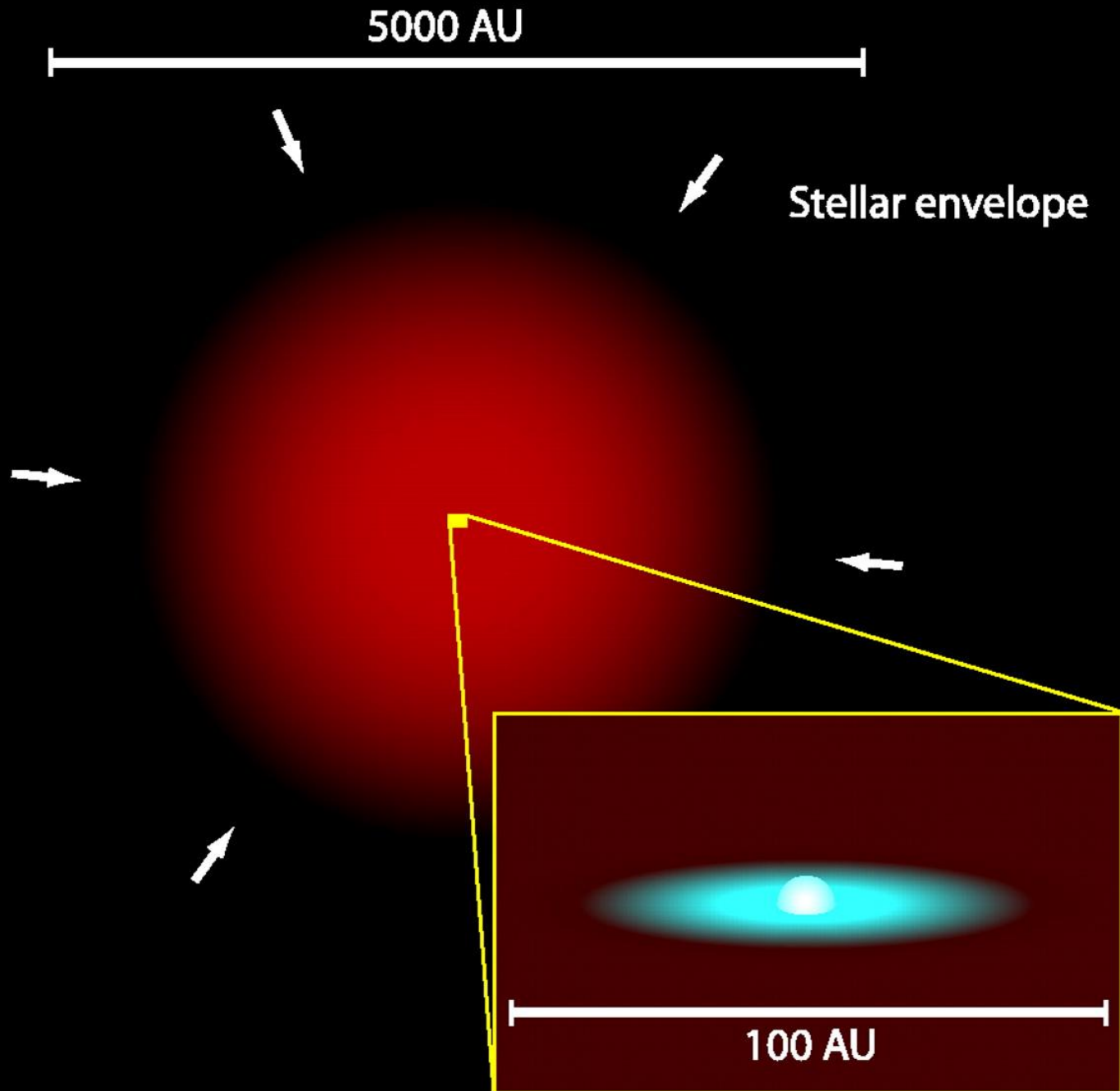


*A core collapse inside-
out and form a protostar
with a toroid.*

*A stellar wind with a
bipolar flow forms.*

*A star is formed with
a circumstellar disk.*

Figure 7 The four stages of star formation. (a) Cores form within molecular clouds as magnetic and turbulent support is lost through ambipolar diffusion. (b) A protostar with a surrounding nebular disk forms at the center of a cloud core collapsing from inside-out. (c) A stellar wind breaks out along the rotational axis of the system, creating a bipolar flow. (d) The infall terminates, revealing a newly formed star with a circumstellar disk.



Central condensed protostar,
 $r \sim \text{a few } R_{\odot}$

Circumstellar disk,
 $r \sim 100 \text{ au}$

Surrounding envelope,
 $r \sim 5000 \text{ au}$

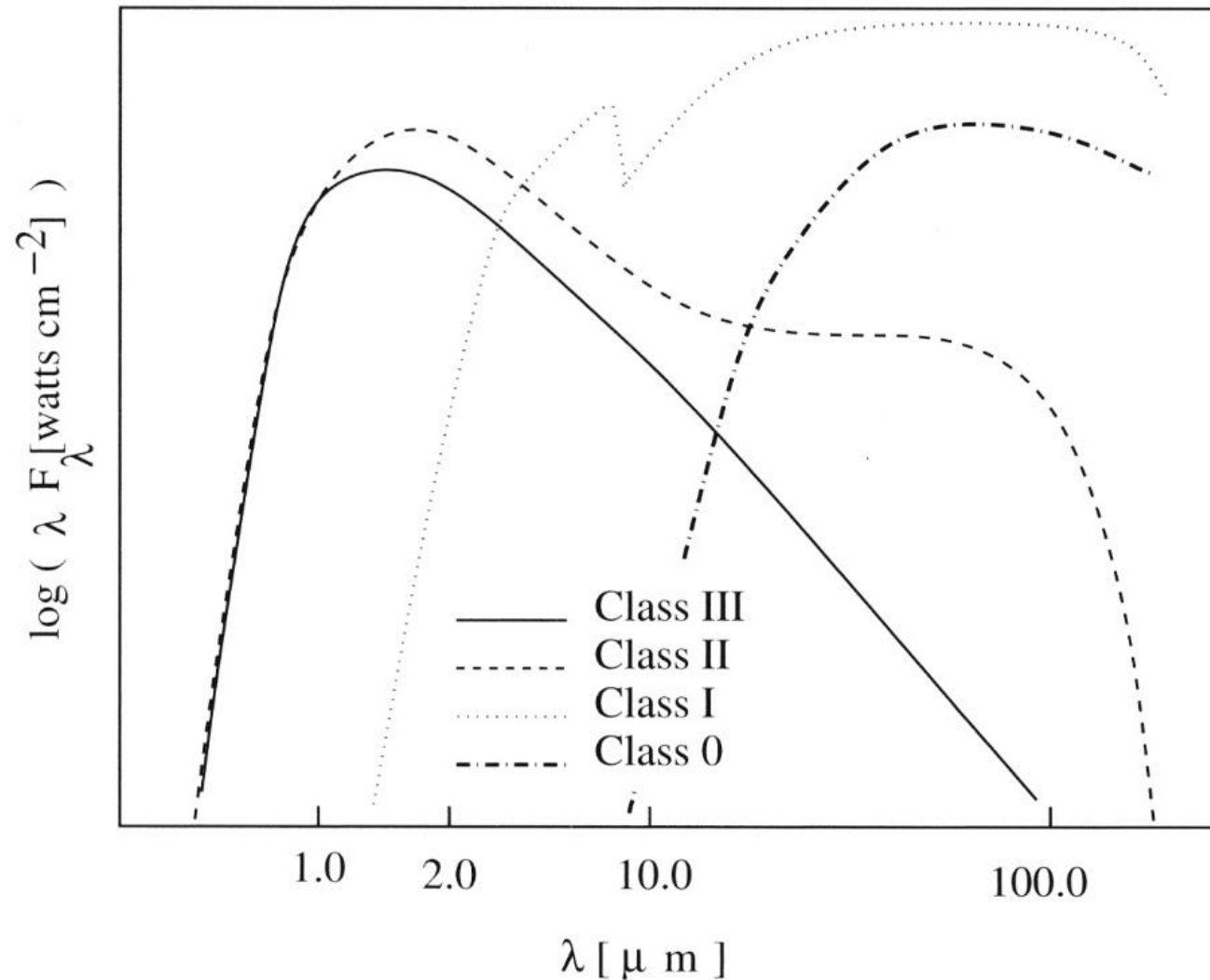
Matter accretes from the
envelope via the disk onto
the protostar

Ward-Thomson (2002)

Spectral energy distribution

F_λ vs λ

or $\log \lambda F_\lambda$ vs $\log \lambda$



Spectral index useful to classify a young stellar object (YSO)

$$\alpha = \frac{d \log (\lambda F_{\lambda})}{d \log (\lambda)} \quad \text{where } \lambda \text{ wavelength, between 2.2 and } 20 \text{ } \mu\text{m}; F_{\lambda} = \text{flux density}$$

Class 0 sources --- undetectable at $\lambda < 20 \text{ } \mu\text{m}$

Class I sources --- $\alpha > 0.3$

Flat spectrum sources --- $0.3 > \alpha > -0.3$

Class II sources --- $0.3 > \alpha > -1.6$

Class III sources --- $\alpha < -1.6$

➔ Evolutionary sequence in decreasing amounts of circumstellar material (disk clearing)

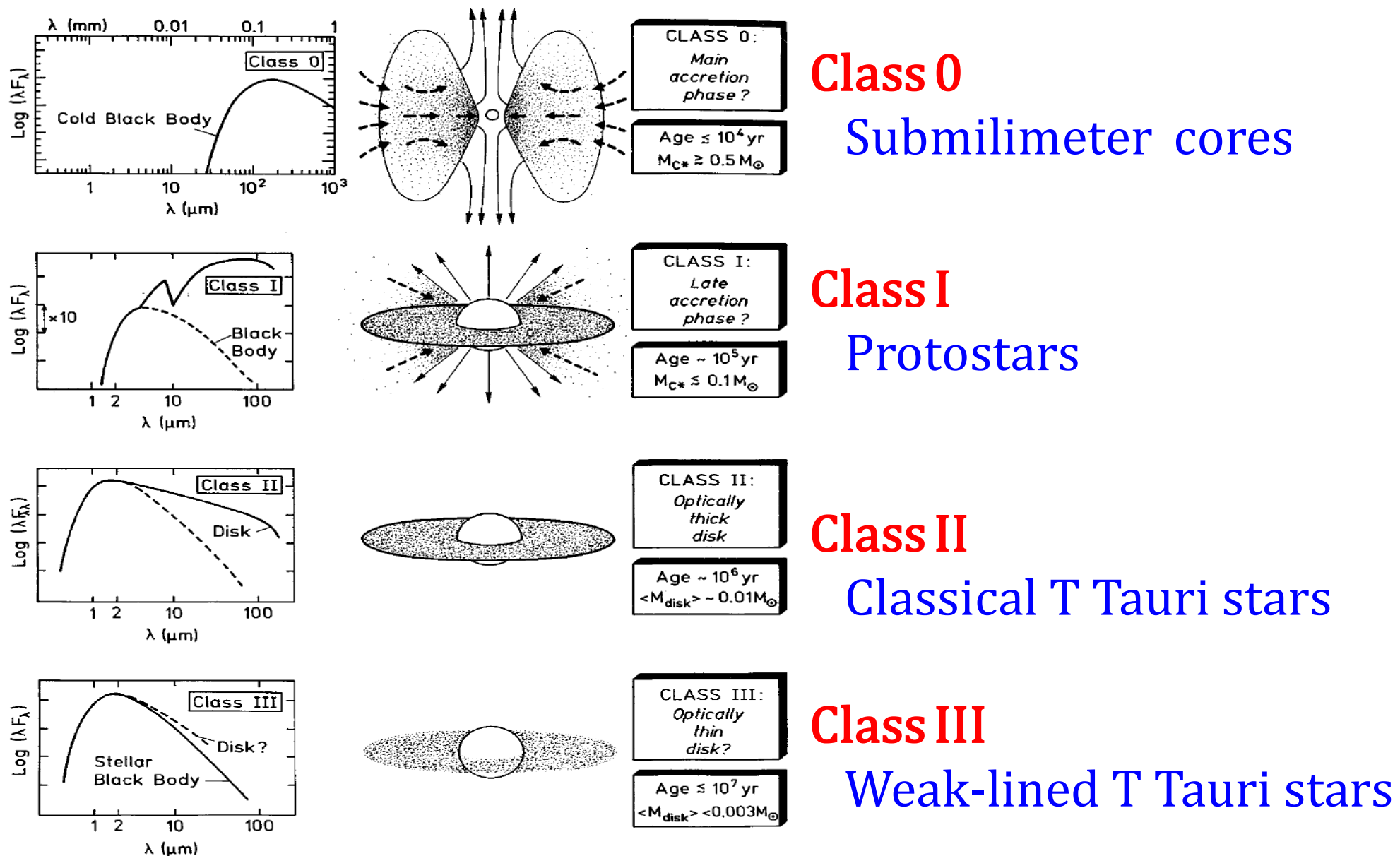


Figure 11 Evolutionary sequence of the spectral energy distributions for low-mass YSOs as proposed by André (1994). The four classes 0, I, II, and III correspond to successive stages of evolution.

Star Formation Rate (SFR): The rate at which gas and dust forms stars.
[*Solar masses*]/[*Year*] [unit area in disk]

Milky Way galaxy: $1 \sim 3 \text{ M}_{\odot} \text{ yr}^{-1}$ (a few new-born stars per year)

M31: $0.4 \text{ M}_{\odot} \text{ yr}^{-1}$

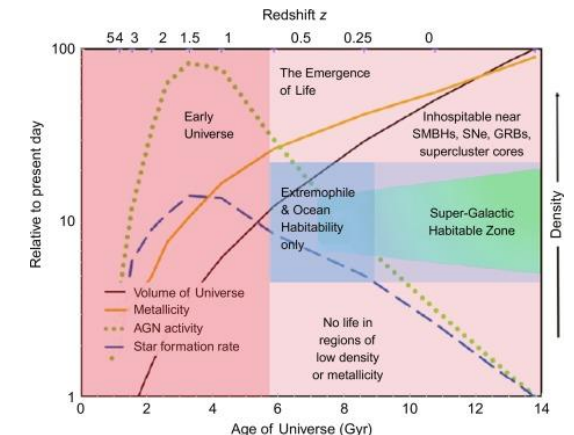
$\text{SFR} \Leftrightarrow \text{LFIR}, \text{L}(\text{H}_{\alpha}), \text{UV} \dots$

Kennicutt-Schmidt empirical “law”: $\Sigma_{\text{SFR}} \propto (\Sigma_{\text{gas}})^n, n \approx 1.4$ (surface?)

Star Formation Efficiency (SFE): Within a region, the ratio of
[*Mass of stars formed*]/[*Total mass of the gas and dust available*],

usually a few percent; e.g., nearby
star clusters 10% to 30% (Lada & Lada 03)

or SFR per unit of gas,
e.g., $\text{SFE}(\text{H}_2)$ (Leroy+08)



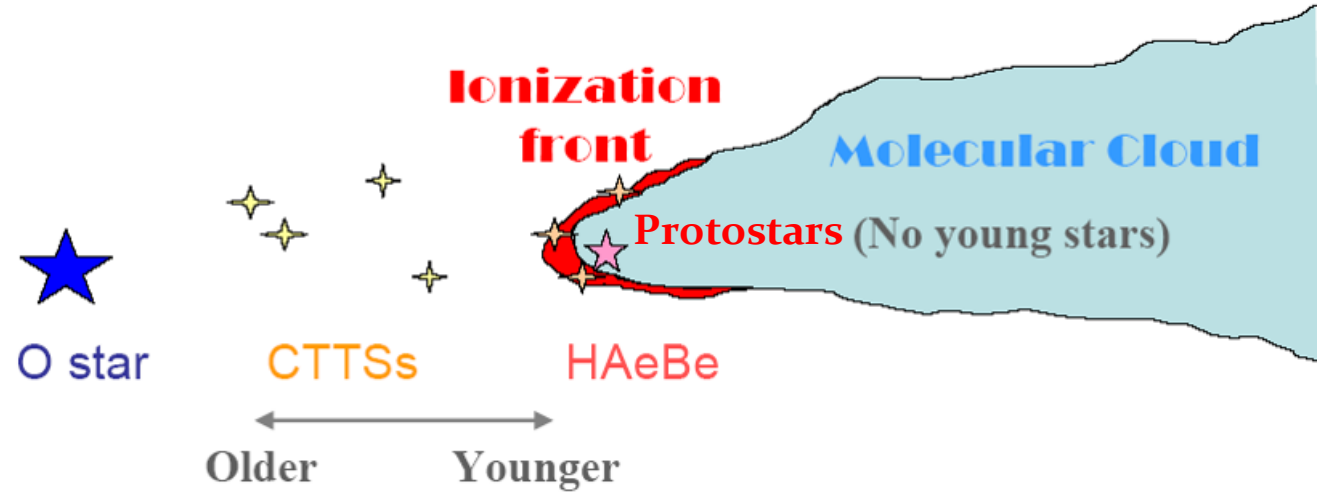
Massive Star Formation and Feedback

Triggered/sequential/induced SF

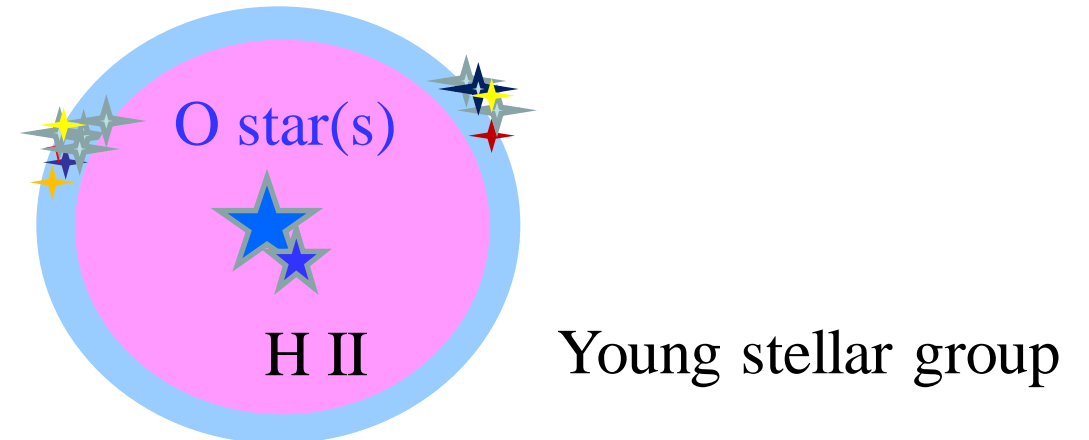
Stellar winds + radiation

Other possible triggerers:
SNe, cloud-cloud collisions,
density waves (spiral-arm),
merging galaxies, etc.

Radiation-Driven Implosion



Collect-and-Collapse



Antennae Galaxies



HST image of NGC 4038 (top) and NGC 4039 (bottom)



HST (blue, young stars) and ALMA (red, pink, and yellow, cold gas)

Conclusions

- ISM has a variety of forms (atomic, ionic, molecular) in solid or gaseous state, under differing conditions (temperature, density, composition ...)
- Stars form out of cold, dense ISM cloud cores. Rotation, magnetic field, turbulence, etc. play crucial roles. Planets/life ...
→ A universal initial stellar mass function ... more lower-mass stars
- Stars continue to interact with ISM. Evolved stars condense dust in their atmospheres. Dying stars enrich the ISM with complex elements (“metals”) from which new stars form.
- Some galaxies are rich in such gas and dust, some not. Our Milky Way galaxy is producing stars. Cosmic SF history?