Post-main Sequence Evolution

Remaining Classes

- June 4
- June 11
- June 13 (Th) ... 5 pm
- June 18 ... final exam

Evolution of the Sun in the HRD







Evolution in the HR-diagram of a $5 M_{\odot}$ model (Z = 0.015, Y = 0.275) just prior to and during core helium burning – first approximation

Iben (2013)



https://www.e-education.psu.edu/astro801/content/I6_p5.html



Fig. 20.1.1

Evolutionary path of <u>a 25 M_{\odot} model</u> through core hydrogen and core helium burning to the onset of core carbon burning (Z = 0.015, Y = 0.275) **Iben** (2013)



Thermally pulsing AGB

Iben (2013) 7

Luminosity Class



http://en.wikipedia.org/wiki/File:HR-diag-no-text-2.svg

Hypergiants

luminosity class 0; excessive mass loss

Supergiants

Ia luminous supergiants; Ib supergiants; $Ia^+ = 0$

Subgiants

luminous class IV; between MS turn-off and the red giant branch

Dwarfs

luminosity class V = MS stars

Subdwarfs (sd)

luminosity class VI, 1.5 to 2 mag lower than MS; lower metallicity $_{8}$



For single stars, more massive stars evolve off the MS sooner. Accordingly the MS is "peeled off" from the top down. For an old star cluster, only the bottom MS remains.



Mass Loss during Stellar Evolution

- Stars lose mass at every evolutionary stage.
- <u>Pre-main sequence</u>: protostellar (bipolar) outflows
 YSO jets, (star/disk) winds
- <u>Main sequence</u>: solar wind $\dot{\mathcal{M}} = 10^{-14} M_{\odot} \text{ yr}^{-1}$ For $\tau_{\text{MS}} \approx 10^{10} \text{ yr} \rightarrow \tau_{\text{loss,MS}} \approx 10^{-4} M_{\odot}$ (negligible) Some stars, e.g., WR stars $\dot{\mathcal{M}} = 10^{-5} M_{\odot} \text{ yr}^{-1}$
- <u>Post-main sequence</u>: $R \uparrow \rightarrow g \downarrow$, and $P_{rad} \uparrow \Rightarrow \dot{\mathcal{M}} \uparrow$





Fig. 7.6. Schematic representation of an irradiated flared disk. Below the radius R_g where matter remains bound by the gravity of the central star an optically thin atmosphere develops. Above this radius flared matter may escape and form some kind of slow wind. Adapted from Hollenbach et al. [403].

• For a stationary, isotropic wind, the mass loss rate

$$\dot{\mathcal{M}} = 4 \pi r^2 \rho(r) \frac{\mathrm{d}r}{\mathrm{d}t} = 4 \pi r^2 \rho(r) v(r)$$
 $v(r)$: velocity law

- $v(r) \uparrow$, at $r \to \infty$, $v_{\infty} \equiv v(r \to \infty)$ terminal velocity Often $v(r) \approx v_0 + (v_{\infty} - v_0) \left(1 - \frac{R_*}{r}\right)^{\beta}$, where $v_0 = v(R_*)$ at photosphere
- $\beta \leq 1, v \rightarrow v_{\infty}$ gradually $\beta \geq 1, v \rightarrow v_{\infty}$ slowly
- For hot stars, $\beta \approx 0.8$. Cool stars experience slower acceleration, so have larger β .

$\dot{\mathcal{M}} = 4 \pi r^2 \rho(r) v(r)$ mass conservation

$$\ddot{r} = -\frac{1}{\rho}\frac{\mathrm{d}P}{\mathrm{d}r} - \frac{GM}{r^2} = \frac{\mathrm{d}v}{\mathrm{d}t} = \frac{\mathrm{d}v}{\mathrm{d}r}\frac{\mathrm{d}r}{\mathrm{d}t} = v\frac{\mathrm{d}v}{\mathrm{d}r}$$
 momentum conservation

Massive stars \rightarrow radiation pressure

- \rightarrow outer atmosphere expands supersonically
- \rightarrow winds driven by spectral-line opacity in UV.



Mass loss (Reimers 1975) $\dot{M} \approx 4 \times 10^{-13} \frac{L/L_{\odot}}{(g/g_{\odot}) (R/R_{\odot})} [M_{\odot} \text{ yr}^{-1}]$

$$g = GM/R^2$$

Fig. 8.8. The evolutionary paths in the Hertzsprung–Russell diagram of Population I stars having $1.0 \mathcal{M}_{\odot}$ and $1.1 \mathcal{M}_{\odot}$, from central hydrogen burning (A) to the helium flash (E), without taking mass losses into account. After A. V. Sweigart and P. G. Gross (1978). The ejection of a mass of $0.1 \mathcal{M}_{\odot}$ during the helium flash was assumed. The further evolution of the star of $1.0 \mathcal{M}_{\odot}$ was calculated taking the mass loss according to (7.105) into account, after D. Schönberner (1979). F \rightarrow G: the asymptotic giant branch; only one of the thermal pulses (helium flashes) which occur after I is drawn in, at J. The mass loss becomes important at H and leads to a final mass of $0.6 \mathcal{M}_{\odot}$, which is reached at K

Sun now $\dot{M} \approx 2 \times 10^{-14} \text{ M}_{\odot} \text{ yr}^{-1}$ Cool supergiant $\dot{M} \approx 10^{-7} \text{to } 10^{-5} \text{ M}_{\odot} \text{ yr}^{-1}$







P Cygni profile of a spectral line ---- a blue-shifted absorption superimposed on an emission line \rightarrow mass loss (cool gas toward us)

Lamers and Cassinelli, *Introduction to Stellar Winds*, Cambridge, 1999 17

P Cygni stars

- Higher mass-loss rate, $> 10^{-5} M_{\odot} \text{ yr}^{-1}$
- Lower terminal velocity, $v_{\infty} < 10^{2.5} \text{ km s}^{-1}$
- Higher wind density, $n_H > 10^{10} \text{ cm}^{-3}$ at 2 R_*

than normal stars (Lamers 1986).

Stellar Pulsation



FIG. 5.—Color-magnitude diagram for M3 stars in the arguments V and B - V



https://en.wikipedia.org/wiki/Subgiant#/media/File:M5_colour_magnitude_diagram.png

Stellar Variability

□ Time to transmit a perturbation of pressure changes across the star

$$t_{\rm vib} \sim \frac{2R}{\bar{v_s}}$$
 where $v_s = \sqrt{\gamma \frac{P_g}{\rho}}$

$$\gamma = c_P / c_V = 5/3$$
 for monatomic gas.

$$\Box \text{ Virial theorem, } 2K + \Omega = 0, \therefore$$

$$v_s^2 = \frac{GM}{R}$$

$$t_{\rm vib} \sim \frac{2R}{\sqrt{GM/R}} \sim \frac{1}{\sqrt{G\rho}}$$

cf. free-fall time

Approximate Relation between Stellar Density, Pulsation and Minimum Rotational Period

Star	Density g cm ⁻³	t _{vib} sec	t _{rot, min} sec
Neutron star	10^{15}	10^{-4}	$3 \ge 10^{-4}$
White Dwarf	107	1	3
RR Lyrae star	10^{-2}	10 ^{4.5}	10 ⁵
Cepheid Variable	10^{-6}	$10^{6.5}$	107

t (Crab Nebula) ~ 33 ms \rightarrow cannot be a white dwarf

- Rotational Variation --- sub-seconds .. weeks
- Pulsational Variation --- hours .. weeks
- Orbital (Eclipsing Binaries) --- hours .. days



 $\therefore Heating \to T \uparrow \to \mathcal{K} \downarrow \to cooling$

· contraction -> releases energy

expansion -> absorbs energy

Normally T $\nearrow \kappa \searrow$

Recall Kramers opacity

K mechanism - a partially ionized layer to absorb energy during compression (and release energy ding expansion)

In stars, there are 2 ionization Eones $- T \sim (1 - 1.5) \times 10^{4} K$ $HI \rightarrow HI, HeI \rightarrow HeI$ $- T \sim (4 - 5) \times 10^{4} K$ $HeI \rightarrow HeII$ But if there is an ionization layer, e.g., He⁺ \rightarrow He⁺⁺

T \land → κ \land energy trapped → expansion

Energy escaped → Contraction



Depths & Sonilation Eones R.S. Teff ~ 7500K, Zones near surface -> not enough mass available to drive the oscillation . Teff ~ \$ 500K, Zones deeper => significant pulsation Teff & Stock, convective outer layer -> pulsation suppresses . Teff ~ 500 - 7500K for pulsation to take place.

There is a certain surface temperature range for stellar pulsation ...

Instability "strip"



Figure 4.9. Examples of various types of pulsating variable stars plotted as small circles on the Hertzsprung–Russell diagram. The dark line to the right is the main sequence with evolutionary tracks branching off to the right for different stellar masses. The ultimate evolutionary track of a star that ends its life as a compact star of 0.63 M_{\odot} is shown. It moves leftward through the planetary nebulae nuclei variables (PNNV) and then downward as a cooling white dwarf, passing through regions of pulsational instability sequentially classified as DOV, DBV, and DAV (DAV = Dwarf + type/temperature A + Variable). Other types of intrinsic variables are shown: β Cephei stars, Mira (M), Semiregular (Sr), luminous blue (LBV), Wolf–Rayet (WR), slowly pulsating B stars (SPB), and subdwarf B stars (sdBV). The *classical instability strip* is shown as two parallel lines encompassing Cepheid, RR Lyrae, and δ Scuti variables; if extended, it intersects the pulsating DAV stars. The thin lines represent loci of constant radius. [Provided by A. Gautschy; see Gautschy H. Saio, *ARAA* 33, 77 (1995)]

Bradt "Astrophycs Processes"

Normally TI => K 1 plays a role also in red gianto Core - increased energy output Envelope - expansion, cooling + K1 => Red giants have convective envelopes of PMS Hayashi tracks The envelope extends from just outside of the H-burning shell to the surface. -> Dredge-up of processed material from deep interior to surface

R.g., observations of heavy elements on isotope ratios in evolved stars different from (enrichment) young stars (In a star cluster) => Evidence of stellar evolutions . of nuclear reactions.

Convection \rightarrow chemical mixing

Much more efficient than the slow change of chemical composition produced by nuclear reaction.

In a convection region,
$$\frac{\partial X_i}{\partial m} = 0$$



Fig. 8.1. The abundances X_i are smeared out owing to rapid mixing inside a convection zone extending from m_1 to m_2 . At these borders X_i can be discontinuous

The Dredge-ups
H shell burning
$$\rightarrow$$
 He core f , $T \uparrow$
 \downarrow
envelope Axpands \rightarrow red giant branch
(RGB)
CNO cycle \rightarrow low T , high opacity, $\nabla T \uparrow$
 \therefore convective envelope
 \downarrow
Material in the core brought up and
mixed with envelope
 \Rightarrow The (first) dredge-up
Photosphere observed N \uparrow at the expenses T
C and O

Schematic view of an AGB star



http://www.univie.ac.at/agb/agbdetail.html

J. Hron, Inst. for Astronomy, Univ. of Vienna

Electron Degeneracy

Fermi-Dirac distribution for non-interacting, indistinguishable particles obeying Pauli exclusion principle; applicable to half-integer spin in TE. Examples of fermions include the electron, proton, neutrons, and nuclei with odd mass numbers, e.g., ³He (2 e⁻, 2 p⁺, 1 n⁰)

Bose-Einstein distribution for particles not limited to single occupancy of the same energy state. i.e., that do not obey Pauli exclusion principle; with integer values of spin. Example bosons include ⁴He, the Higgs boson, gauge boson, graviton, meson.

A Fermi gas is called degenerate if the temperature is low in comparison with the Fermi temperature/energy.


Chemical Potential (µ)

- Temperature governs the flow of energy between two systems.
- Chemical potential governs the <u>flow of particles</u>; from higher chemical potential to the lower.







As time goes on, electron degeneray becomes increasingly important, e.g. pe ~ 1.7% of total processe at 12 ~ 0 T~ 9.2× 10 yr ~ 7.5% " Taking electron deg. pressure into account, Misothermal core ~ 0.13 Mo => presence insufficient to puppert overlying Layers => core contraction => heated, Enue 1 => Overlying layers pushed butwards => Enue in a narrowing shell End of main-sequence phase

46

For low-mass stars (0.7-2Mg) Pe is high -> e degeneray sets in before core He burning begins When He burning starts -> Te 1 (but Pe does not) $\rightarrow \in 11$ => He flash Erelease ~ 10 Lo in a few seconds Energy absorbed by envelope (being pushed) no observable effects !

WHY IS THERE A HELIUM FLASH ? normal ideal gas pt => Tf . Energy input => T1 => P1 => expand stable. against thermal ... Th instability => a safty-valve mechanism If the helium core is degenerate P + > T when TZIOK, TTT => runaway thermal instability within a few seconds, He ignited => helium flash

The helium flash occurs for $M_{\rm core} \approx 1 M_{\odot}$

If $\mathcal{M} \leq 0.5 \mathcal{M}_{\odot} \rightarrow \text{core never hot enough}$

If $\mathcal{M} \geq 2.25 \mathcal{M}_{\odot} \rightarrow$ core too hot, He ignited before a degenerate core develops

→ Only $\mathcal{M} \approx 0.5 - 2.25 \mathcal{M}_{\odot}$ stars experience the He flash.

After the helium flash



Core He burning is much shorter than the MS phase of core H burning, because He is short in abundance, not as efficient in energy supply (1/10 per mass), and the stellar luminosity is higher.





Evolution of the Sun in the HRD

□ MS (core H burning)

- Subgiant branch (shell H burning)
- Red giant branch (shell H burning)
- Red giant (core He flash)
- Horizontal branch (core He burning)
- Asymptotic giant branch (shell He burning)
- Red supergiant
- Protoplanetary nebula
- Planetary nebula
- □ White/black dwarf⁵⁴

The red clump = HB (core He burning) of metal-rich stars



Clump ... 5,000 K and *M_V*~0.5





For high-mass stais, e.g.,
$$\pm H_0$$

L grav contributes ; L, \uparrow for $M_r < o.1 M$
 $\Rightarrow \nabla T \Rightarrow kater He burning begins before
 $e^{-} deg. sets 7n$
Shell burning pushes the core and envelope $\rightarrow L_r (r > 0.2) \downarrow$
 $\epsilon_{shell} \uparrow \uparrow \Rightarrow envelope expands \uparrow \uparrow$
 $\mapsto adds mass until Schönberg-Chandrasekhar kint$
 $\Rightarrow core contracts, Te \uparrow \rightarrow \epsilon_{shell} \uparrow \uparrow \uparrow$
 $Fushe envelope, Tett b, L_r \leq const$$



Fig. 1.7. The color apparent magnitude diagram for 47 Tucanae. The new measurements go down to stars as faint as 23rd magnitude, though for the faint stars the scatter becomes large. The main sequence and the giant and subgiant branches are surprisingly sharp, showing that there are very few or no binaries in this globular cluster. The red stub of the horizontal branch is seen at $V \sim 14$ and $B - V \sim 0.8$. The asymptotic giant branch (see Chapter 14) is seen above the horizontal branch. From Hesser *et al.* (1987).



Fig. 1.8. The color absolute magnitude diagram for the globular cluster M92 (cluster 92 in the Messier catalog of nebulous objects). The new observations for M92, like those for 47 Tuc, go to very faint magnitudes. For M92 the main sequence is now clearly recognizable. In addition the subgiant, red giant and horizontal branches are clearly seen. Also seen is the so-called asymptotic branch, for $(B - V)_0 \sim 0.6$ above the horizontal branch. The thin lines shown are the theoretical isochrones, i.e. the location where stars are expected to be seen at a given time. From Hesser *et al.* (1987).

HB morphology differs from one Gc to another.



If H-shell burning -> WD w/ athin layer 80% of all DA white dwarfs (H lives, no He lives If He-shell burning - wD He layer L. less freq. DB (HeIline, no H. 16% metals) => expect more DA white awarfs than DBs obs 25%. He lines DC (continuous, no lines) DO (He I lives)

DQ (C domínated)

• Origins of DA and non-DA uncertain: (1) exact phase when the last thermal pulse takes place after the AGB phase, or (2) convective mixing, radiative levitation, or diffusion.

 $M: \circ. \overline{7} - 1.0 M_{\odot}$ $M: \circ. \overline{7} - 1.0 M_{\odot}$ $MS \rightarrow RG - He core \stackrel{<}{\sim} 0.4 M_{\odot} WD$ $MS \rightarrow RG - He core \stackrel{<}{\sim} 0.4 M_{\odot} WD$ nc AGB, PN phases

Mass distribution of DA white dwarfs in the First Data Release of the Sloan Digital Sky Survey

A&A 419, L5–L8 (2004)

J. Madej¹, M. Należyty¹, and L. G. Althaus²

¹ Astronomical Observatory, University of Warsaw, Al. Ujazdowskie 4, 00-478 Warsaw, Poland

² Departament de Fisica Aplicada, Universitat Politecnica de Catalunya, Av. del Canal Olimpic s/n, 08860, Castelldefels, Spain

Received 4 March 2004 / Accepted 23 March 2004

Abstract. We investigate the sample of 1175 new nonmagnetic DA white dwarfs with the effective temperatures $T_{\text{eff}} \ge 12000$ K, which were extracted from the Data Release 1 of the Sloan Digital Sky Survey. We determined masses, radii, and bolometric luminosities of stars in the sample. The above parameters were derived from the effective temperatures T_{eff} and surface gravities log *g* published in the DR1, and the new theoretical M - R relations for carbon-core and oxygen-core white dwarfs. Mass distribution of white dwarfs in this sample exhibits the peak at $M = 0.562 M_{\odot}$ (carbon-core stars), and the tail towards higher masses. Both the shape of the mass distribution function and the empirical mass-radius relation are practically identical for white dwarfs with either pure carbon or pure oxygen cores.





< 0.16 M_{\odot} \rightarrow no RGB < 0.5 M_{\odot} \rightarrow $\tau_{MS} > \tau_{Universe}$ < 0.5~0.7 M_{\odot} \rightarrow no core He burning

Very low-mass stars are completely convective \rightarrow more H to burn $\rightarrow \tau_{MS}$ lengthened

A 1 M_{\bigodot} main sequence star

- $\tau_{\rm MS} \sim 10^{10} {
 m yrs}$
- $\tau_{RGB} \sim 10^9 \text{ yrs}$
- $\tau_{HB} \sim 10^8 \text{ yrs}$
- $\tau_{AGB} \sim 2 \times 10^7 \text{ yrs}$
- $\tau_{PS} \sim 5 \times 10^4 \text{ yrs}$

A remnant of a 0.6 WD



Mass loss rate low

 $\mathcal{M} = 20 - 25 \,\mathrm{M}_{\bigodot}$ 0 type star \rightarrow red supergiant \rightarrow supernova $\mathcal{M} < 20$ 0 type star \rightarrow red supergiant \rightarrow Cepheid \rightarrow red supergiant \rightarrow supernova Mass loss not sufficient to remove the entire envelope

 $\mathcal{M} = 40 - 60 \,\mathrm{M}_{\bigodot}$ 0 type star \rightarrow blue super giant \rightarrow yellow supergiant \rightarrow red supergiant \rightarrow blue supergiant \rightarrow WN \rightarrow supernova $\mathcal{M} = 25 - 40 \,\mathrm{M}_{\bigodot}$ 0 type star \rightarrow blue super giant \rightarrow yellow supergiant \rightarrow red supergiant

 \rightarrow supernova



Mass loss fierce $\approx 10^{-1}$ M_{\odot} yr⁻¹, rid of almost entire envelope during the LBV stage, left with a WR star, evolving toward a SN.

0 type star \rightarrow 0f star \rightarrow blue super giant

→ luminous blue variable → WN star → WC star → supernova



The evolution of massive stars and their spectra

I. A non-rotating 60 M_{\odot} star from the zero-age main sequence to the pre-supernova stage^{*,**}

Jose H. <u>Groh¹</u>, Georges Meynet¹, Sylvia Ekström¹, and Cyril Georgy²

¹ Geneva Observatory, Geneva University, Chemin des Maillettes 51, 1290 Sauverny, Switzerland

```
e-mail: jose.groh@unige.ch
```

² Astrophysics group, EPSAM, Keele University, Lennard-Jones Labs, Keele, ST5 5BG, UK

ABSTRACT

For the first time, the interior and spectroscopic evolution of a massive star is analyzed from the zero-age main sequence (ZAMS) to the pre-supernova (SN) stage. For this purpose, we combined stellar evolution models using the Geneva code and stellar atmospheric/wind models using CMFGEN. With our approach, we were able to produce observables, such as a synthetic high-resolution spectrum and photometry, thereby aiding the comparison between evolution models and observed data. Here we analyze the evolution of a nonrotating 60 M_{\odot} star and its spectrum throughout its lifetime. Interestingly, the star has a supergiant appearance (luminosity class I) even at the ZAMS. We find the following evolutionary sequence of spectral types: O3 I (at the ZAMS), O4 I (middle of the H-core burning) phase), B supergiant (BSG), B hypergiant (BHG), hot luminous blue variable (LBV; end of H-core burning), cool LBV (H-shell burning through the beginning of the He-core burning phase), rapid evolution through late WN and early WN, early WC (middle of He-core burning), and WO (end of He-core burning until core collapse). We find the following spectroscopic phase lifetimes: 3.22×10^6 yr for the O-type, 0.34×10^5 yr (BSG), 0.79×10^5 yr (BHG), 2.35×10^5 yr (LBV), 1.05×10^5 yr (WN), 2.57×10^5 yr (WC), and 3.80×10^4 yr (WO). Compared to previous studies, we find a much longer (shorter) duration for the early WN (late WN) phase, as well as a long-lived LBV phase. We show that LBVs arise naturally in single-star evolution models at the end of the MS when the mass-loss rate increases as a consequence of crossing the bistability limit. We discuss the evolution of the spectra, magnitudes, colors, and ionizing flux across the star's lifetime, and the way they are related to the evolution of the interior. We find that the absolute magnitude of the star typically changes by ~ 6 mag in optical filters across the evolution, with the star becoming significantly fainter in optical filters at the end of the evolution, when it becomes a WO just a few 10^4 years before the SN explosion. We also discuss the origin of the different spectroscopic phases (i.e., O-type, LBV, WR) and how they are related to evolutionary phases (H-core burning, H-shell burning, He-core burning).

Read the first 4 paragraphs of this paper?

Stellar Rotation



Fig. 3. Projected equatorial velocities, averaged over all possible inclinations, as a function of spectral type. On the main sequence (luminosity class V), early-type stars have rotational velocities that reach and even exceed 200 km/s; these velocities drop to a few km/s for late-type stars, such as the Sun (type G2) (Slettebak [20]; courtesy Gordon & Breach)

Fig. 2.2 *Panel A* The *blue curve* is the median equatorial velocity $(4/\pi) \langle v \sin i \rangle$ for each spectral type from Glebocki and Gnacinski (2005). The *green curve* shows the equatorial velocity of the *Kepler* targets, $\bar{v}(s.t.)$, derived from the measured rotation periods and the KIC radii. The *black points* show measurements by Reiners and Mohanty (2012). In this sample 201 stars have an upper $v \sin i$ limit of 4 km/s (due to instrumental limitations), these stars are represented by the *solid bar. Panel B* The rotation periods P_{rot} of the stars in our sample, averaged within each spectral type. *Panel C* The same as panel B, but for comparison we show the median of the rotation periods measured by McQuillan et al. (2013) (*black points* with *errorbars*), for the stars overlapping with our sample. Similarly, the *red curve* shows the median of the rotation periods found by Debosscher et al. (2011). *Shaded areas* and *error bars* span the *upper* and *lower* 34th percentile values from the median. Reproduced with permission from Astronomy & Astrophysics, © ESO



Rotation \rightarrow star cooler and fainter





FIG. 1.—Angular momentum per unit mass, as a function of mass fraction interior to a given cylinder about the axis of rotation, for three assumed laws of differential rotation (Cases A, B, and C) and for a uniformly rotating model (Case D) of $30 \mathfrak{M}_{\odot}$, log J = 52.73.

D: solid body rotation

<u>Rotation law</u>:

angular momentum distribution $j(m_w)$ as a function of, m_w , the mass fraction interior to the cylinder of radius w about the rotation axis.



Bodenheimer (1971) ApJ, 167, 153

1. Introduction

Massive stars are essential constituents of stellar populations and galaxies in the near and far Universe. They are among the most important sources of ionizing photons, energy, and some chemical species, which are ejected into the interstellar medium through powerful stellar winds and during their extraordinary deaths as supernovae (SN) and long gamma-ray bursts (GRB). For these reasons, massive stars are often depicted as cosmic engines, because they are directly or indirectly related to most of the major areas of astrophysical research.

Despite their importance, our current understanding of massive stars is still limited. This inconvenient shortcoming can be explained by many reasons on which we elaborate below. First, the physics of star formation mean that massive stars are rare (Salpeter 1955). Moreover, their lifetime is short, of a few to tens of millions of years (e.g., Ekström et al. 2012; Langer 2012). These factors make it challenging to construct evolutionary sequences and relate different classes of massive stars. This is in sharp contrast to what can be done for low-mass stars.

Second, one can also argue that the evolution of massive stars is extremely sensitive to the effects of some physical processes, such as mass loss and rotation (Maeder & Meynet 2000; Heger et al. 2000), that have relatively less impact on the evolution of low-mass stars. However, the current implementation of rotation in one-dimensional codes relies on parametrized formulas, and the choice of the diffusion coefficients has a key impact on the evolution (Meynet et al. 2013). Likewise, mass-loss recipes arising from first principles are only available for main sequence (MS) objects (Vink et al. 2000, 2001) and a restricted range of Wolf-Rayet (WR) star parameters (Gräfener & Hamann 2008). Third, binarity seems to affect the evolution of massive stars, given that a large portion of them are in binary systems that will interact during the evolution (Sana et al. 2012).

Fourth, our understanding of different classes of stars is often built by comparing evolutionary models and observations. However, mass loss may affect the spectra, magnitudes, and colors of massive stars, thus making the comparison between evolutionary models and observations a challenge. In addition to luminosity, effective temperature, and surface gravity, the observables of massive stars can be strongly influenced by a radiatively driven stellar wind that is characteristic of these stars. The effects of mass loss on the observables depend on the initial mass and metallicity, since they are in general more noticeable in MS stars with large initial masses, during the post-MS phase, and at high metallicities. When the wind density is significant, the mass-loss rate, wind clumping, wind terminal velocity, and velocity law have a strong impact on the spectral morphology. This makes the analysis of a fraction of massive stars a difficult task, and obtaining their fundamental parameters, such as luminosity and effective temperature, is subject to the uncertainties that comes from our limited understanding of mass loss and clumping. Furthermore, the definition of effective temperature of massive stars with dense winds is problematic and, while referring to an optical depth surface, it does not relate to a hydrostatic surface. This is caused by the atmosphere becoming extended, with the extension being larger the stronger the wind is. Stellar evolution models are able to predict the stellar parameters only up to the stellar hydrostatic surface, which is not directly reached by the observations of massive stars when a dense stellar wind is present. Since current evolutionary models do not thoroughly simulate the physical mechanisms happening at the atmosphere and wind, model predictions of the evolution of massive stars are difficult to be directly compared to observed quantities, such as a spectrum or a photometric measurement.



Fig. 4. Evolution of the ultraviolet **a**) (*top*) and optical spectra **b**) (*bottom*) of a non-rotating 60 M_{\odot} star. The evolution proceeds from top to bottom, with labels indicating the evolutionary phase, spectral type, scale factor when appropriate, age, and model stage according to Table 1. Note that certain spectra have been scaled for the sake of displaying the full range of UV and optical emission lines.

Initial Mass Function

The birthrate function B(M, t) is the number of stars per unit volume, with masses between M and M + dM that are formed out of ISM during time interval t and t + dt.

 $B(M,t) dM dt = \psi(t) \xi(M) dM dt$, where $\psi(t)$ is the **star formation rate** (SFR), and $\xi(M)$ is the **initial mass function** (IMF).

For the Galactic disk, SFR is $5.0 \pm 0.5 M_{\odot} \text{ pc}^{-2} \text{ Gyr}^{-1}$ integrated over the *z* direction.

IMF: many more low-mass stars than higher mass stars as a result of cloud fragmentation?

The IMF specifies the fractional distribution in mass of a newly formed stellar system. It is often assumed to have a simple power law $\xi(M) = cM^{-\alpha} = cM^{-(1+\Gamma)}$

In general, $\xi(M)$ extends from a lower to an upper cutoff, e.g., from 0.1 to 125 solar masses. Commonly used IMFs are those of Salpeter (1955), Scalo (1986), and Miller and Scalo (1979).



http://webast.ast.obs-mip.fr/hyperz/hyperz_manual1/node7.html

- Edwin Salpeter (1955) on solar-neighborhood stars (ApJ, 121, 161) Present-day LF \rightarrow mass-luminosity relation \rightarrow present-day mass function \rightarrow stellar evolution \rightarrow initial mass function $\alpha = 2.35$ or $\Gamma = 1.35$
- Glenn E. Miller and John M. Scalo extended work below 1 M $_{\odot}$ (1979, ApJS, 41, 513) $\alpha \approx 0$ for M < 1 M $_{\odot}$
- Pavel Kroupa (2002, Sci, 295, 82) $\alpha = 2.3 \text{ for } M > 0.5 \text{ M}_{\odot}$ $\alpha = 1.3 \text{ for } 0.08 \text{ M}_{\odot} < M < 0.5 \text{ M}_{\odot}$ $\alpha = 0.3 \text{ for } M < 0.08 \text{ M}_{\odot}$
- A universal IMF among stellar systems (SFRs, star clusters, galaxies) (Bastian et al. 2010, ARAA). But why?
THE LUMINOSITY FUNCTION AND STELLAR EVOLUTION

EDWIN E. SALPETER*

Australian National University, Canberra, and Cornell University Received July 29, 1954

ABSTRACT

The evolutionary significance of the observed luminosity function for main-sequence stars in the solar neighborhood is discussed. The hypothesis is made that stars move off the main sequence after burning about 10 per cent of their hydrogen mass and that stars have been created at a uniform rate in the solar neighborhood for the last five billion years.

Using this hypothesis and the observed luminosity function, the rate of star creation as a function of stellar mass is calculated. The total number and mass of stars which have moved off the main sequence is found to be comparable with the total number of white dwarfs and with the total mass of all fainter main-sequence stars, respectively.



Figure 1. Initial mass function for field stars in the solar neighborhood taken from a variety of recent studies. These results have been normalized at 1 M_{\odot} . For both the MS79 and Scalo 86 IMFs we have adopted 15 Gyr as the age of the Milky Way. Current work suggests that the upper end of the IMF (> 5M \odot) is best represented by a power–law similar to Salpeter (1955) while the low mass end (< 1M \odot) is flatter (Kroupa, Tout, and Gilmore 1993). The shape of the IMF from 1–5 M \odot is highly uncertain. From Meyer et al. (2000) Protostars & Planets IV

Orion Nebula Cluster





α [J2000]

http://www.astro.caltech.edu/~jmc/papers/onc/gif/figure1.gif



Fig. 12. *HR diagram for the Orion Nebula Cluster.* Triangles indicate lower limits in luminosity. Filled circles/triangles indicate proper motion cluster members plus all sources which have been identified as being externally ionized; open circles/triangles indicate that no proper motion information is available; crosses indicate proper motion nonmembers. Typical errors are ≤ 0.02 in log T_{eff} for late-type (K-M) stars but increase towards earlier spectral types, and ≤ 0.2 in log (L_e, IL_\odot) at all spectral types. Two luminosities are plotted for all stars later than M7, with the asterisk indicating the luminosity calculated assuming the star has the V-I color and bolometric correction of an M7 star; see text. Superimposed are the zero-age main sequence and the pre-main sequence evolutionary tracks of D'Antona & Mazzitelli (1994, model 1); over the mass range from 0.1 M_☉ to 2.5 M_☉; Swenson *et al.* (1994, model F) from 3 M_☉ to 5 M_☉; and Ezer & Cameron (1967) from 10 M_☉ to 50 M_☉. The apparent trend of increasing stellar age with mass suggests errors in the zero point of the pre-main-sequence evolutionary tracks, i.e., the initial mass-radius relationship with which the calculations begin.



FIG. 13. Low-mass end of the HR diagram for the Orion Nebula Cluster. All lines and symbols are the same as in Fig. 12, with the pre-main sequence evolutionary calculations of D'Antona & Mazzitelli now shown down to 0.02 M_{\odot}. The hydrogen-burning mass limit of 0.08 M_{\odot} is emphasized. The temperature-spectral-type relationship over the range from K3–M9 is denoted. Note the locations of stars M6.5 and later relative to the tracks. These are probably young brown dwarfs. For a magnitude-limited sample restricted to $I_C < 17.5$ mag, our data begin to become incomplete at ages older than 1 Myr and masses less than 0.1 M_{\odot}, assuming a typical extinction of $A_V = 2$ mag.



FIG. 17. The Initial Mass Function as measured in the Orion Nebula Cluster.

Hillenbrand 1997, AJ, 113, 1733



Fig. 9. The IMF determined in a number of young (< 10 Myr) clusters and star forming regions (offset for clarity). The solid lines show the log-normal model that best fits the Pleiades (see Fig. 8). The MFs may be generally consistent with that of the Pleiades but the MF of Upper Sco is quite different. Figure constructed by Bouvier & Moraux.

Jeffries 2012

Stellar Initial Mass Function and Dense Core Mass Function



Andre et al. (2000) Protostars & Planets IV 97

Formation of Massive Stars

D Competitive accretion (of cloud cores)

... low-mass protostars competing with each other, and accrete matter from the parent molecular cloud

Coalescence of two or more stars with lower masses