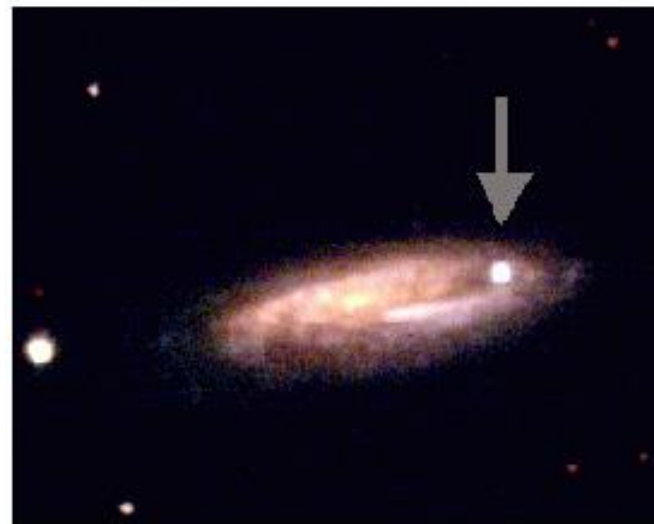
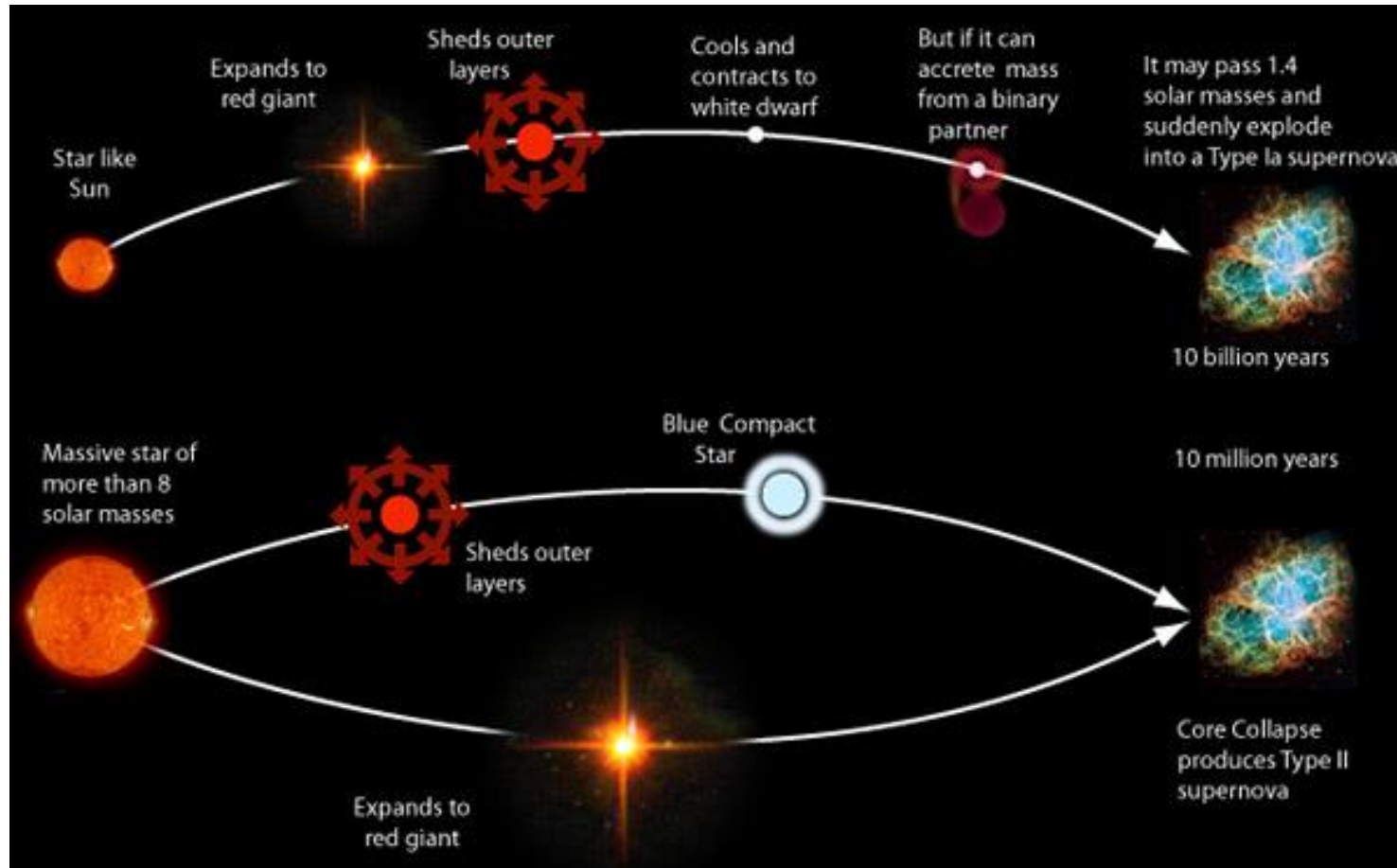


# Supernovae



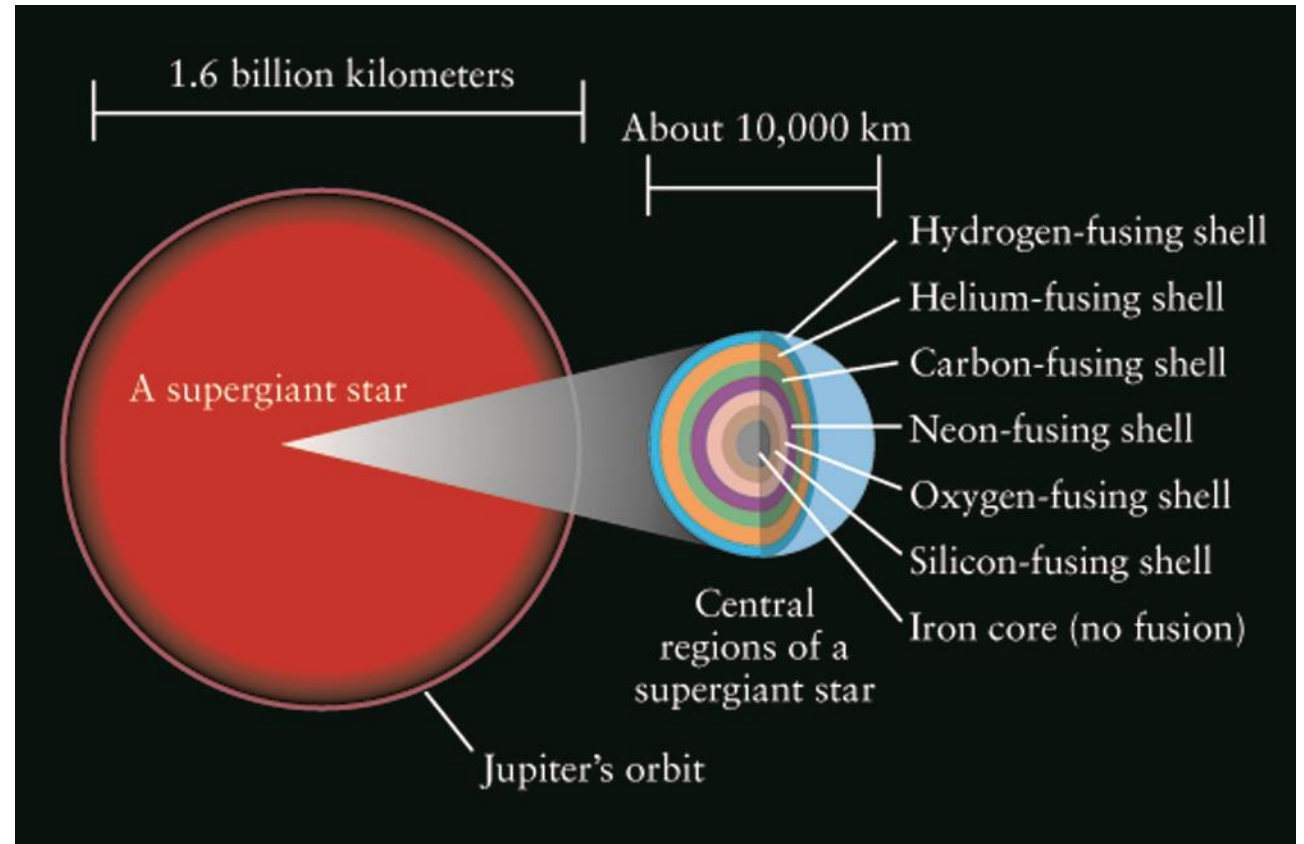
# Possible evolutionary paths

- Core collapse
- Thermonuclear runaway



# Evolution of an Intermediate-mass (8 to 25 $M_{\odot}$ ) or High-mass ( $> 25 M_{\odot}$ ) Star

- ❑ Core size  $\sim$  Earth
- ❑ Layers of nuclear reactions (cf an onion)
- ❑ Envelope as a supergiant, with the diameter comparable to the Jupiter's orbit



Each subsequent reaction proceeds ever faster; silicon  $\rightarrow$  iron

An iron nucleus most compact between protons and neutrons

$\rightarrow$  further fusion does not release energy

$\rightarrow$  iron core collapses ( $D \sim 3000$  km, collapses in 0.1 s)

Evolutionary Stages of a $25-M_{\odot}$ Star			
Stage	Central temperature (K)	Central density ( $\text{kg}/\text{m}^3$ )	Duration of stage
Hydrogen fusion	$4 \times 10^7$	$5 \times 10^3$	$7 \times 10^6$ yr
Helium fusion	$2 \times 10^8$	$7 \times 10^5$	$5 \times 10^5$ yr
Carbon fusion	$6 \times 10^8$	$2 \times 10^8$	600 yr
Neon fusion	$1.2 \times 10^9$	$4 \times 10^9$	1 yr
Oxygen fusion	$1.5 \times 10^9$	$1 \times 10^{10}$	6 mo
Silicon fusion	$2.7 \times 10^9$	$3 \times 10^{10}$	1 d
Core collapse	$5.4 \times 10^9$	$3 \times 10^{12}$	0.2 s
Core bounce	$2.3 \times 10^{10}$	$4 \times 10^{17}$	milliseconds
Supernova explosion	about $10^9$	varies	10 seconds

Iron core collapse  $\rightarrow$  5 billion K  $\rightarrow$  **photodisintegration** by energetic gamma rays

The star spends millions of years on the main sequence, synthesizing simple nuclei such as H and He to iron, then takes less than a second to disintegrate back to protons, neutrons and electrons.

Density of the core  $\nearrow \nearrow$ , reaching  $4 \times 10^{17}$  kg/m<sup>3</sup> (cf density of a nucleus) in  $< 1$  s  $\rightarrow$  even the electron degenerate pressure cannot support the core  $\rightarrow e^- + p^+ \rightarrow n^0 + \nu$

Core supported by neutron degenerate pressure  
 $\rightarrow$  **neutron star**

Core bounces  $\rightarrow$  **supernova explosion** + **supernova remnant**

# Evolution of A Binary System

- Both stars of a few solar masses
- More massive component  $\rightarrow$  RG  $\rightarrow$  transfers and loses mass  $\rightarrow$  a hot WD
- Secondary  $\rightarrow$  RG  $\rightarrow$  fills the Roche lobe  $\rightarrow$  transfers mass to the hot WD via an accreting disk
- Accreted material compressed and heated, and if  $T > 10^7$  K  $\rightarrow$  CNO takes place at the base of the accreted layer (even with a thermonuclear runaway if the material is degenerate)

$\rightarrow$  A **nova** explosion

If accretion onto a C-O WD  $\rightarrow$  core mass  $> M_{\text{Ch}} = 1.4 M_{\odot}$

$\rightarrow$  Catastrophic collapse + C burning  $\rightarrow$  a Type Ia **supernova**

“A nova is a transient, possibly recurring, outburst of a low-luminosity star.”

Absolute mag  $-6$  to  $-9$

Expanding shell (500–2000) km/s

Each outburst ejects  $10^{-4} - 10^{-6} M_{\odot}$   
(not a lot! hence possible recurrent events for a single system)

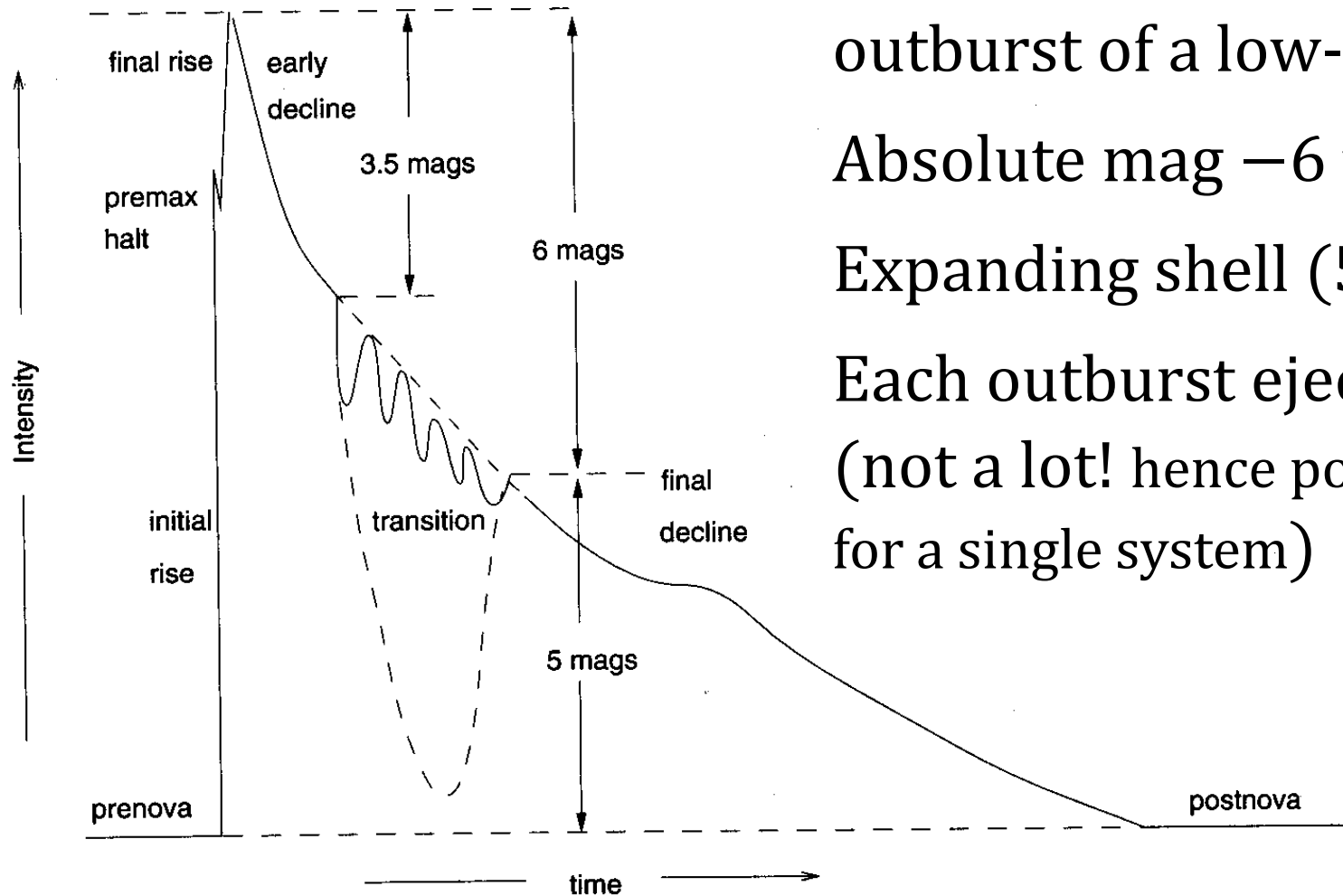


Fig. 7.10. Schematic light curve for a typical nova; the time axis is arbitrary and not to scale.

# Accreting Binary Systems

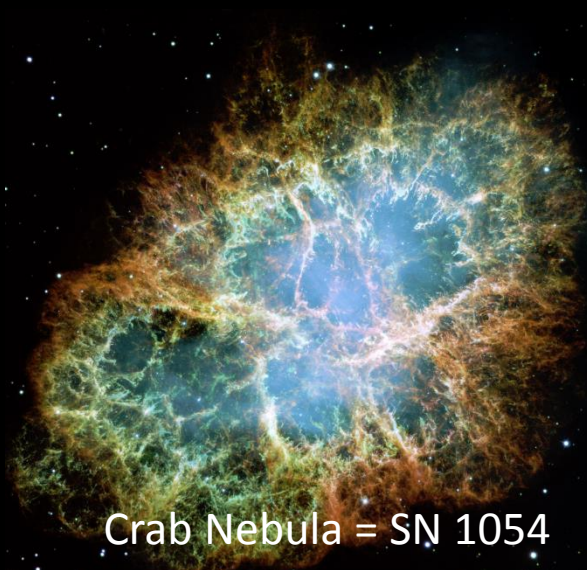
A semi-detached binary system with the primary being a WD: (in increasing L)

- ✓ dwarf nova
- ✓ classical nova
- ✓ type Ia supernova

Table 7.4. Taxonomy of binary systems

Name	Description	Remarks
Algols	Two normal stars (main sequence or subgiants): semidetached binary	Provide checks on stellar evolution, information on mass loss
RS Canum Venaticorum	Chromospherically active binaries	Useful for studies of dynamo-based magnetic activity; exhibits starspot chromospheres, corona, and flares similar to the Sun
W Ursae Majoris	Short period (0.2–0.8 days) Contact binaries	High levels of magnetic activity, important for studying stellar dynamo model
Cataclysmic variables and novae	White dwarfs with cool M-type secondaries; short periods	Exhibits accretion phenomena and accretion disks
X-ray binaries	Neutron star or black hole as the compact component; powerful x-ray sources with $L_x > 10^{35} \text{ ergs s}^{-1}$	Study of structure and evolution of compact remnants; indirect evidence for black holes
$\zeta$ Aurigae/ VV Cephei	Long-period interacting binaries; Late-type supergiant plus a hot companion	Study of supergiant phase, especially atmospheres of supergiants

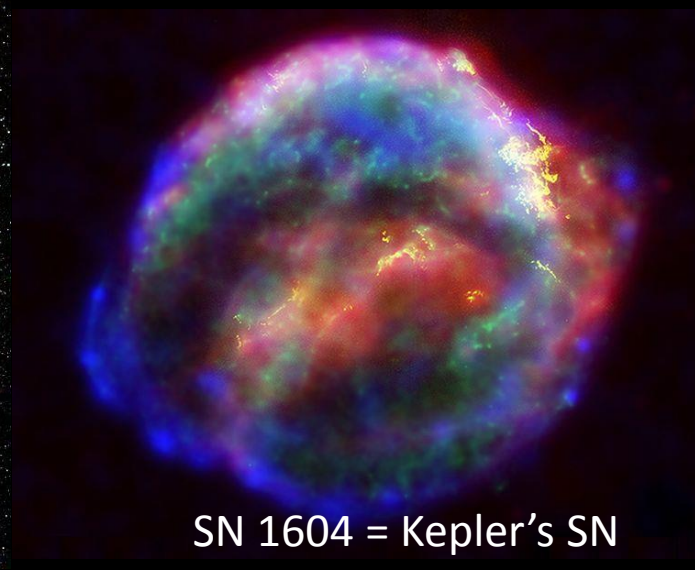




Crab Nebula = SN 1054



SN 1572 = Tycho's SN



SN 1604 = Kepler's SN



W49B SNR



N63A in LMC

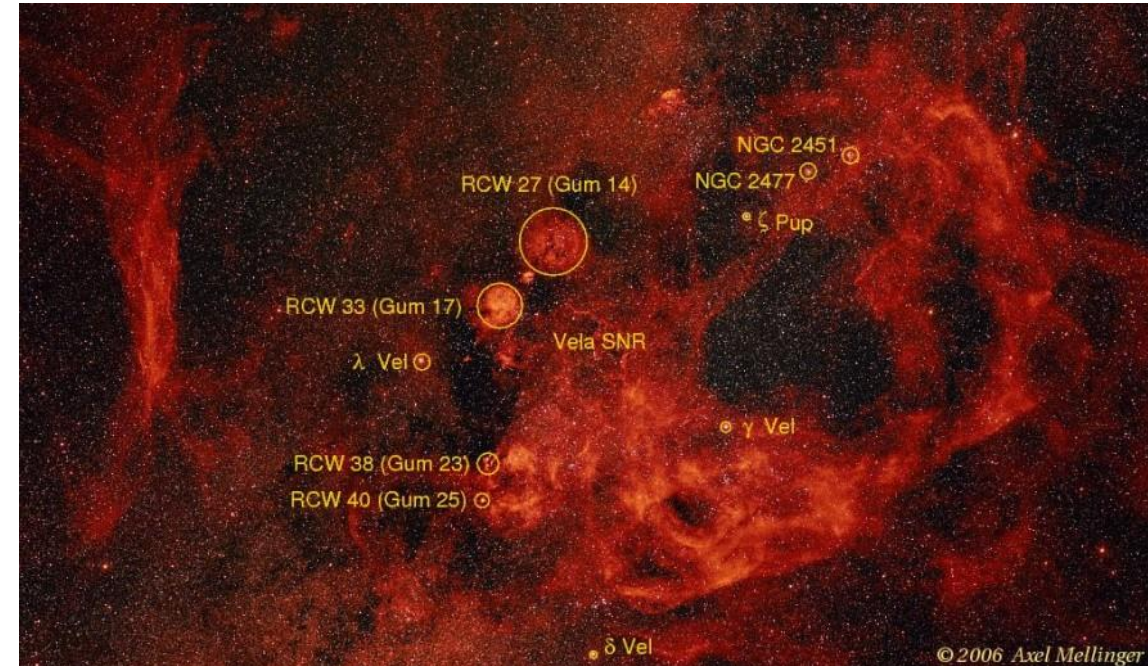


Vela SNR



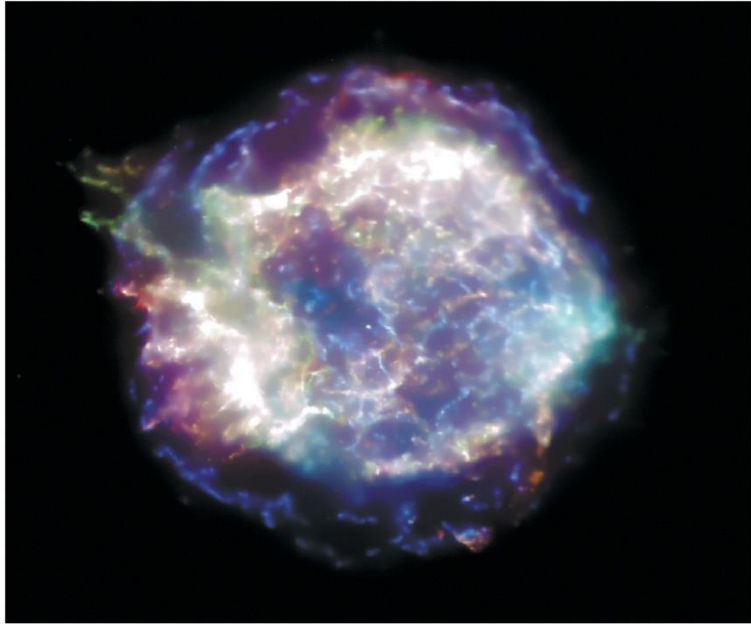
Figure 13-11  
*Discovering the Universe, Seventh Ed*  
 © 2006 W.H. Freeman and Company

**Gum Nebula** is the largest SNR in the sky, originated from a supernova explosion perhaps a Myr ago.

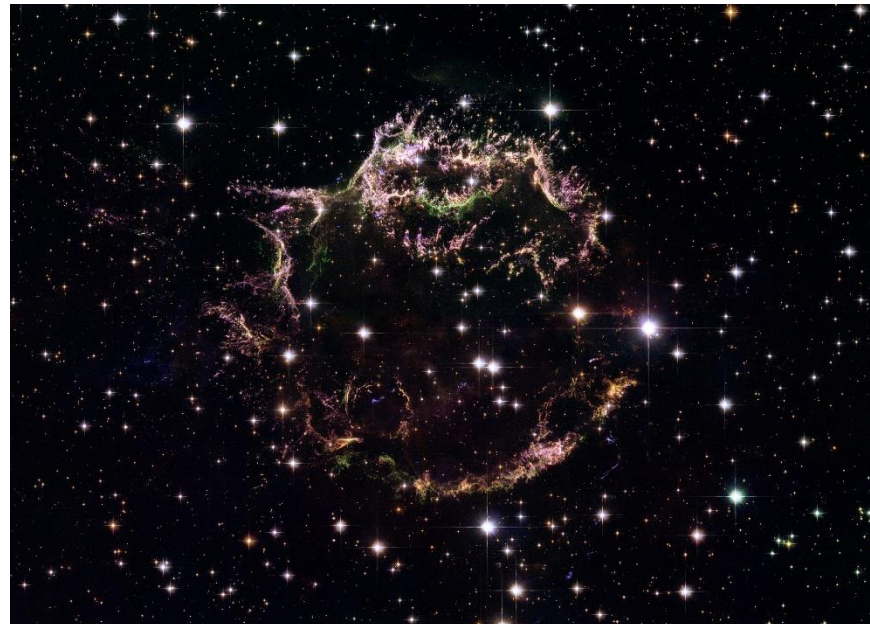


Gum Nebula has a angular extent  $> 40$  deg  $\rightarrow$  linear size more than 2300 ly across  $\rightarrow$  The closest part from Earth  $\sim 300$  ly

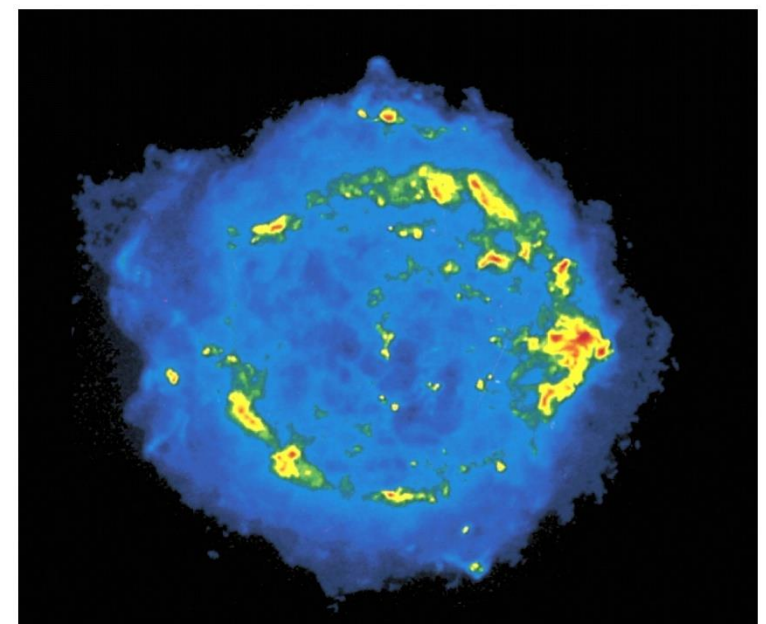
Cassiopeia A SNR is 3.4 kpc from us. The explosion should have been seen 300 years ago, but was not recorded.



X rays



Visible  
(HST)



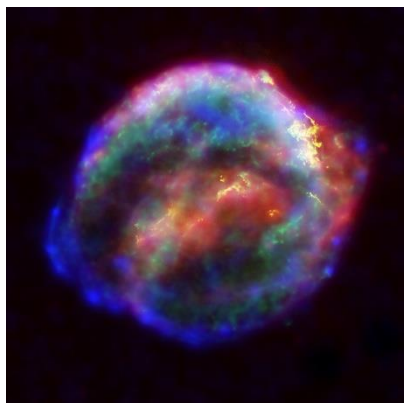
Radio

# Supernovae in History

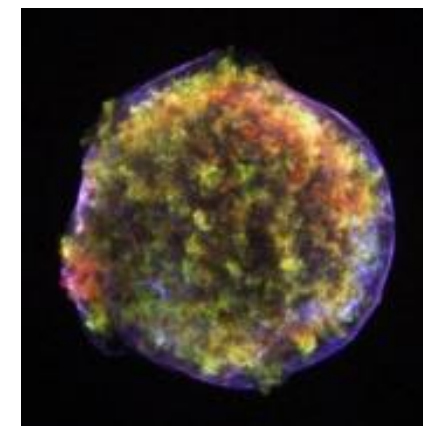
- OB association in Scorpius-Centaurus Solar system within 150 ly 2 Myr ago; should have experienced SN explosions

**Table 10.1** Historical supernovae

<i>Galaxy:</i> <i>Name</i>	<i>Year</i>	<i>Distance</i> <i>× 3000 ly</i>
Milky Way:		
Lupus	1006	1.4
Crab	1054	2.4
3C 58	1181(?)	2.6
Tycho	1572	2.5
Kepler	1604	4.2
Cas A	1658±3	2.8
Andromeda	1885	700
LMC: SN1987A	1987	50



Chandra SN1604



Chandra SN1572

# Crab Nebula (in Taurus)

# The Expanding Crab Nebula 1973 to 2001

SN clearly recorded in  
AD1054 by Chinese  
astronomers

→ “Chinese supernova”

西元1054年七月（宋仁宗至和元年五月）金牛座超新星爆炸，據記載最明亮時相當於太陽（金）星的光芒，長達23天在白天可見，直到1056年四月（宋嘉祐元年三月）肉眼才看不見。  
**天闕客星**



凡十一日没三年三月乙巳出東南方大中祥符四年正月丁丑見南斗魁前天禧五年四月丙辰出軒轅前星西北大如桃速行經軒轅太星入太微垣掩右執法犯次將歷屏星西北凡七十五日入濁没明道元年六月乙巳出東方近濁有芒彗至丁巳凡十三日没至和元年五月己丑出天關東南可數寸歲餘稍没熙寧二年六月丙辰出箕度中至七月丁卯犯箕乃散三年十一月丁未出天困元祐六年十一月辛亥出參度中犯掩側星壬子犯九游星十二月癸酉入奎至七年三月辛亥乃散紹興八年五月守婁



SN 1987A

First observed 24 Feb, 1987

not quite SN II

pre SN progenitor observed and sp. classified

Sanduleak - 69 202

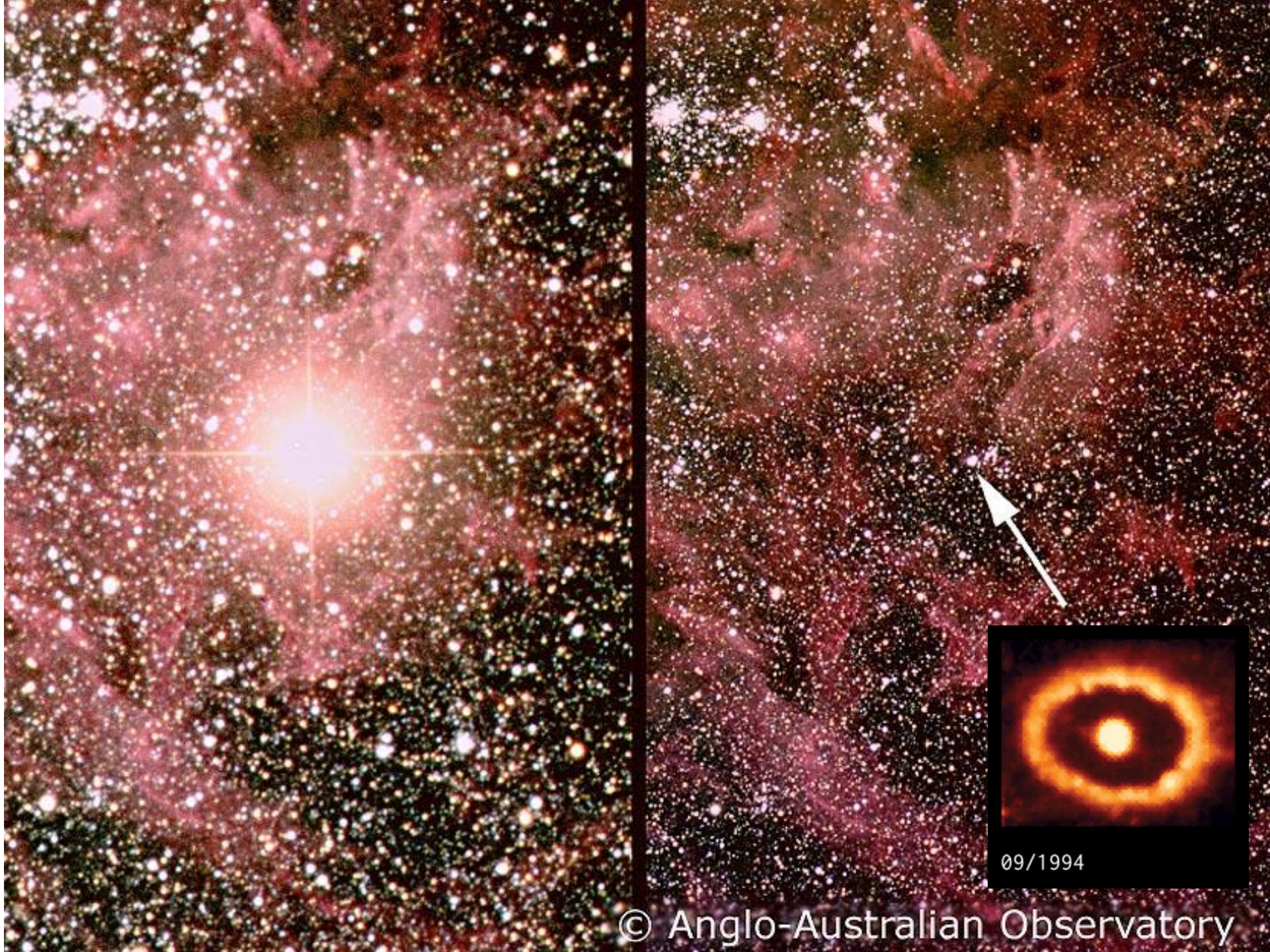
Sp = B3 I

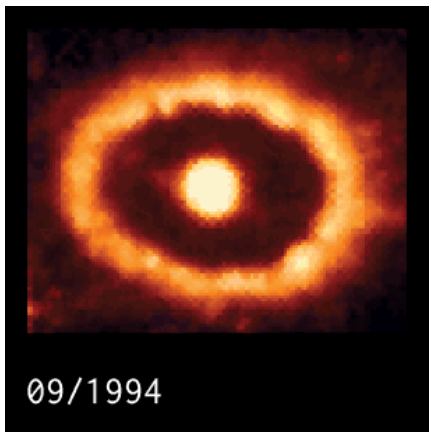
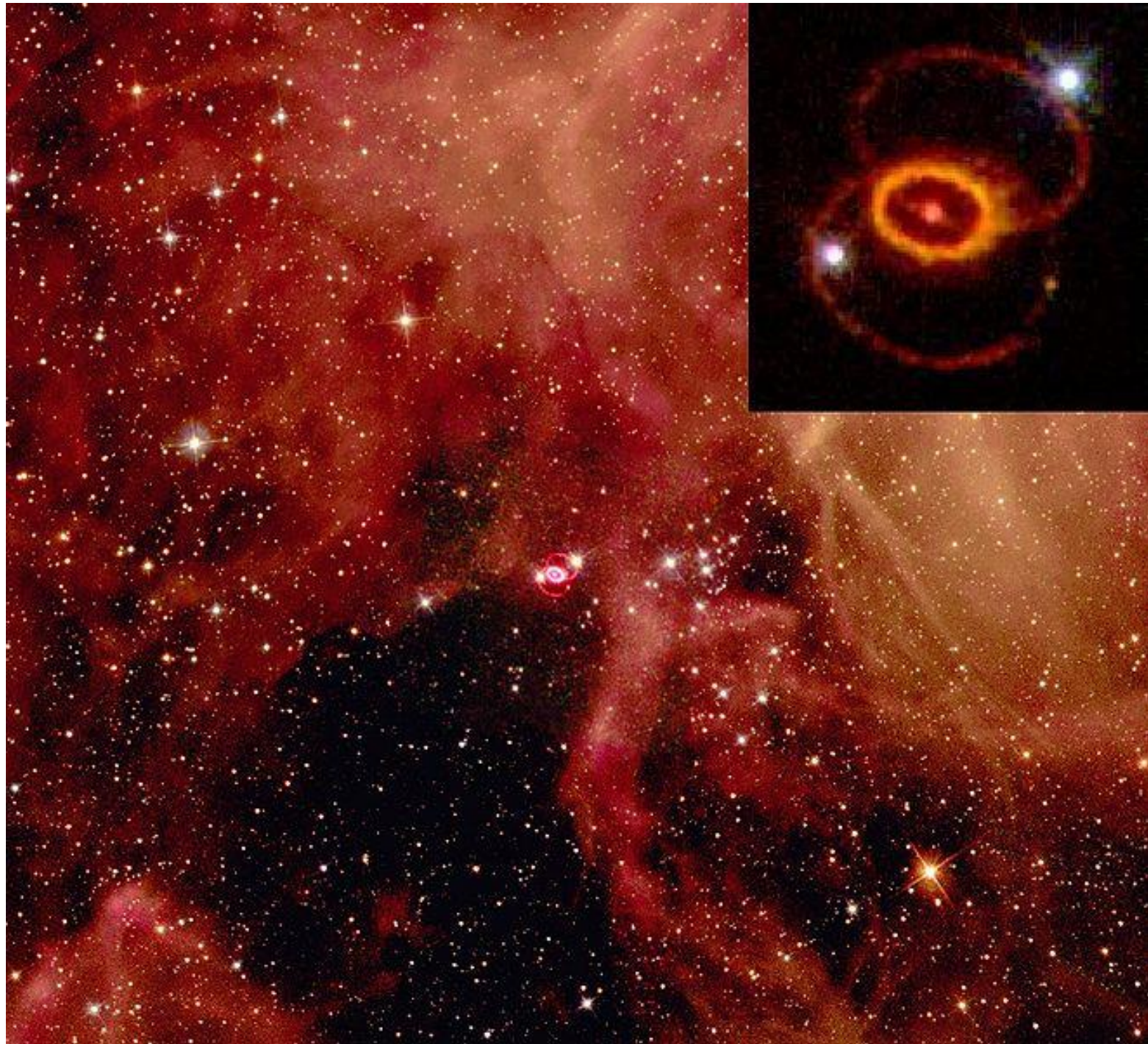
$L \sim 1.1 \times 10^5 L_{\odot}$  ;  $T_{\text{eff}} \sim 16,000 \text{ K}$

(  $M \sim 16 - 22 M_{\odot}$  )

Pop I but metal-poor

Neutrino events ( Kamiokande ) detected  
hours before SN visible





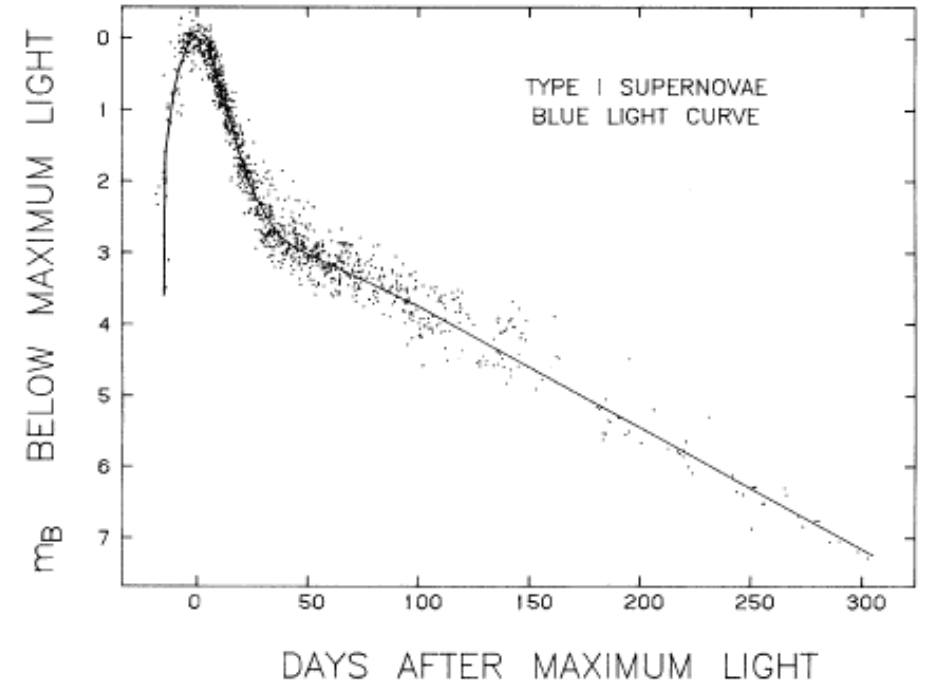


# Supernova classification

Divided into two types based on spectra

## Type I – with no H lines

- Further classification based also on spectra:
  - ✓ Ia – strong Si line
  - ✓ Ib – no H or Si line, but have He lines
  - ✓ Ic – no Si, He or H lines
- Ia found in all types of galaxies
  - ➔ associated with white dwarfs in binary systems



Doggett and Branch (1985)  
*Astron. J.*, **90**, 2303

# Supernova classification II

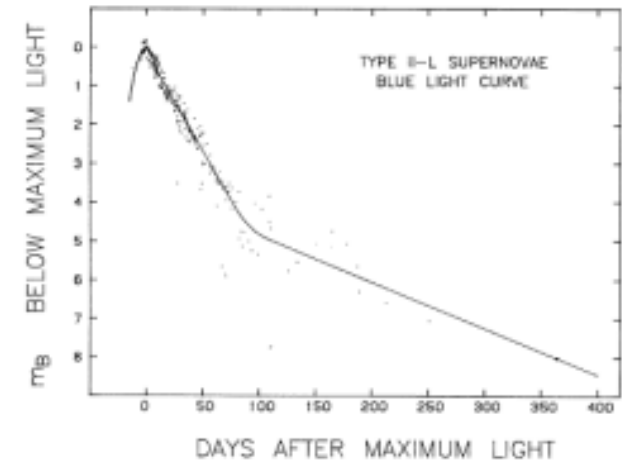
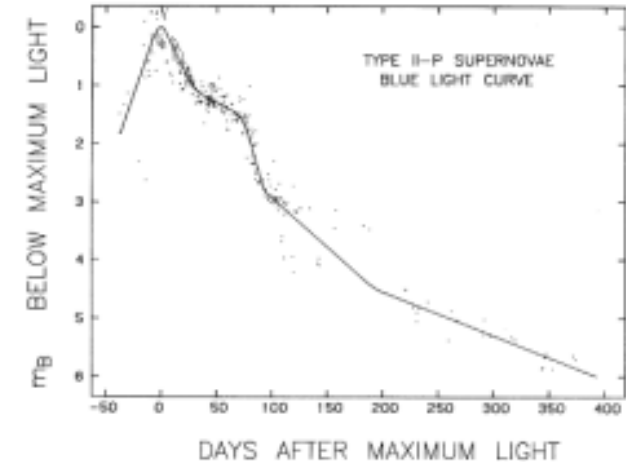
## Type II – with H lines

Further classification based on light curve

- ✓ II P – flat ‘plateau’ in LC
- ✓ II L - linear light curve

- Type II, Ib, Ic found only in spiral arms of spiral galaxies (i.e. regions of recent star formation) → massive stars

Core collapse supernovae with mass loss in Ib and Ic



Doggett and Branch (1985)  
*Astron. J.*, **90**, 2303

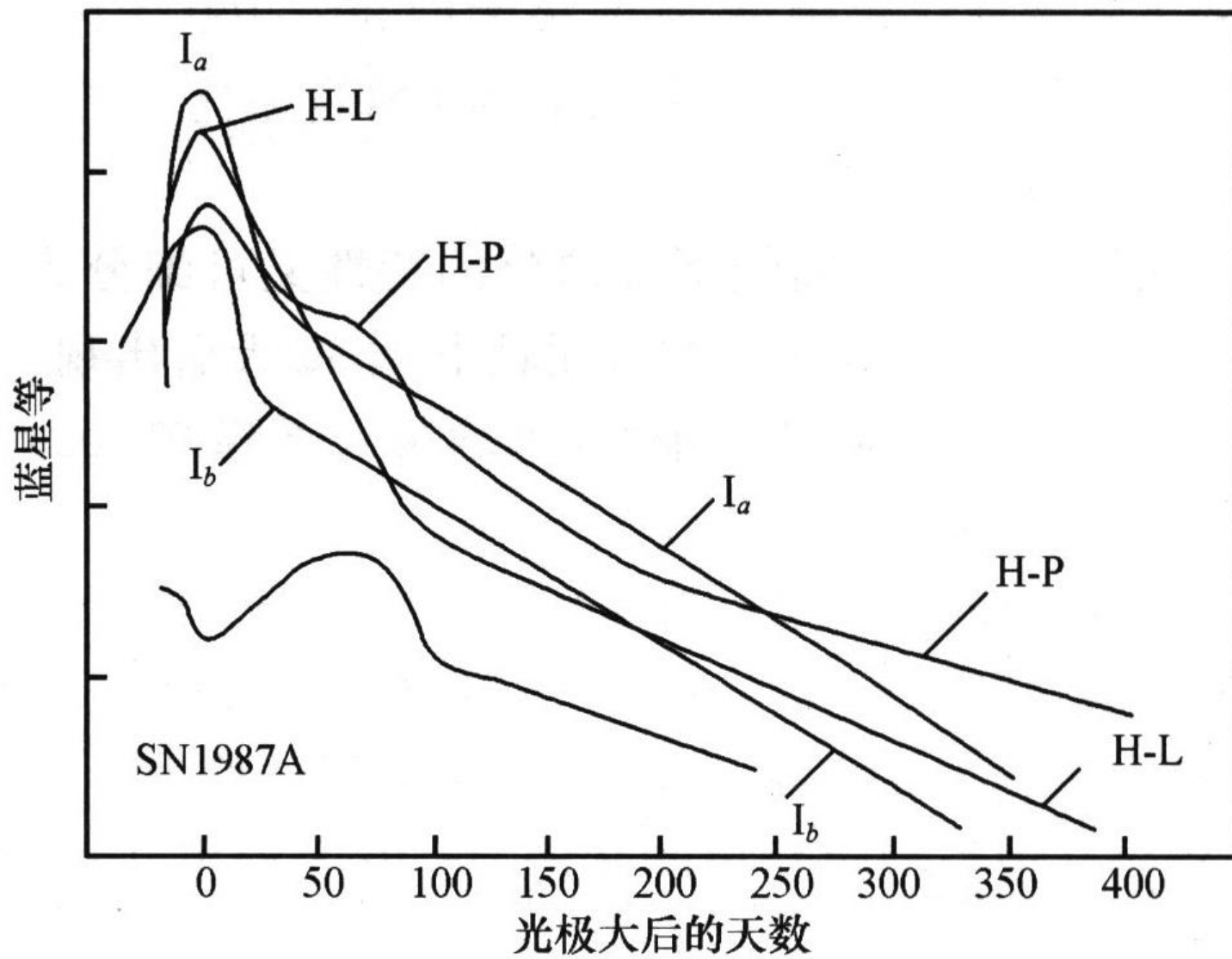
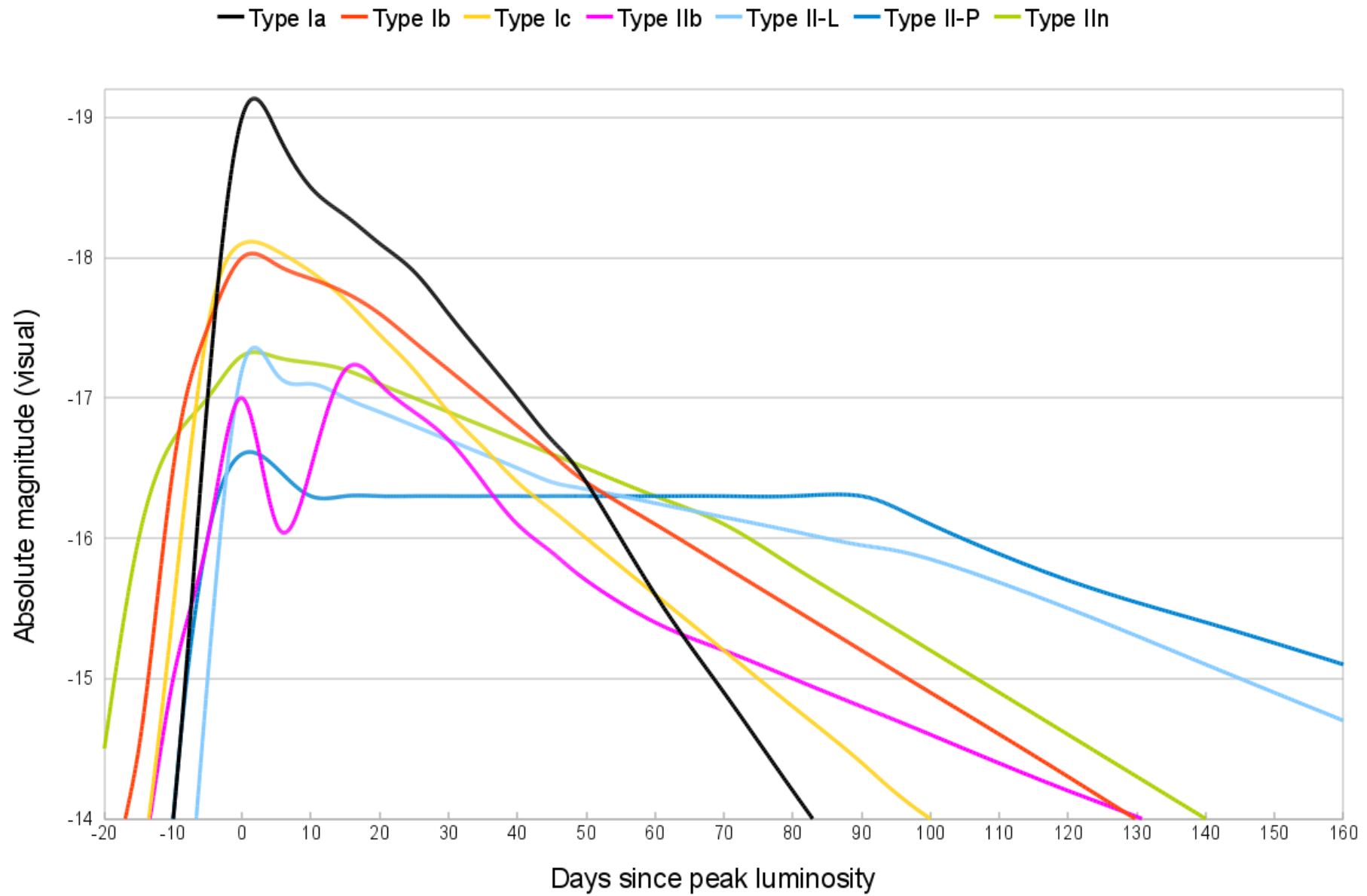


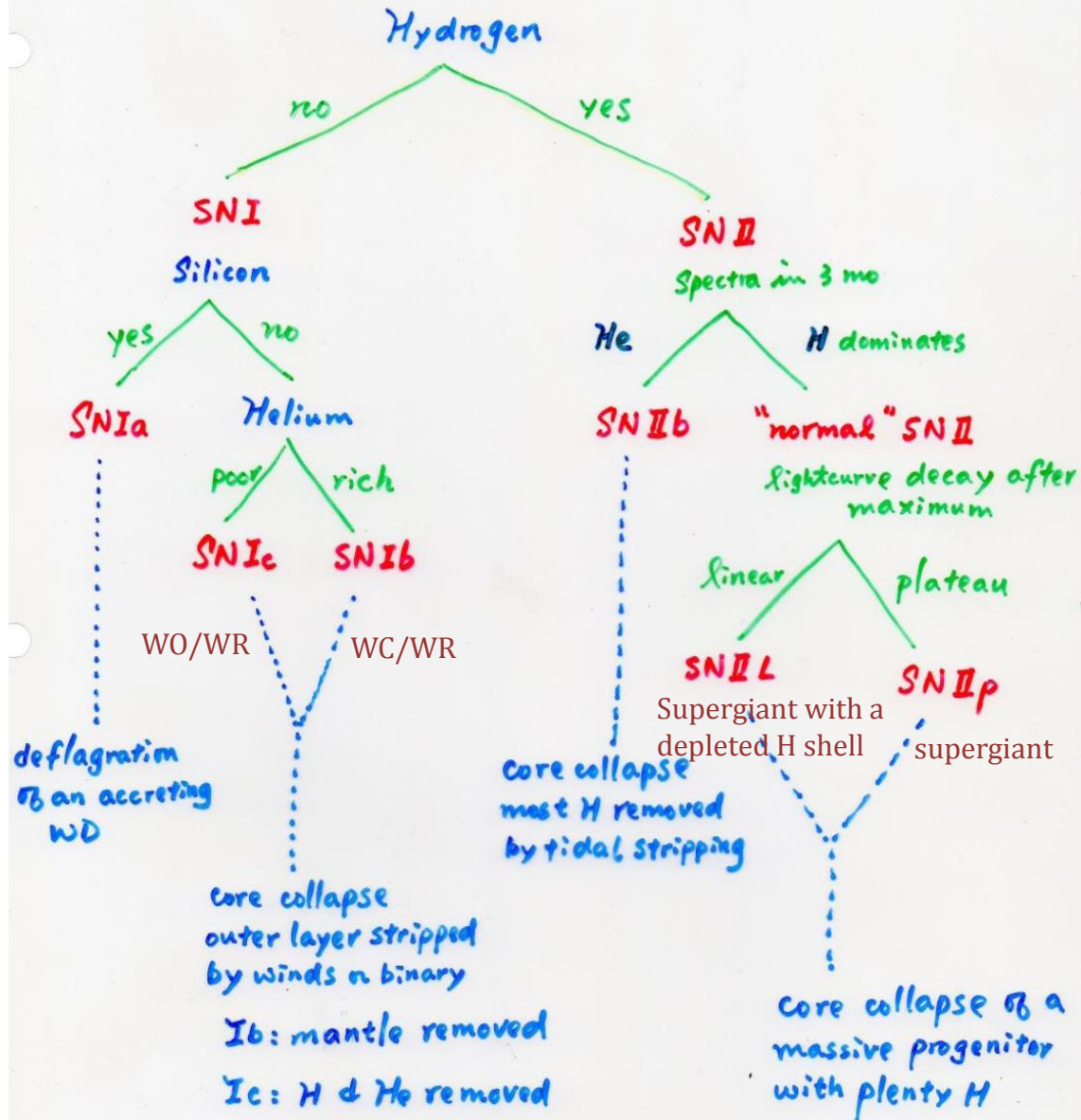
图 10.8 几种类型超新星的光变曲线(Wheeler, Harkness, 1992)



[http://upload.wikimedia.org/wikipedia/commons/e/e0/Comparative\\_supernova\\_type\\_light\\_curves.png](http://upload.wikimedia.org/wikipedia/commons/e/e0/Comparative_supernova_type_light_curves.png)

# Observational Classification of Supernovae

Early Spectra



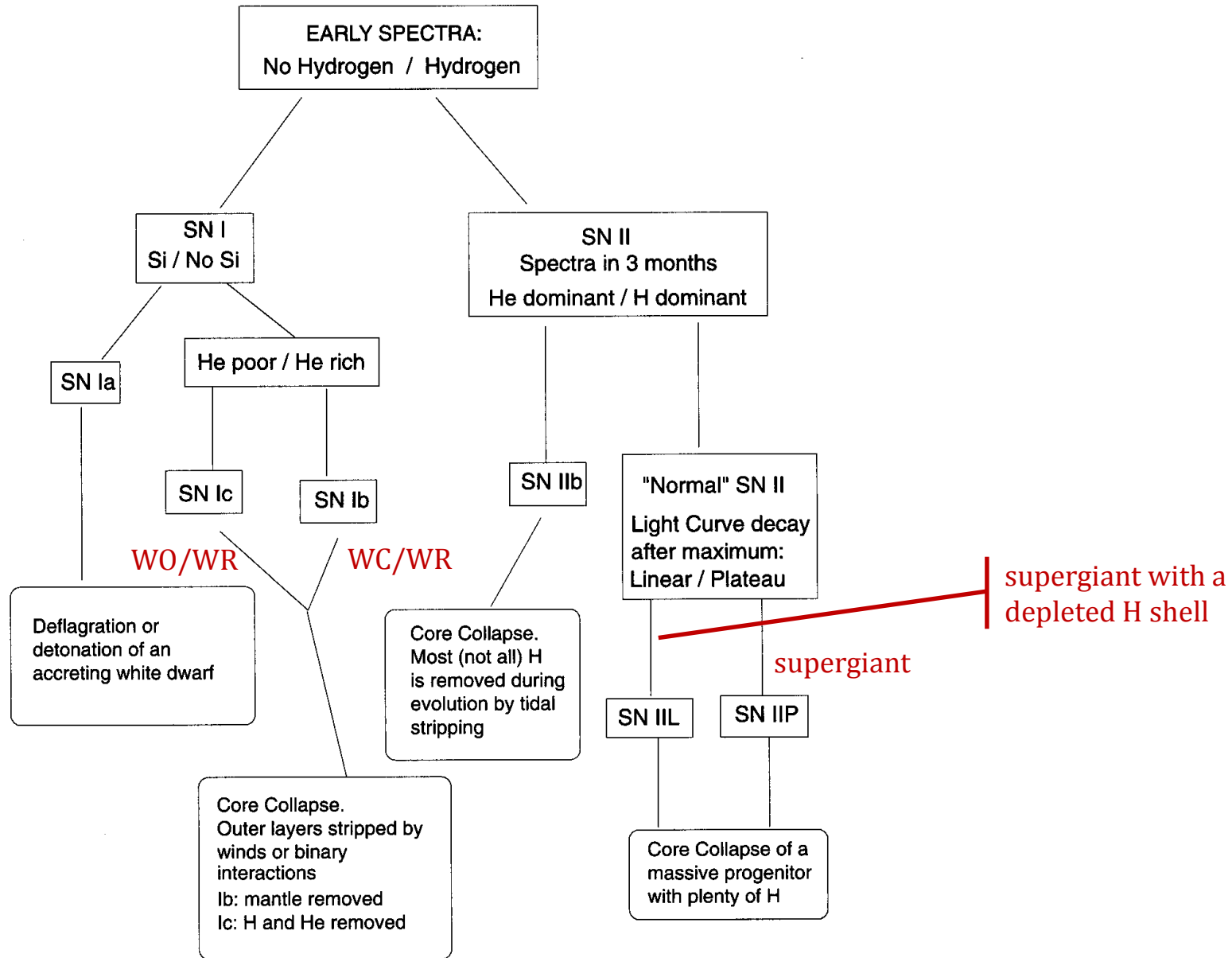


Fig. 7.12. Observational classification of supernovas (SNs).

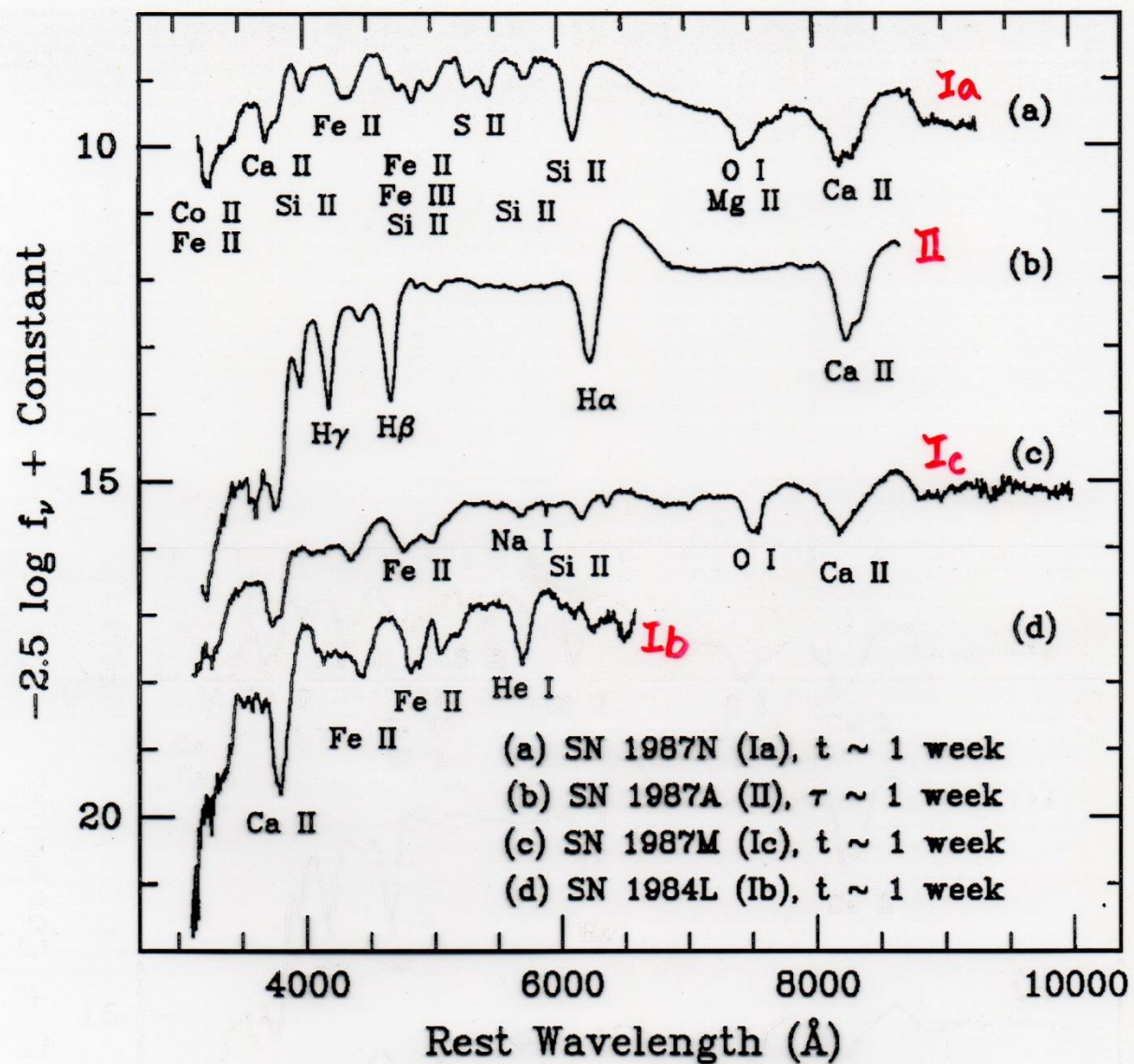


Figure 1 Spectra of SNe, showing early-time distinctions between the four major types and subtypes. The parent galaxies and their redshifts (kilometers per second) are as follows: SN 1987N (NGC 7606; 2171), SN 1987A (LMC; 291), SN 1987M (NGC 2715; 1339), and SN 1984L (NGC 991; 1532). In this review, the variables  $t$  and  $\tau$  represent time after observed B-band maximum and time after core collapse, respectively. The ordinate units are essentially “AB magnitudes” as defined by Oke & Gunn (1983).

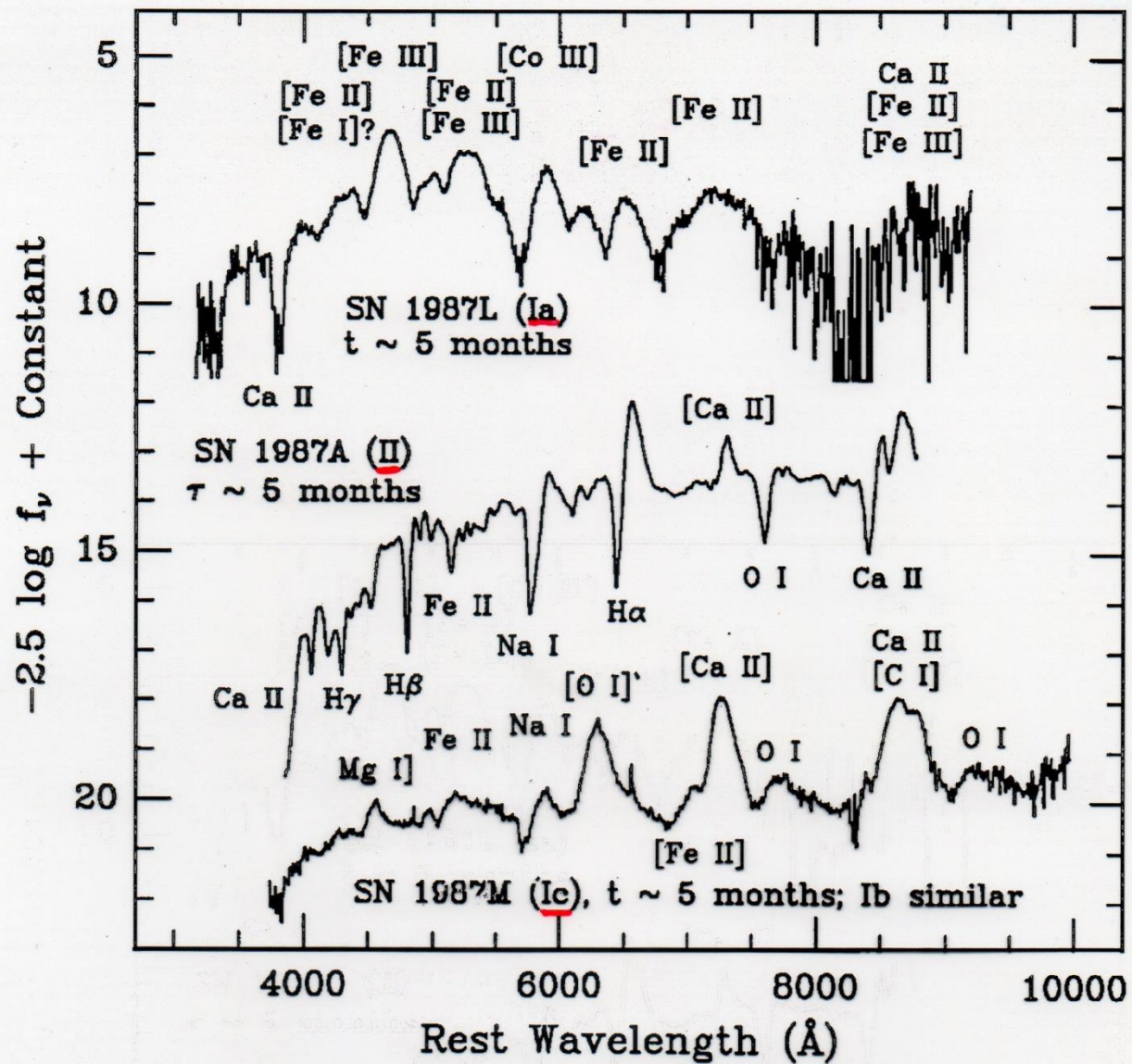


Figure 2 Spectra of SNe, showing late-time distinctions between various types and subtypes. Notation is the same as in Figure 1. The parent galaxy of SN 1987L is NGC 2336 ( $cz = 2206 \text{ km s}^{-1}$ ); others are listed in the caption of Figure 1. At even later phases, SN 1987A was dominated by strong emission lines of  $\text{H}\alpha$ ,  $[\text{O I}]$ ,  $[\text{Ca II}]$ , and the Ca II near-IR triplet, with only a weak continuum.



# Elements observed in SN I spectra

Subclass

~ maximum

~ 6 months

SN Ia

O, Mg, Si, S, Ca, Fe

Fe, Co

SN Ib

O, Ca, Fe

O, Ca, Mg

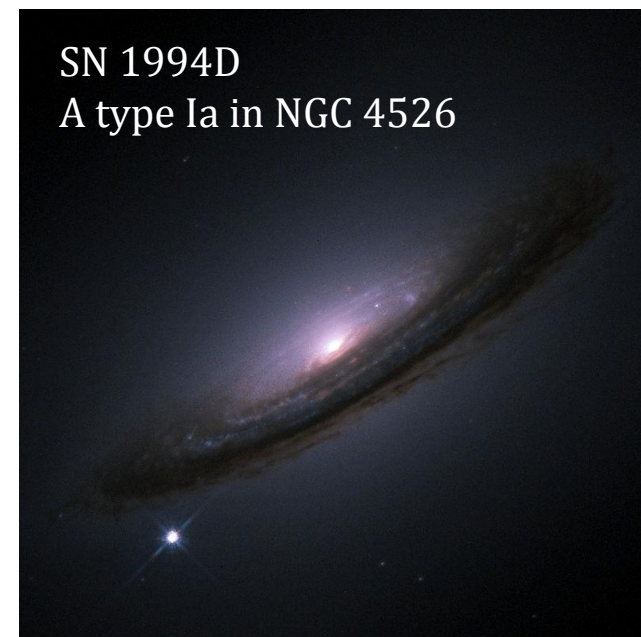
SN Ic

He, Fe, Ca

O, Mg

Hansen + Kawaler

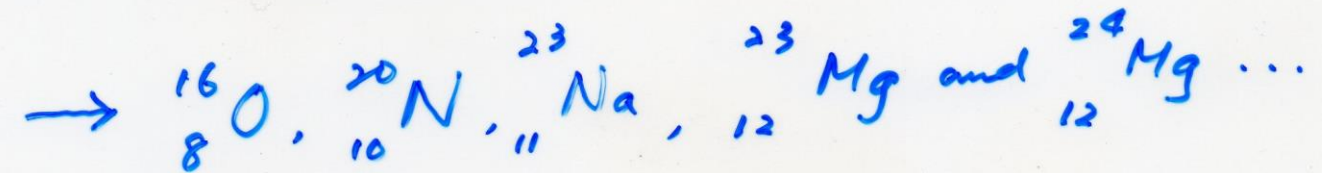
- The energy source of the type Ia supernovae comes from nuclear fusion. The explosion produces various radioactive isotopes , e.g., nickel becomes cobalt.
- So far, a few thousands SNe have been detected in external galaxies.
- Applying the statistics, the Milky Way should have occurred one type Ia SN every 36 years, and one type II SN every 44 years.
- Each century, therefore, we should have seen about 5 supernovae. So, what happened?
- Which is most likely the next? In the solar neighborhood?



SN 1994D  
A type Ia in NGC 4526

# Supernovae

$M > 8 M_{\odot}$  core carbon burning



Eventually  ${}_{26}^{54}\text{Fe}$ ,  ${}_{26}^{56}\text{Fe}$ , and  ${}_{28}^{56}\text{Ni}$

"iron" core

## Three critical processes

### ① Neutrino cooling

At this stage, a lot of  $\nu_s$

Ex. during Si burning, a  $20 M_{\odot}$

$$L_{20 M_{\odot}} \sim 4.4 \times 10^{38} \text{ erg s}^{-1}$$

$$L_{\nu} \sim 3.1 \times 10^{45} \text{ erg s}^{-1}$$

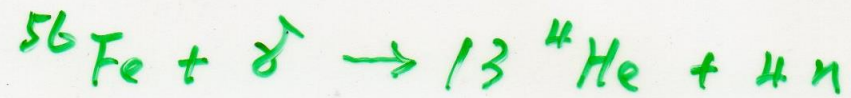
Solar neutrino flux  
 $= 7 \times 10^{10} / \text{cm}^2 / \text{s}$

Neutrino mass  
 $< 0.32 \text{ eV}$  for the sum of  
masses of 3 known flavors

## ② Photodisintegration

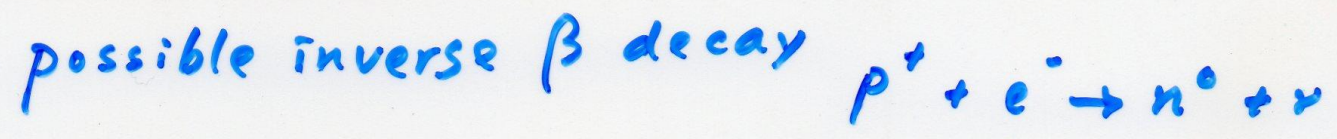
Energetic photons disintegrate iron nuclei  
into  $\alpha$  particles and protons

This is an <sup>吸熱</sup> endothermic process; i.e. takes  
energy away and lowers pressure support  
at the core



### 3. Neutronization

possible inverse  $\beta$  decay



$$n_e \downarrow \Rightarrow P_{deg} \downarrow$$

$\nu$  escape  $\Rightarrow$  cooling

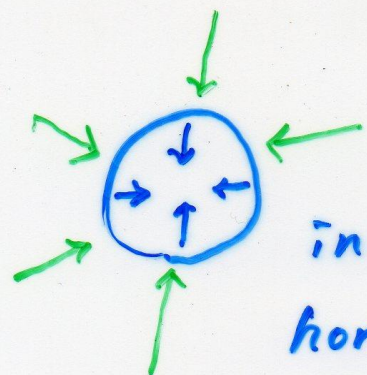
$\Rightarrow$  A rapid collapse of the core

Note

放熱

exothermic

releasing energy



Outer core/mantle

collapses supersonically (free fall)

$$v \sim 70,000 \text{ km s}^{-1}$$

inner core collapse

homologously (infall speed  $\propto$   
distance to center)  
subsonically

Inner core collapses until  $\rho_c \sim 8 \times 10^{14} \text{ g cm}^{-3}$

This is  $3 \times \rho_{\text{nucleus}} \rightarrow$  nuclear reactions  
produce repulsive force  
(cannot "squeeze" anymore)

This sends an outgoing pressure wave through  
the infalling material

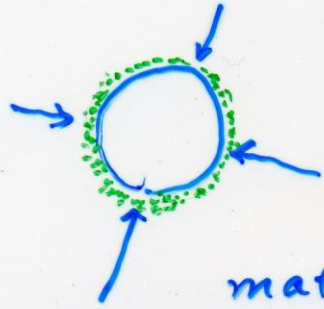
## Two possibilities

When the shock propagates through the inner core  $\rightarrow$  photodisintegration

- (i) If the iron core is small, shock emerges energetically  $\rightarrow$  an explosion on the outer material
- prompt hydrodynamic explosion

This can explain the explosion of MS stars with  $8 \sim 12 M_{\odot}$ , ending with a core  $< 1.2 M_{\odot}$ . But the progenitor of SN1987A had  $20 M_{\odot}$   $\rightarrow$  need an alternative mechanism to explain more massive SNe

(ii) If the core is massive, inner shock stalls



$$\rho_{\text{crit}} > 1.5 \times 10^{11} \text{ g cm}^{-3}$$

accretion  
shock

of protostars

material becomes so dense that even  $\nu$ s  
cannot escape  $\rightarrow$  formation of a  
neutrino sphere

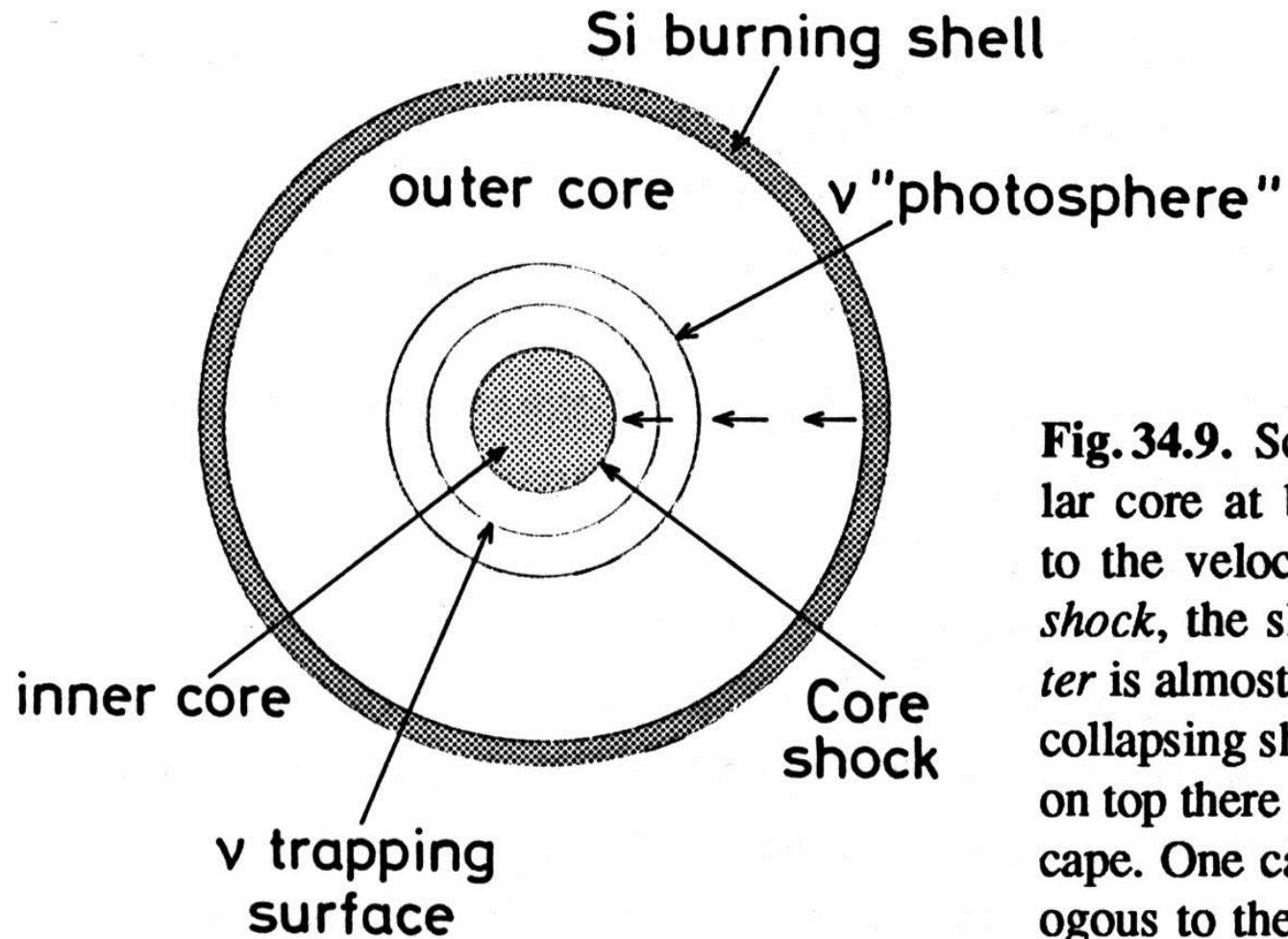
of photosphere of a  
star

$$\text{when } \rho > \rho_{\text{crit}} \quad \tau_{\text{diff}}^{\nu} > \tau_{\text{free fall}}$$

Thus deposits some energy to the inner shock  
 $\rightarrow$  explosion

delayed-explosion mechanism





**Fig. 34.9.** Schematic picture of a collapsing stellar core at bounce. The short arrows correspond to the velocity field. At the sphere labelled *core shock*, the shock is formed inside which the *matter* is almost at rest. Above the shock there is a still collapsing shell in which neutrinos are trapped. But on top there is a shell from which neutrinos can escape. One can define a neutrino photosphere analogous to the photosphere in a stellar atmosphere

Total kinetic energy of outgoing shock

$$\dot{E}_{kin} \sim 10^{51} \text{ ergs}$$

( this is only 1% of the energy in energy )  
neutrinos

→ outer material expands & becomes optically thin

⇒ SN explosion, releasing  $\sim 10^{49}$  ergs

in photons  
with  $L_{peak} \sim 10^{43} \text{ ergs}^{-1} \sim 10^9 L_{\odot}$

e.f.  $L_{\text{Milky Way}}$

Roughly if original mass  $< 2.5 M_{\odot}$ ; can be supported neutron pressure; may survive the explosion  $\rightarrow$  a neutron star

If  $M > 2.5 M_{\odot} \rightarrow$  collapse to a black hole

## Neutrino Trapping

Mean free path  $\lambda = 1/n\sigma$

Cross section  $\sigma = \sigma_0 \epsilon^2$

For neutrinos,  $\sigma_0 \sim 2 \times 10^{-44} \text{ [cm}^2\text{]}$

$\epsilon =$  relative energy in unit  
of  $e^-$  rest mass

In lead  $\rho = 11.34 \text{ g cm}^{-3}$ ,  $A = 208$

A neutrino of 1 MeV, or  $\epsilon = 2$ ,  $\lambda \sim 3.8 \times 10^{20} \text{ cm}$   
 $\sim 380 \text{ ly}$

In a collapsing stellar core

$$\rho \sim 4 \times 10^{14} \text{ g cm}^{-3}$$

Neutrinos have  $\sim 150 \text{ MeV}$ , or  $\epsilon \sim 300$

$$\rightarrow \lambda = 2.2 \text{ cm}$$

So if  $R \sim 10 \text{ km}$ , the mean free time, or

$$\text{diffusion time } \tau \sim \frac{1}{2} \text{ s}$$

# Supernova Observations

$$L_{\text{peak}} \sim 10^9 - 10^{10} L_{\odot}$$

Time before peak (rising time)  $\sim 2$  wks

$$\text{Shell expansion } v \sim 5 - 10 \times 10^3 \text{ km s}^{-1}$$

supernova remnant (SNR)

lasting  $\sim 10^3$  yrs

$$\bar{E}_{\text{total}} \sim 10^{51} - 10^{53} \text{ ergs} = \underbrace{\bar{E}_{\text{photons}}}_{\text{usually minor } (\sim 1\%)} + \underbrace{\bar{E}_{\text{neutrinos}} + \bar{E}_{\text{kinetic}}}_{\text{predominant}}$$

cooling core  $\rightarrow$  a neutron star

$$\rho \sim 10^{14} \text{ g cm}^{-3}, M \sim M_{\odot}$$

- 1932 Chadwick discovered the neutron.
- Landau thought neutron stars might exist.
- 1934 Baade & Zwicky suggested neutron stars as remnants of supernova explosions.
- 1939 Oppenheimer & Volkoff proposed the first model for neutron stars, with estimates of masses and sizes.
- 1967 Hewish & Bell discovered the pulsar.
- Gold & Pacini proposed pulsars as fast spinning, highly magnetized neutron stars.

Mass limit of neutron degenerate stars  
uncertain because of uncertain EOS at  
 $\rho > \rho_{\text{nuclear}}$ , ranging from  $0.7 M_{\odot}$  for  
non-interacting neutrons  
( Tolman-Oppenheimer-Volkoff limit )  
up to  $\sim 2.5 M_{\odot}$

A pulsar  $\left\{ \begin{array}{l} R \sim 10 \text{ km} \\ B \sim 10^{13} \text{ G} \\ \text{Spin down from periods } \sim \text{ms} \end{array} \right.$



Some SNRs host no pulsars.

- not enough  $e^-$ , not strong enough  $\vec{B}$ ?
- we are not in the 'lighthouse beam'?
- neutron star destroyed completely
- neutron star 'kicked out'

some NSs (or pulsars) have space motion  $\sim 1000 \text{ km s}^{-1}$

*Annu. Rev. Astron. Astrophys. 1992. 30: 359–89*

# TYPE Ia SUPERNOVAE AS STANDARD CANDLES

*David Branch*

Department of Physics and Astronomy, University of Oklahoma,  
Norman, Oklahoma 73019

*G. A. Tammann*

Astronomisches Institut der Universität Basel, Venusstrasse 7,  
CH-4102 Binningen, Switzerland, and European Southern Observatory,  
Karl-Schwarzschild-Str. 2, D-8049 Garching/München, Germany

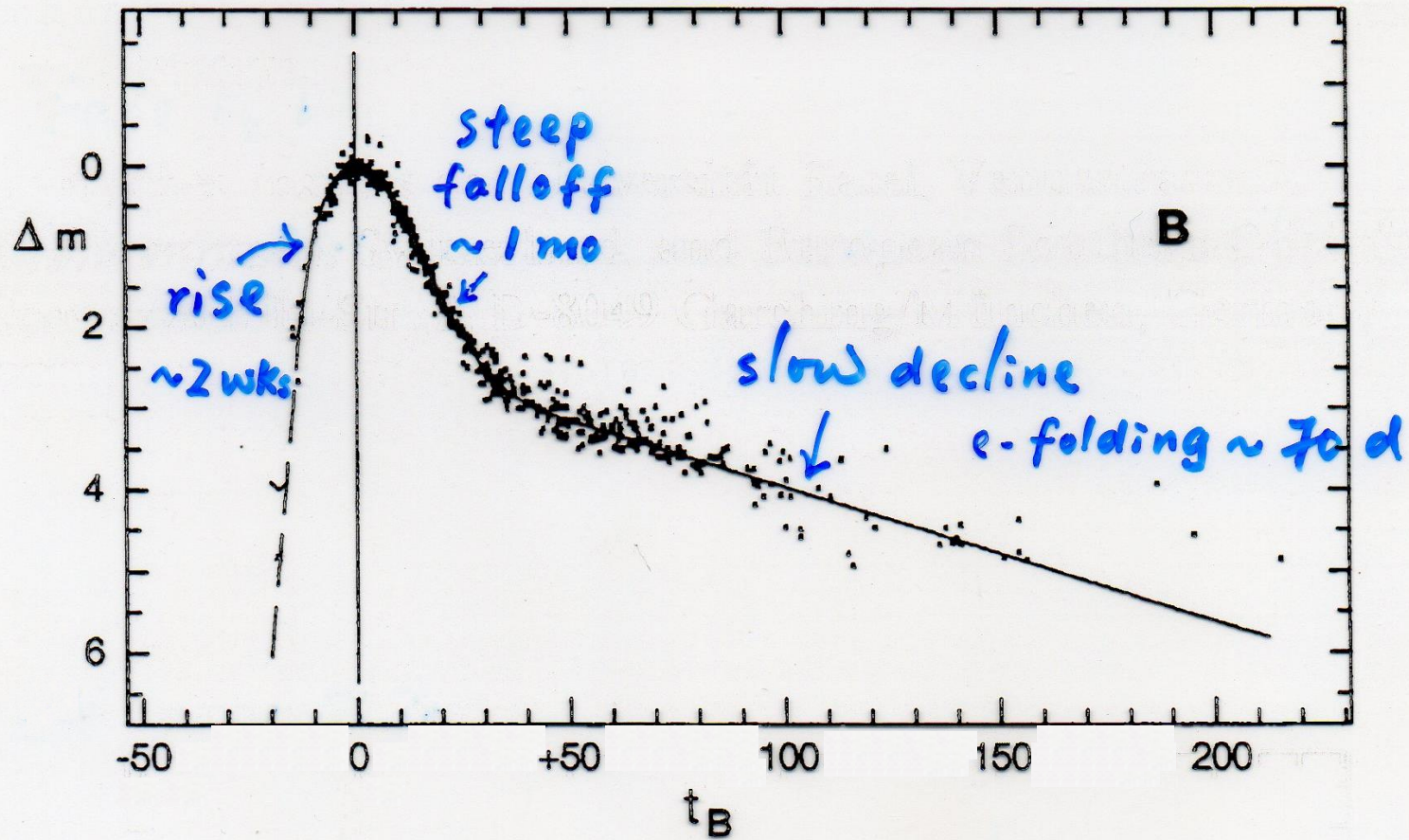


Figure 2 The standard B light curve (adapted from Cadonau 1987), based on observations of 22 SNe Ia.

Many sky survey projects, e.g., Pan-STARRS (PS), Palomar Transient Factory (PTF), Sky Mapper, Large Synoptic Survey Telescope (LSST), to catch SNe early on, for pre-SN characterization

## Type I

No H in spectra

Located in spirals or ellipticals

If in spirals, usually NOT in arms  
but some seen near H II regions or  
arms → Ib

Ia

Standard model

A WD close to Chandrasekhar limit  
+ a mass losing companion

→ accretion onto WD →  $R_{WD} \downarrow$

→  $T \uparrow$ , if heat not carried away

⇒ ignition of C, O, ...

thermonuclear explosion

Fate of WD depends on accretion rate and  $M_{WD}$

- partial explosion w/ a WD left behind
- disrupt completely; no stellar remnant
- NS?

Population II progenitor

SN Ia  $\sim$  80% of Type II

$M_{\text{peak}} \sim -17$  mag

All SN Ia lightcurves similar

→ standard candles

Averaged 1 SNI/100 yrs in a spiral

Type II  $M_{\text{peak}} \sim -19 \text{ mag}$

With hydrogen lines in spectra

Found in spiral arms or Irr.

If formed in the same arm

timescale  $< 10^7 \text{ yr} \Rightarrow M > 10 M_{\odot}$   
progenitor

Standard model

End of massive star evolution

gravitational collapse

Population I progenitor

Fate  $\rightarrow$  NS, BH

# Type II (core collapse) SN progenitors

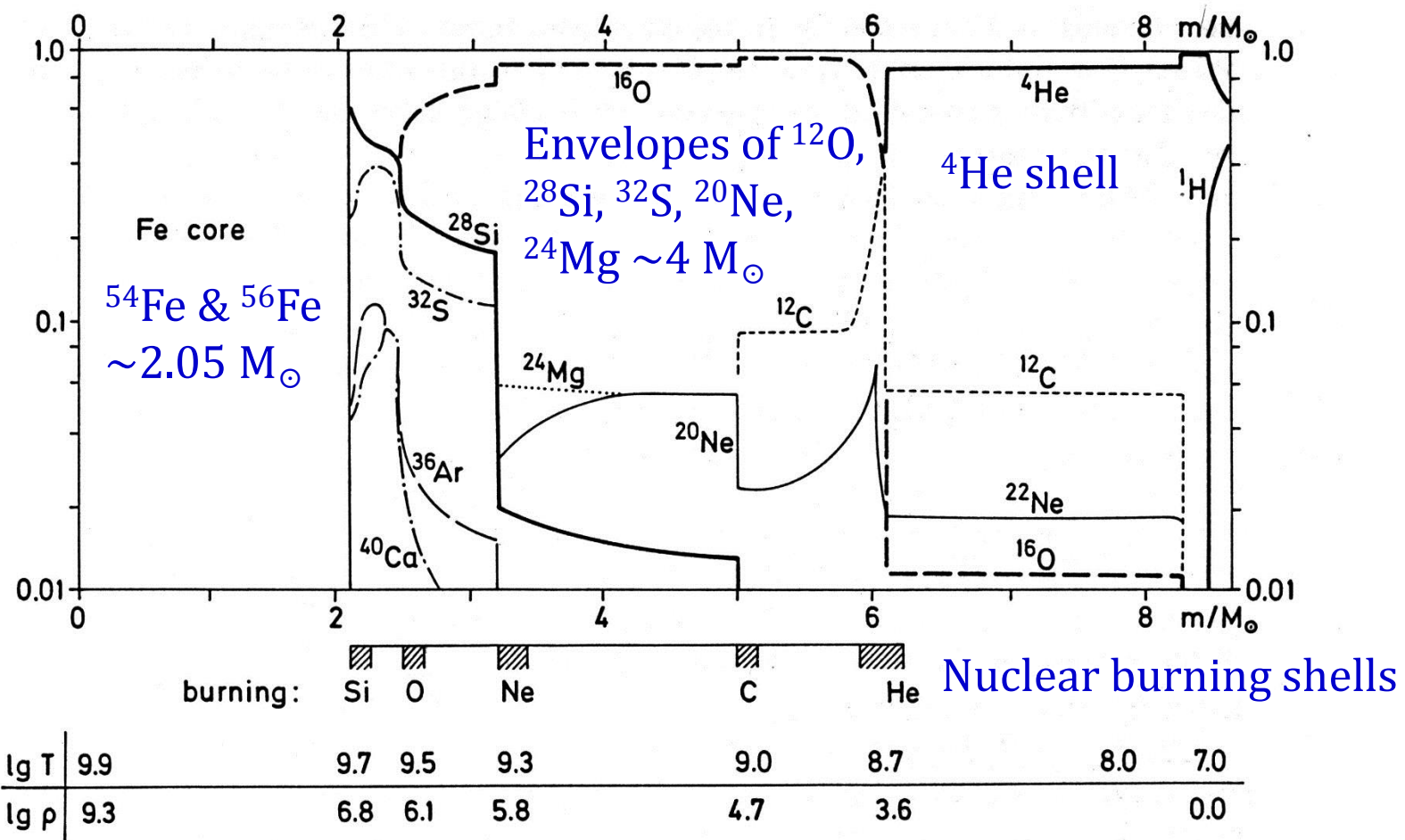


Fig. 34.7. The chemical composition in the interior of a highly evolved model of a  $25M_{\odot}$  star of population I. The mass concentrations of a few important elements are plotted against the mass variable  $m$ . Below the abscissa the location of shell sources and typical values of temperature (in K) and density (in  $\text{g cm}^{-3}$ ) are indicated. (After WOOSLEY, WEAVER, 1986)

# THE PHYSICS OF SUPERNOVA EXPLOSIONS<sup>1</sup>

*S. E. Woosley*

Board of Studies in Astronomy and Astrophysics, Lick Observatory,  
University of California, Santa Cruz, California 95064

*Thomas A. Weaver*

Special Studies Group, Lawrence Livermore National Laboratory,  
Livermore, California 94550

<sup>1</sup> The US Government has the right to retain a nonexclusive royalty-free license in and to any copyright covering this paper.



**Table 1** Presupernova models and explosions<sup>a</sup>

Main sequence mass	Helium core mass	Iron core mass	Explosion energy <sup>b</sup> ( $10^{50}$ erg)	Residual baryon mass <sup>b</sup>	Neutron star mass <sup>b</sup>	Heavies ejected ( $Z \geq 6$ )
11	2.4	— <sup>c</sup>	3.0	1.42	1.31	$\sim 0$
12	3.1	1.31	3.8	1.35	1.26	0.96
15	4.2	1.33	2.0	1.42	1.31	1.24
20	6.2	1.70	—	—	—	2.53
25	8.5	2.05	4.0	2.44	1.96	4.31
35	14	1.80	—	—	—	9.88
50	23	2.45	—	—	—	17.7
75	36	— <sup>d</sup>	—	—	BH?	30?
100	45	$\sim 2.3^d$	$\geq 4$	—	BH?	39?

<sup>a</sup> All masses given in units of  $M_{\odot}$ .

<sup>b</sup> All except for  $100 M_{\odot}$  determined by Wilson et al. (1985).

<sup>c</sup> Never developed iron core in hydrostatic equilibrium.

<sup>d</sup> Pulsational pair instability at oxygen ignition.

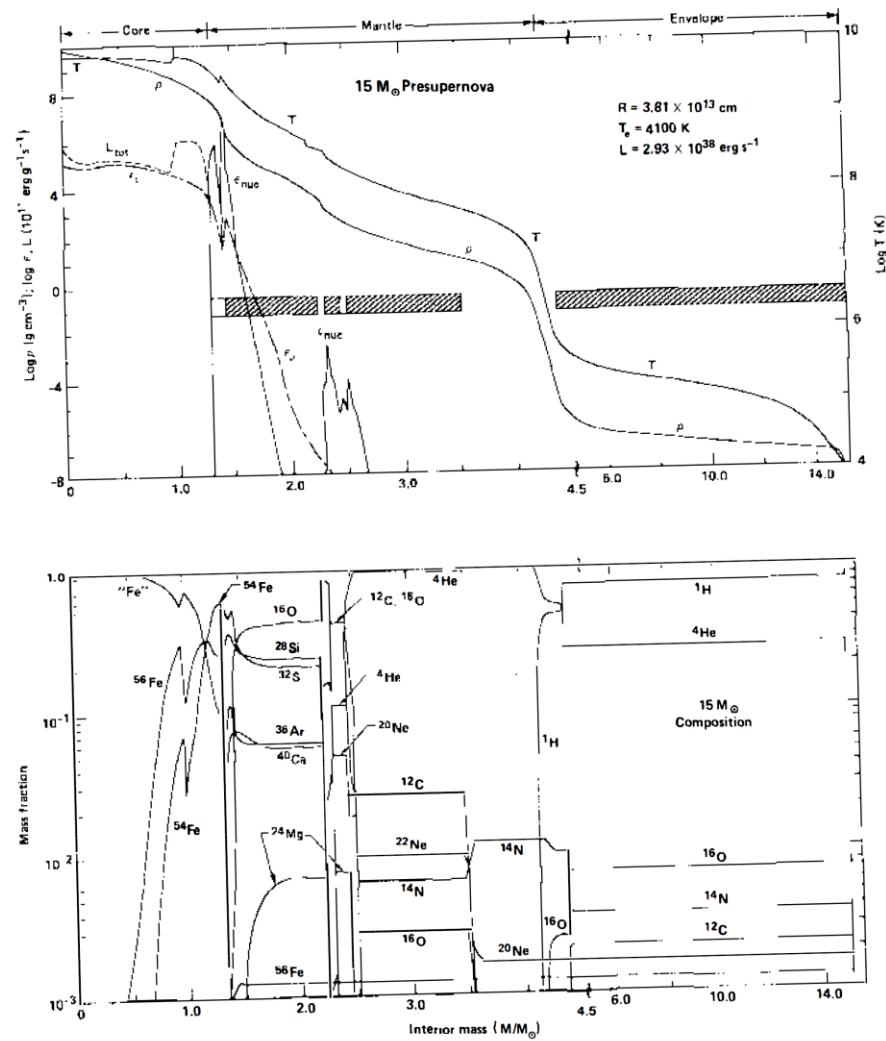
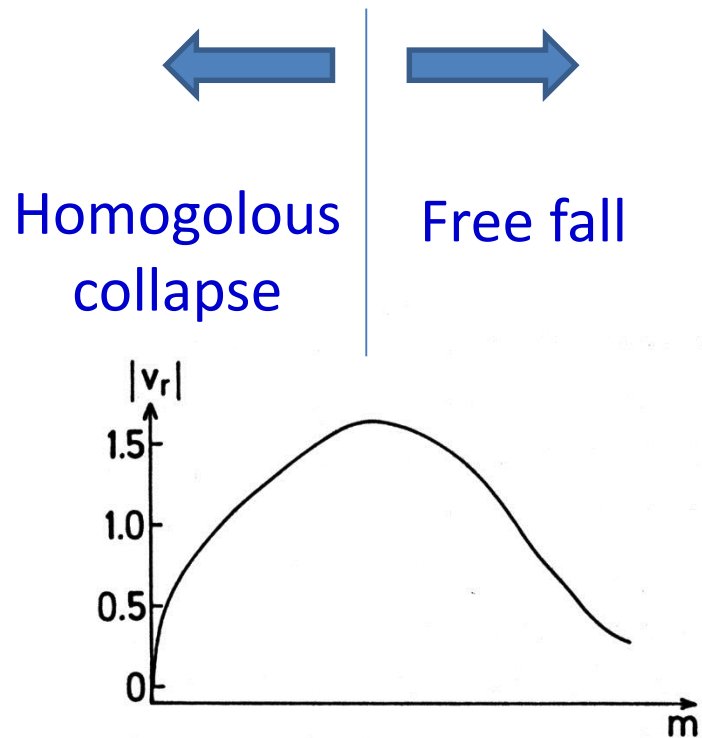


Figure 1 Structure and composition of a  $15 M_{\odot}$  presupernova star at a time when the edge of its iron core begins collapsing at  $1000 \text{ km s}^{-1}$ . Neutrino emission from electron capture ( $\epsilon_{\nu}$ ) dominates photodisintegration in the total energy losses ( $L_{\text{tot}}$ ) throughout most of the iron core. Central temperature here is  $7.62 \times 10^9 \text{ K}$  and density is  $9.95 \times 10^9 \text{ g cm}^{-3}$ . Spikes in the nuclear-energy generation rate ( $\epsilon_{\text{nuc}}$ ) show the location of active burning shells, while cross-hatched, blank, and open bars indicate regions that are convective, semiconvective, and radiative respectively. The species “Fe” includes all isotopes from  $48 \lesssim A \lesssim 65$  having a neutron excess greater than  $^{56}\text{Fe}$ . Note a scale break at  $4.5 M_{\odot}$ . Figure adapted from Woosley & Weaver (1985).

- ◆ Core collapse in free-fall,  
 $\tau_{\text{ff}} \approx (G\bar{\rho})^{-1/2} \approx 1 \text{ ms}$ , if  $\rho = 10^{10} \text{ g cm}^{-3}$
- ◆ Central density and pressure  $\uparrow \uparrow$  and becomes subsonic;  
 outer material remains free-fall and supersonic.
- ◆ Transition zone = constant speed, force free, relativistic  
 electron degenerate pressure balances gravity  
 $\rightarrow$  Chandrasekhar limit
- ◆ Inside  $M_{\text{ch}}$ ,  $\rho \approx 2.3 \times 10^{14} \text{ g cm}^{-3}$  (nuclear),  
 strong force; material incompressible; neutron degeneracy  
 Outside  $M_{\text{ch}} \rightarrow$  supersonic accretion
- $\rightarrow$  Shock wave and bounce



**Fig. 34.8.** Schematic picture of the velocity distribution in a collapsing stellar core originally of  $1.4M_{\odot}$  after numerical calculations (VAN RIPER, 1978). Note the two regimes: on the left  $|v_r|$  (in units of  $10^9 \text{ cm s}^{-1}$ ) increases in the outward direction. It corresponds to a (roughly) homologously collapsing part, while on the right  $|v_r|$  decreases with  $m$ . This corresponds to the free-fall regime

Energy released in a core collapse

R:  $R_{WD} (0.01 R_{\odot}) \rightarrow R_{NS} (10 \text{ km})$

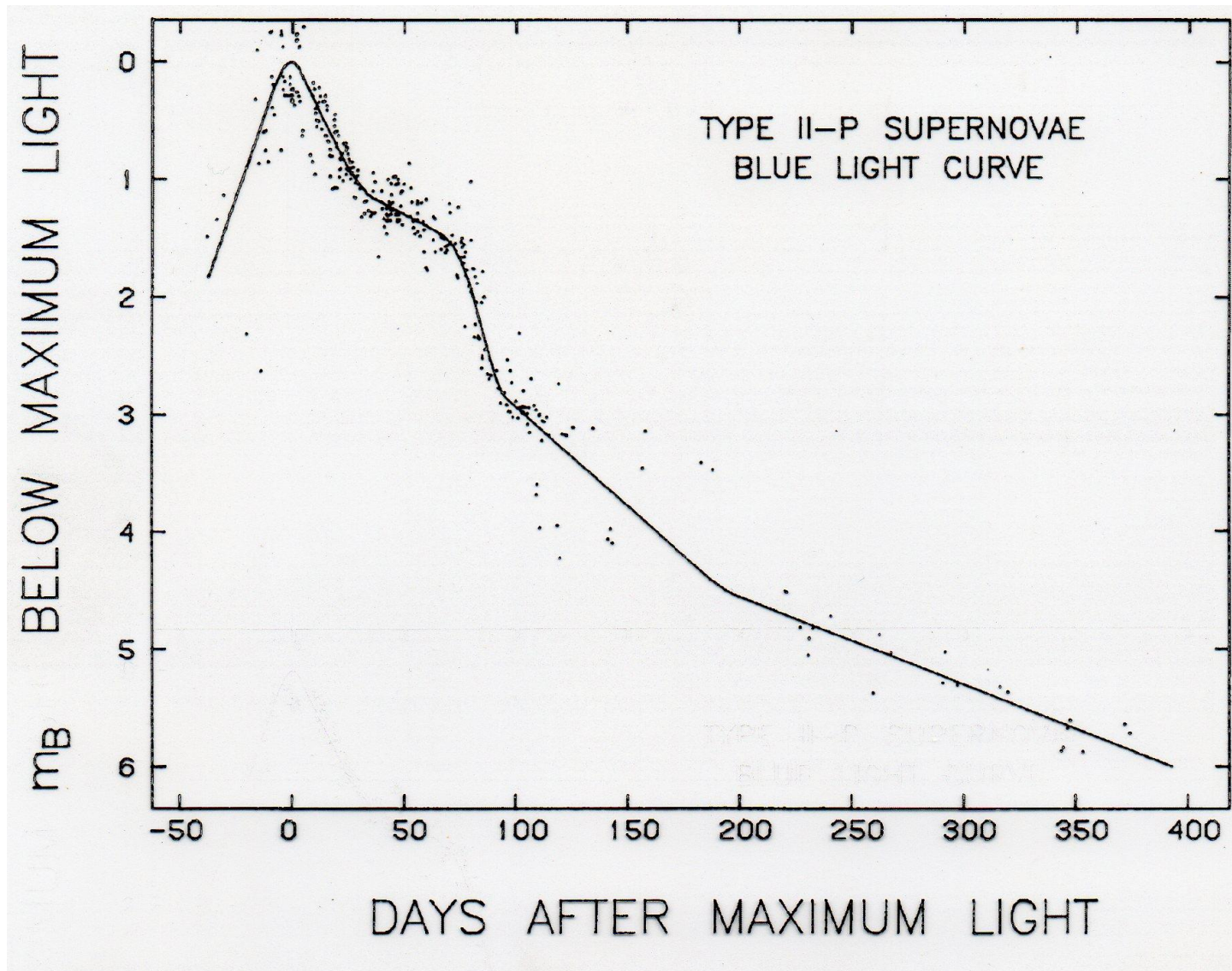
$$\Delta \bar{E}_{\text{grav}} \sim \frac{GM_{\odot}^2}{R_{NS}} \sim 3 \times 10^{53} \text{ ergs}$$

10% used up by nuclear processes

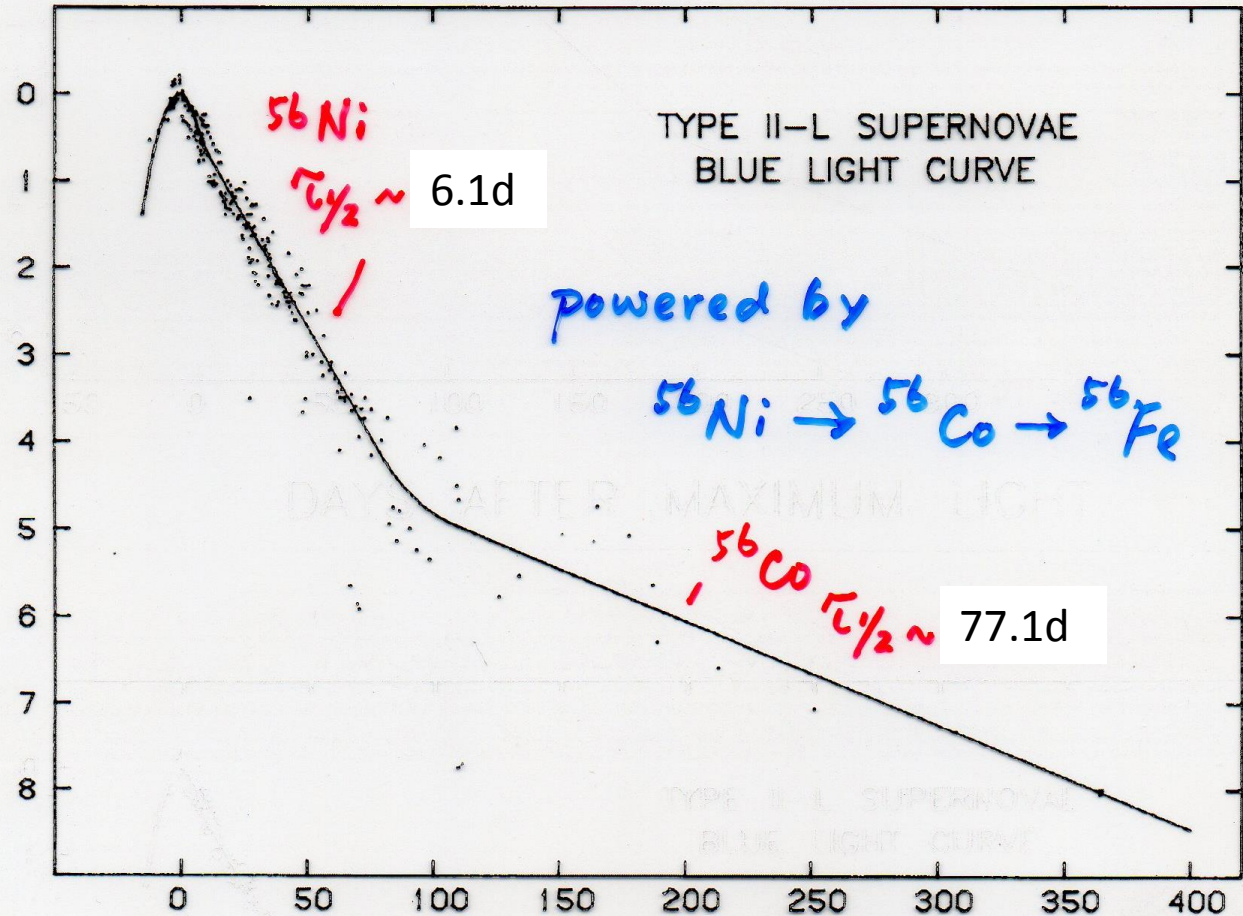
rest to radiation and ejecting material

↓

(luminosity & neutrinos)



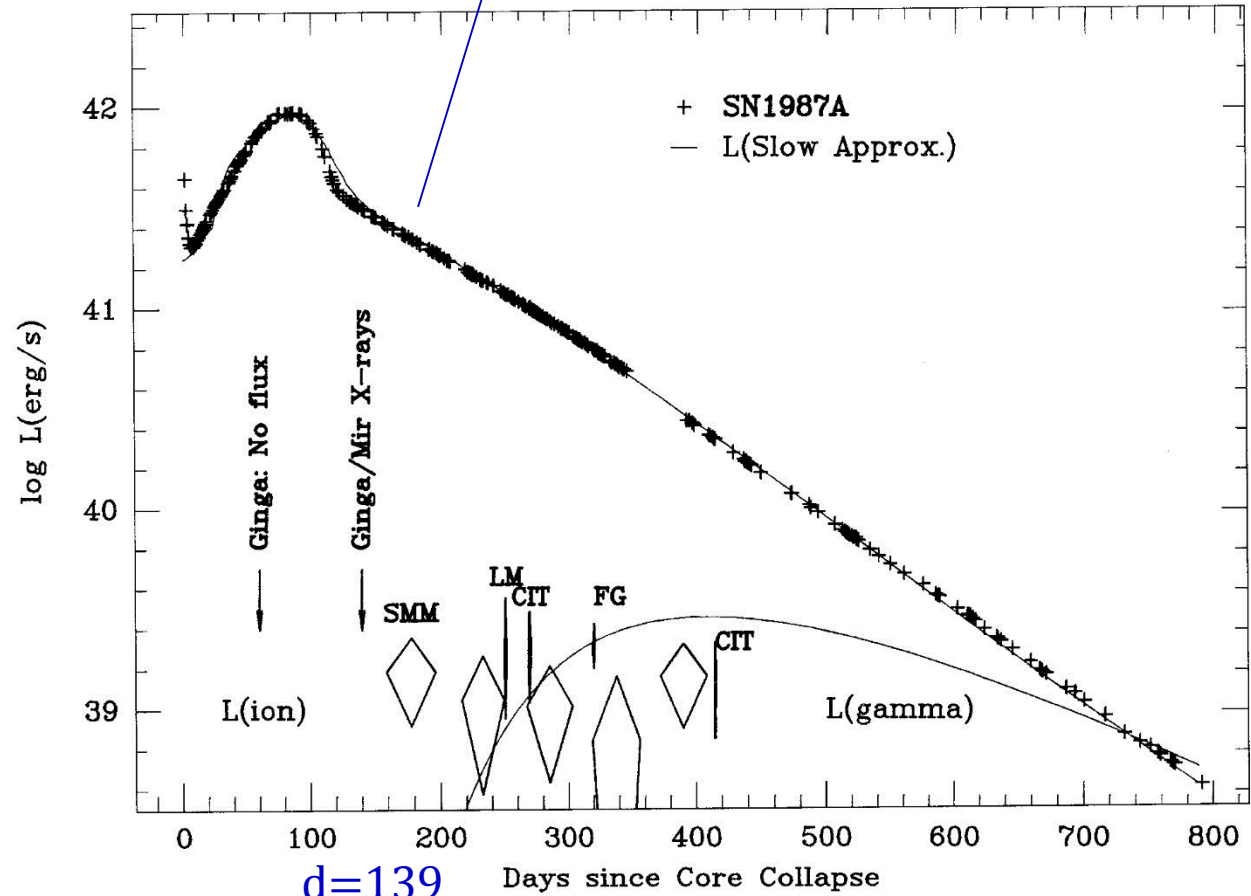
$m_B$  BELOW MAXIMUM LIGHT



DAYS AFTER MAXIMUM LIGHT

Doggert + Branch (1985)  
AJ, 90, 2303

# UVOIR light curve





Evidence of synthesis of heavy elements  
in 1987A

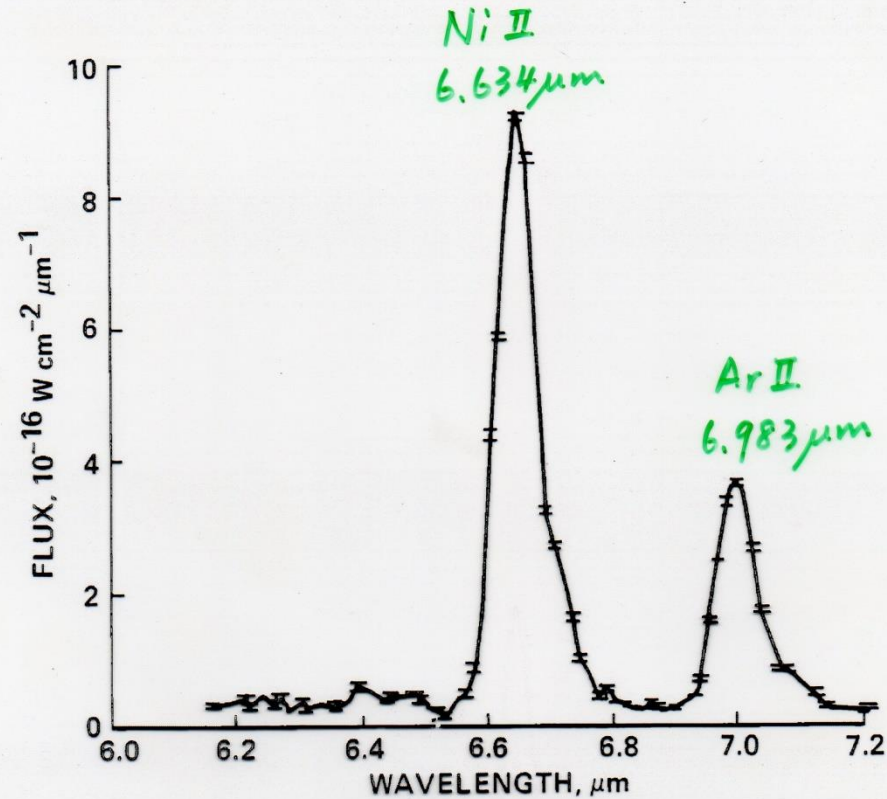


FIG. 1.—Spectrum of SN 1987A. The  $1 \sigma$  error bars are typically  $\pm 5 \times 10^{-18} \text{ W cm}^{-2} \mu\text{m}^{-1}$ . The flux calibration star was  $\alpha$  Bootis.

by Kuiper Airborne Observatory  
in 1988 April

Witteborn + 1989  
ApJL, 338, L9

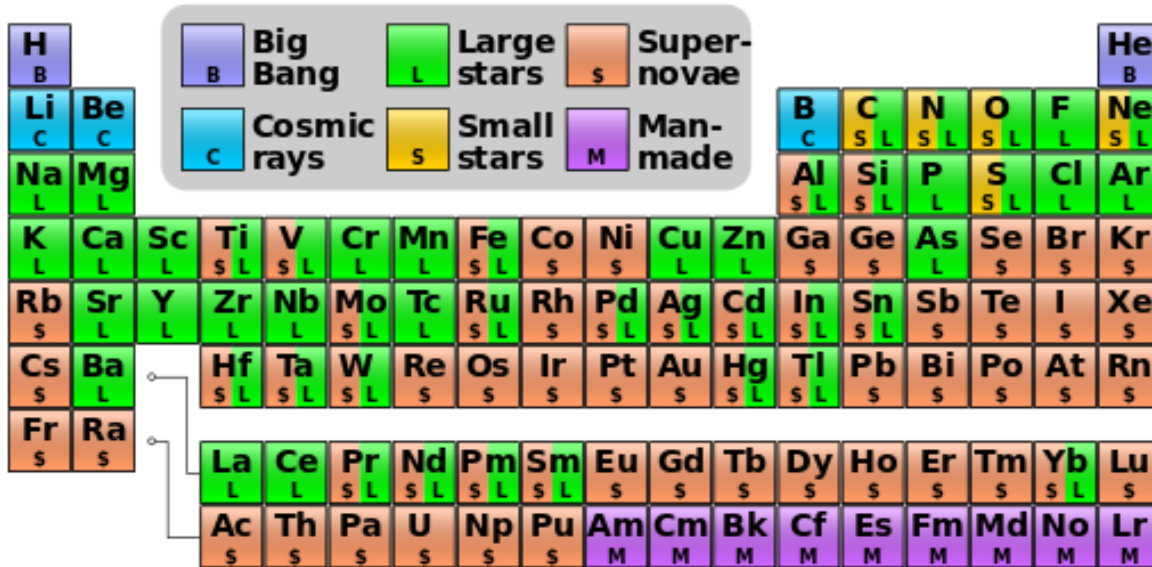
- ◆ During a type II SN explosion, the neutron star reaches  $T \approx 10^{11} \sim 10^{12}$  K, but cools down quickly by neutrinos, to  $T \approx 10^9$  K in a day,  $10^8$  K in 100 years.
- ◆ This is cold,  $kT \approx 10$  keV  
 cf. Fermi energy ( $\rho \approx 10^{14}$  g cm<sup>-3</sup>),  $\varepsilon_F \approx 1000$  MeV,  
 so  $T_{\text{neutron star}} \rightarrow 0$ , and all electrons, protons, and neutrons are at the lowest energy states.
- ◆ Neutron beta decay process,  $n \rightarrow p + e^- + \bar{\nu}_e$ , does not take place, because the resultant electron and neutrino are not energetic enough (energy difference between  $n$  and  $p$ )
- ◆ But inverse beta decay  $p + e^- \rightarrow n + \nu_e$  OK
- ➔ All neutrons

- So far thousands of SNe have been detected in external galaxies.
- In the Milky Way, a type Ia SN is expected every 36 years, and a type II SN is expected every 44 years. Then each century should see about 5 SNe.

### Notable Historical supernovae in the Milky Way

SN 1006	Lupus	Ia	-7.5 mag, brightest in history
SN 1054	Taurus	II	Chinese SN; Crab Nebula as the SNR
SN 1572	Cassiopeia	Ia	Tycho's Nova
SN 1604	Ophiuchus	Ia	Kepler's Star
SN 1680	Cassiopeia	I Ib	Not observed, Cas A as the SNR

# Solar System Abundances



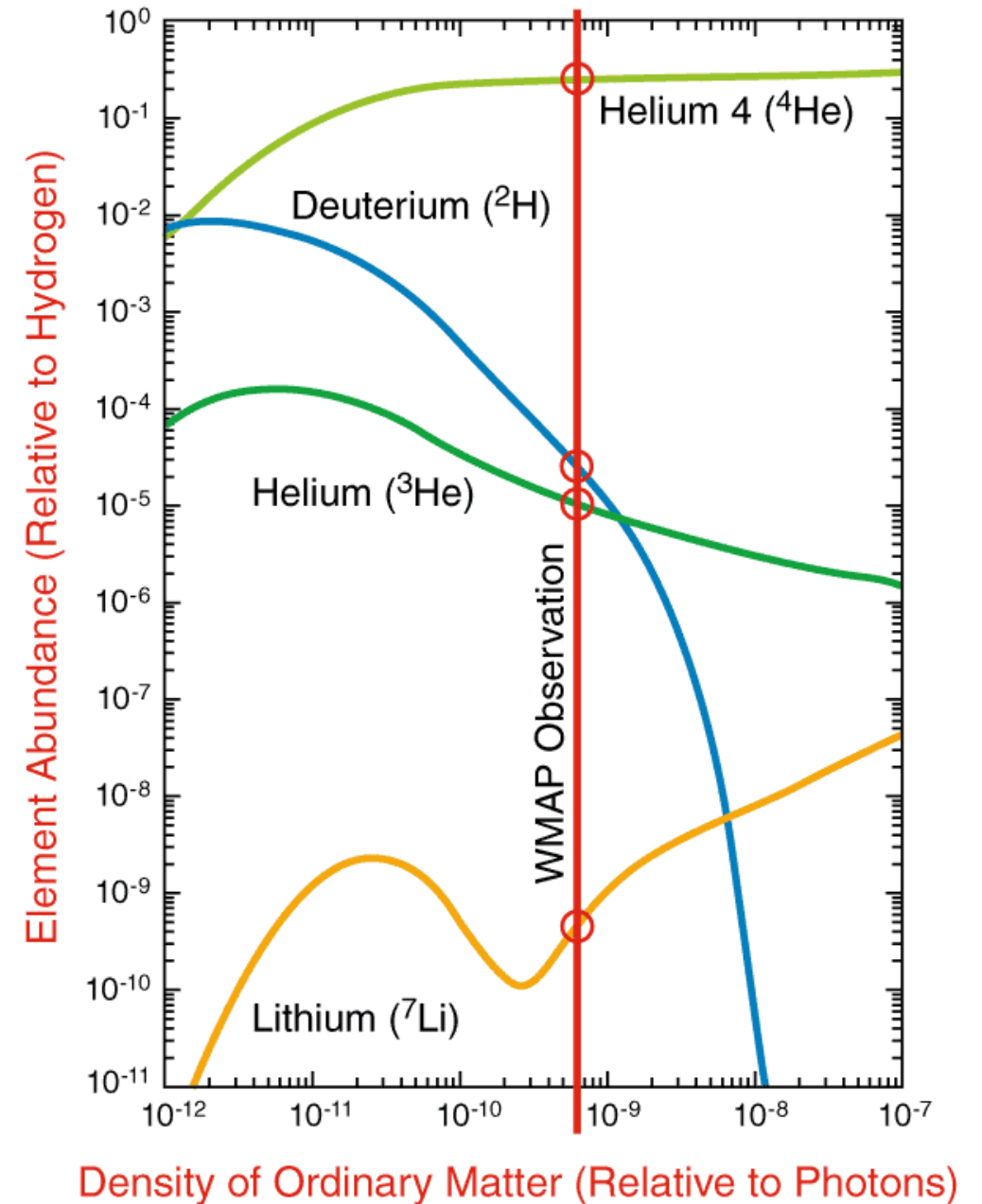
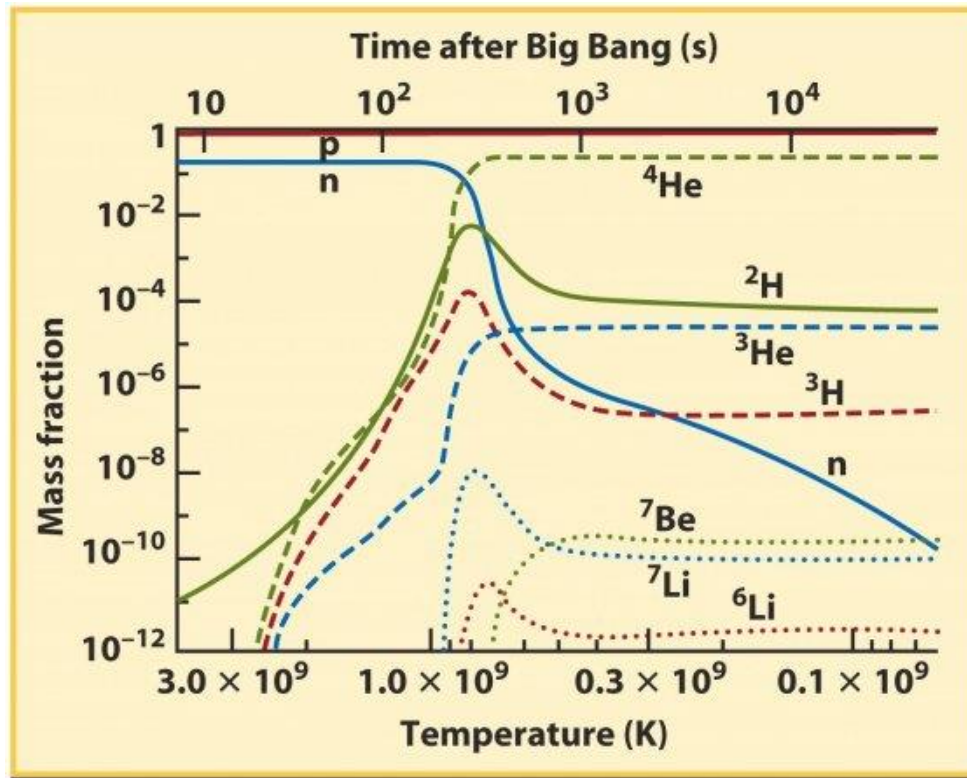
The 25 Most Abundant Nuclei

Rank	Z	Symbol	A	Nucleon Fraction	Source (process)
1	1	H	1	7.057e-01	Big Bang
2	2	He	4	2.752e-01	Big Bang, CNO, pp
3	8	O	16	9.592e-03	Helium
4	6	C	12	3.032e-03	Helium
5	10	Ne	20	1.548e-03	Carbon
6	26	Fe	56	1.169e-03	e-process
7	7	N	14	1.105e-03	CNO
8	14	Si	28	6.530e-04	Oxygen
9	12	Mg	24	5.130e-04	Carbon
10	16	S	32	3.958e-04	Oxygen
11	10	Ne	22	2.076e-04	Helium
12	12	Mg	26	7.892e-05	Carbon
13	18	Ar	36	7.740e-05	Silicon, Oxygen
14	26	Fe	54	7.158e-05	e-process, Silicon
15	12	Mg	25	6.893e-05	Carbon
16	20	Ca	40	5.990e-05	Silicon, Oxygen
17	13	Al	27	5.798e-05	Carbon
18	28	Ni	58	4.915e-05	Silicon, e-process
19	6	C	13	3.683e-05	CNO
20	2	He	3	3.453e-05	Big Bang, pp
21	14	Si	29	3.448e-05	Carbon, Neon
22	11	Na	23	3.339e-05	Carbon
23	26	Fe	57	2.840e-05	e-process
24	14	Si	30	2.345e-05	Carbon, Neon
25	1	H	2	2.317e-05	Big Bang

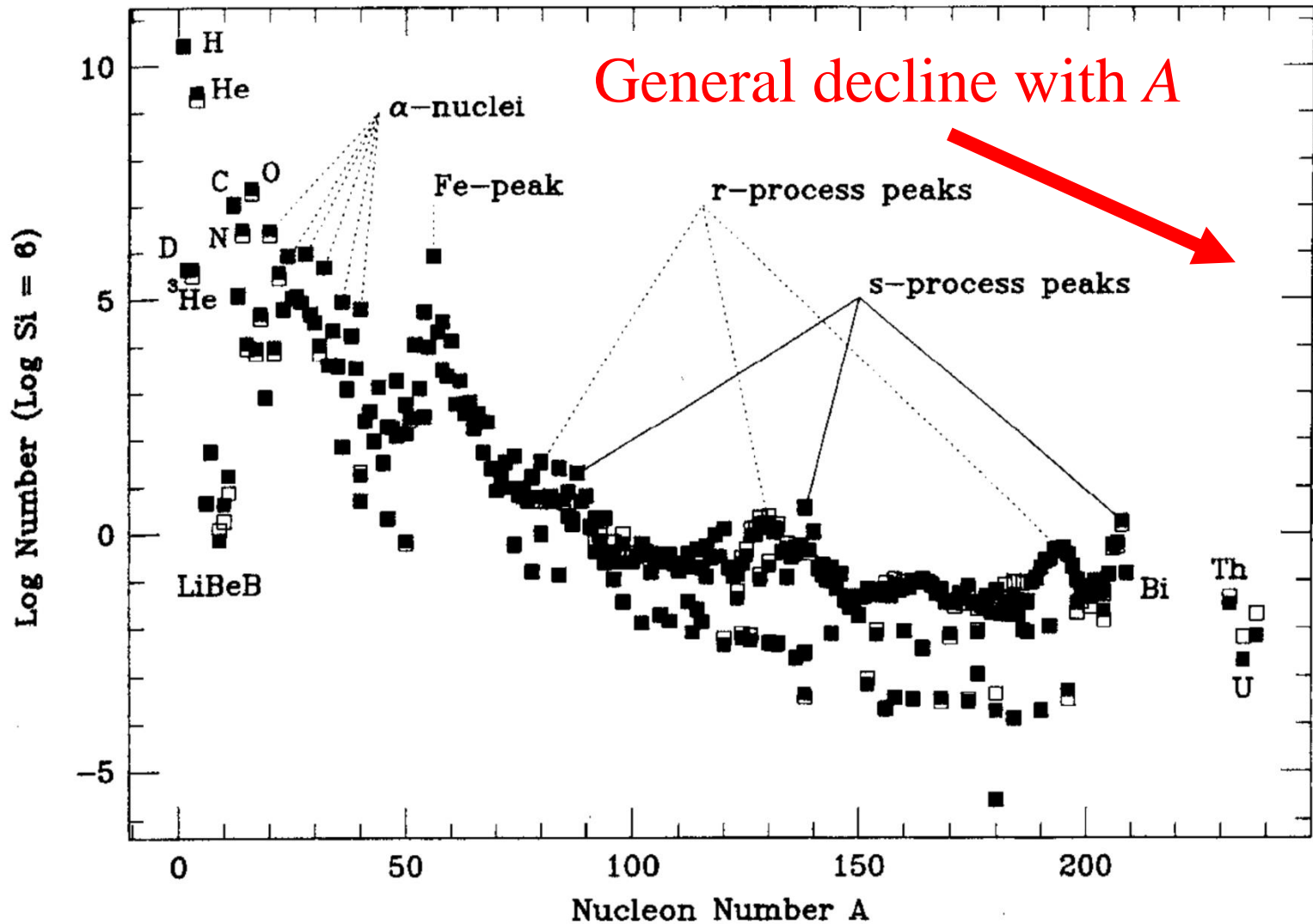
Prediction:

- ✓  $[^4\text{He}/\text{H}] \approx 0.25 \rightarrow$  obs OK
- ✓  $[\text{D}/\text{H}], [^4\text{He}/\text{H}], [^3\text{He}/\text{H}], [\text{Li}/\text{H}]$  density dependent  $\rightarrow$  obs all same densities

WMAP (CMB) obs  $\rightarrow$  consistent result



# Solar System Abundances



$Z \uparrow$ , Coulomb barrier  
 $\uparrow \uparrow$  for charged  
particle reactions  
 $\rightarrow$  elements produced  
by neutron capture

Different symbols from different compilations

Cosmic abundance and stellar/galaxy evolution (Burbidge, E. M., Burbidge, G. R., Fowler, W. A., & Hoyle, F. (1957))

Big Bang  $\rightarrow$  H:He=10:1

## Stellar Interior

$10^7$  K  $\rightarrow$  p-p, CNO (fusing proton, in a proton rich or neutron poor gas) (**p process**)

$10^8$  K  $\rightarrow$  triple-alpha to C  $\rightarrow$  continue to fuse  $\alpha$  particles  
 $\rightarrow$  mass number multiples of 4 by fusing ( **$\alpha$  process**)

$4 \times 10^9$  K  $\rightarrow$  nuclear equilibrium  $\rightarrow$  V, Cr, Mn and elements of the iron group (**e process**)

## Explosive events

Neutron capture rapidly (compared to the competing  $\beta$  decays)  $\rightarrow$  neutron-rich isotopes (**r process**)  
e, g., the radioactive elements  $^{235}\text{U}$ ,  $^{238}\text{U}$ , at the expense of the iron group

Neutron capture slowly (compared to the competing  $\beta$  decays)  $\rightarrow$  neutron-rich isotopes (**s process**)



# Valleys at $A=5$ to 15 (LiBeB) and $A \sim 45$ (Sc=scandium)

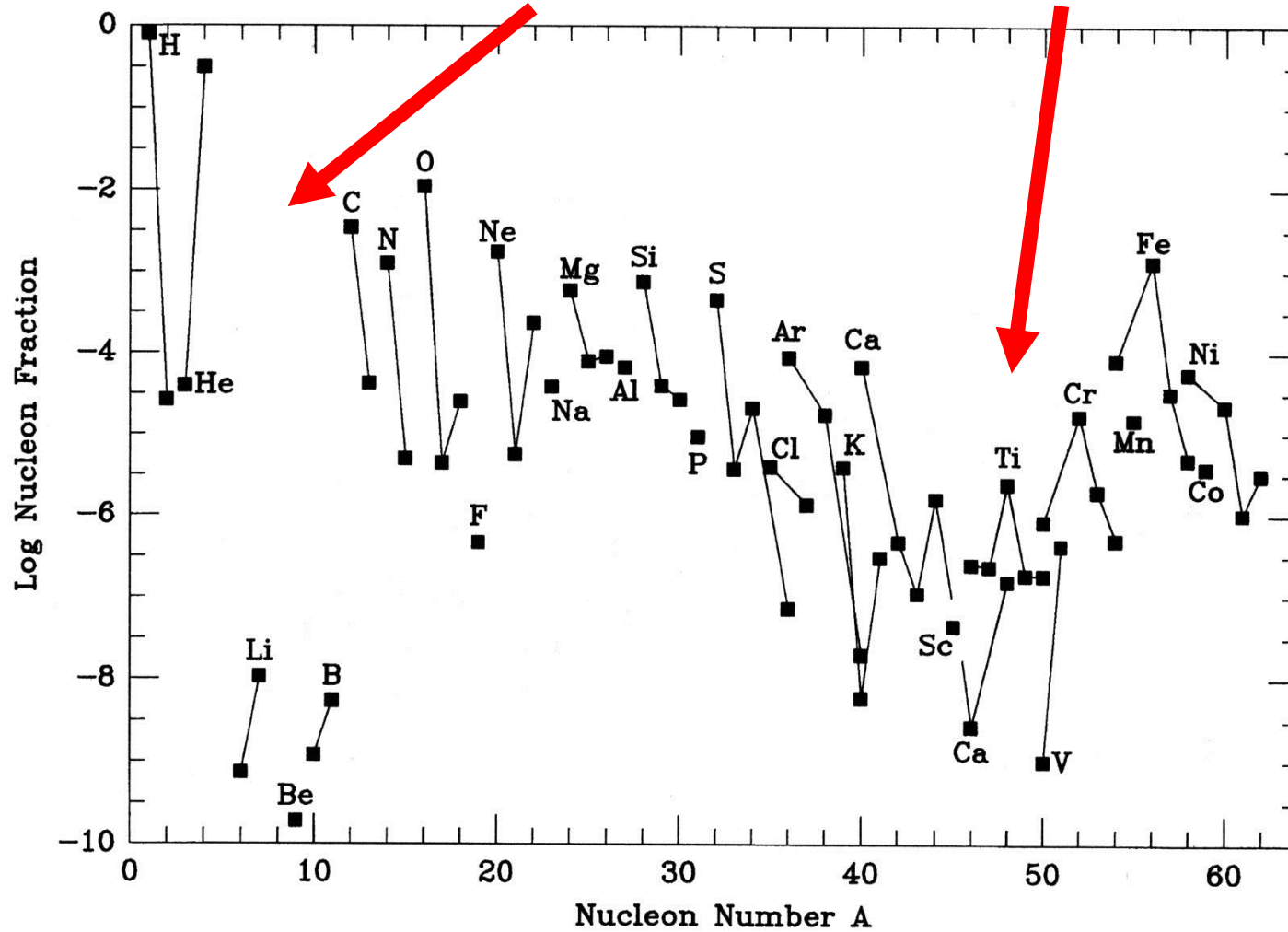


Fig. 2.2. Abundance ( $A = 1, 64$ )

Isotopes connected by lines.

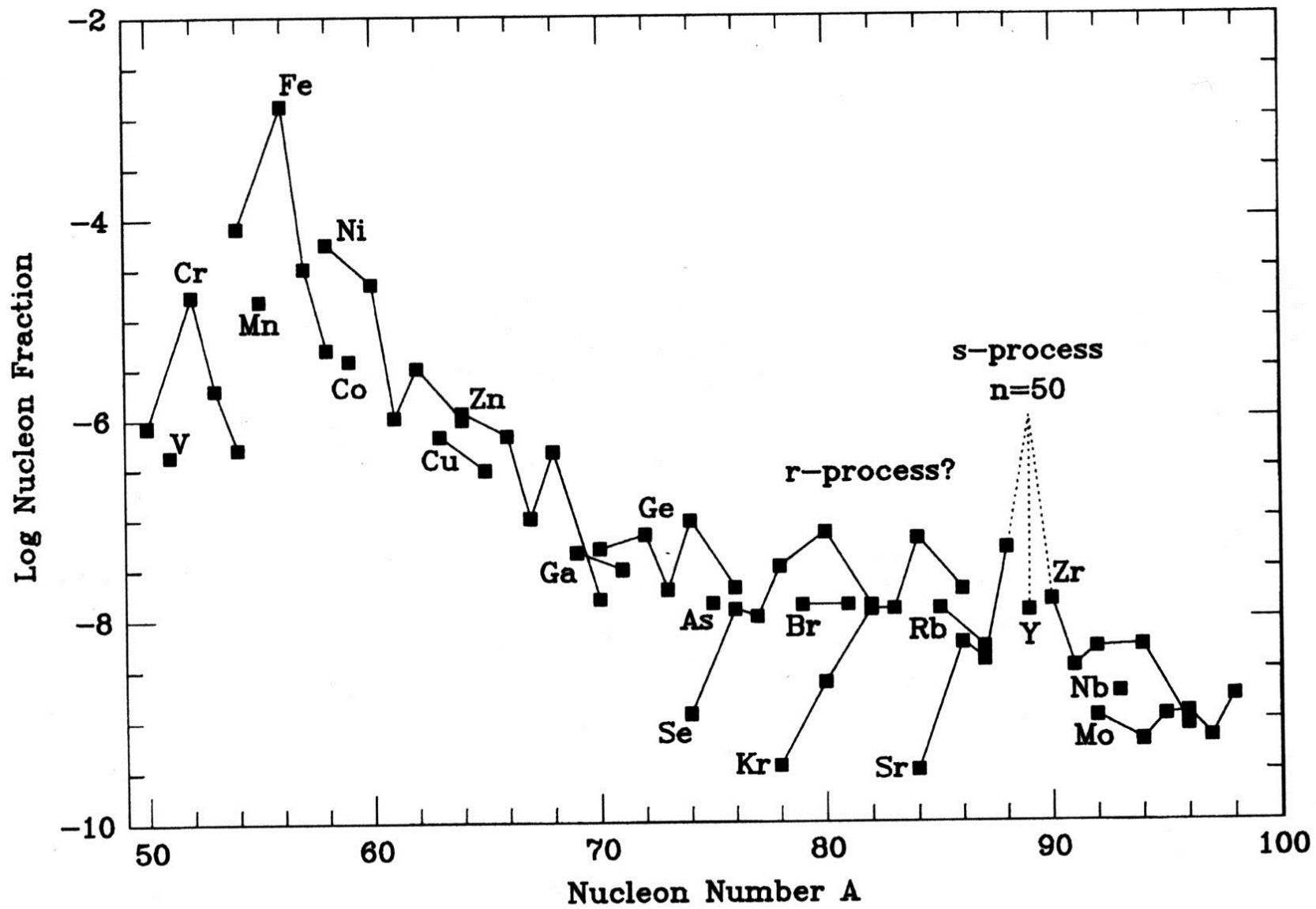


Fig. 2.3. Abundance ( $A = 50, 100$ )

- ◆ Other than H and He, the rest ('metals') is rare
  - ∴ penetration prob. between positively charged nuclei has an exponential dependence ( $Z_1 Z_2$ )
  - e.g.,  $0 + 0 \rightarrow$  64 times stronger than in  $H + H$
- ◆ Even  $A$  nuclei are favored; especially for even-even elements, i.e., even  $Z$  and even  $N$ .
- ◆  $Z = N \rightarrow$   **$\alpha$  particle nuclei** e.g.,  $^{12}\text{C}$ ,  $^{16}\text{O}$ ,  $^{20}\text{Ne}$ ,  $^{24}\text{Mg}$ ,  $^{28}\text{Si}$ ,  $^{32}\text{S}$ ,  $^{36}\text{Ar}$ ,  $^{40}\text{Ca}$
- ◆ First odd- $A$  element is  $^{25}\text{Mg}$ ; placed the 15<sup>th</sup>
- ◆ Among the top, only  $^{14}\text{N}$  is not even-even.

- ◆ Nuclei, like atoms, have a shell structure;  
“**magic numbers**” of protons are particularly tightly bound, e.g.,  ${}^4\text{He}$  ( $Z=N=2$ ),  ${}^{16}\text{O}$  ( $Z=N=8$ )
- ◆  ${}^{56}\text{Fe}$  not even-even; most tightly bound is  ${}^{56}\text{Ni}$ .  
SN I and II light curves provide evidence that  $\text{Ni} \rightarrow \text{Co} \rightarrow \text{Fe}$   
for  $A=56 \rightarrow$  Abundance peaks at  ${}^{56}\text{Fe}$
- ◆ For  $A > 60$ , via neutron capture
  - ✓ **r-process**: rapid relative to beta-decay
  - ✓ **s-process**: slow *nuclei already tightly bound  $\rightarrow$  small cross section for neutron capture (slow compare to beta decays)*  
(Burbidge, Burbidge, Fowler, & Hoyle; see Clayton)

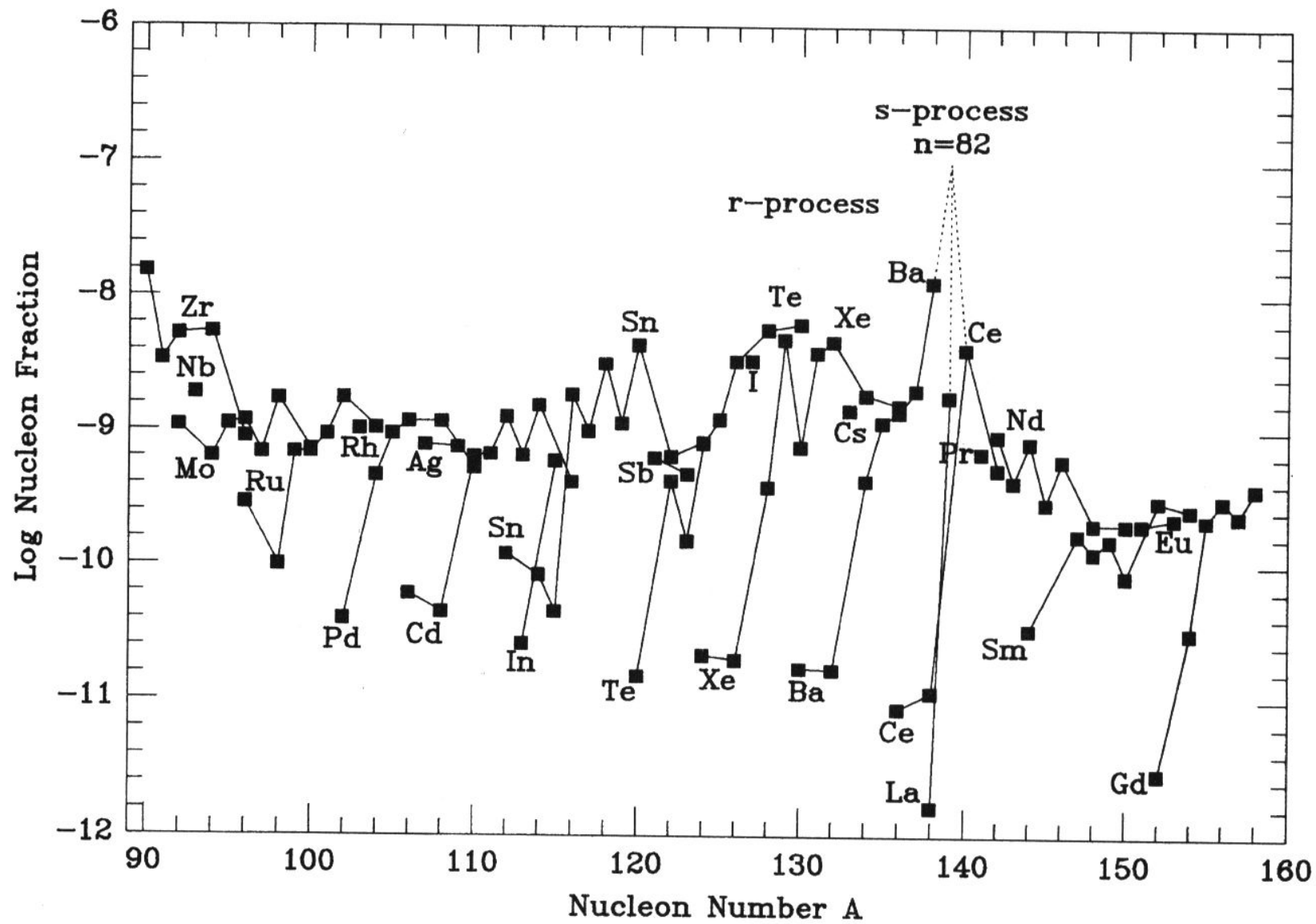


Fig. 2.4. Abundance ( $A = 90, 160$ )

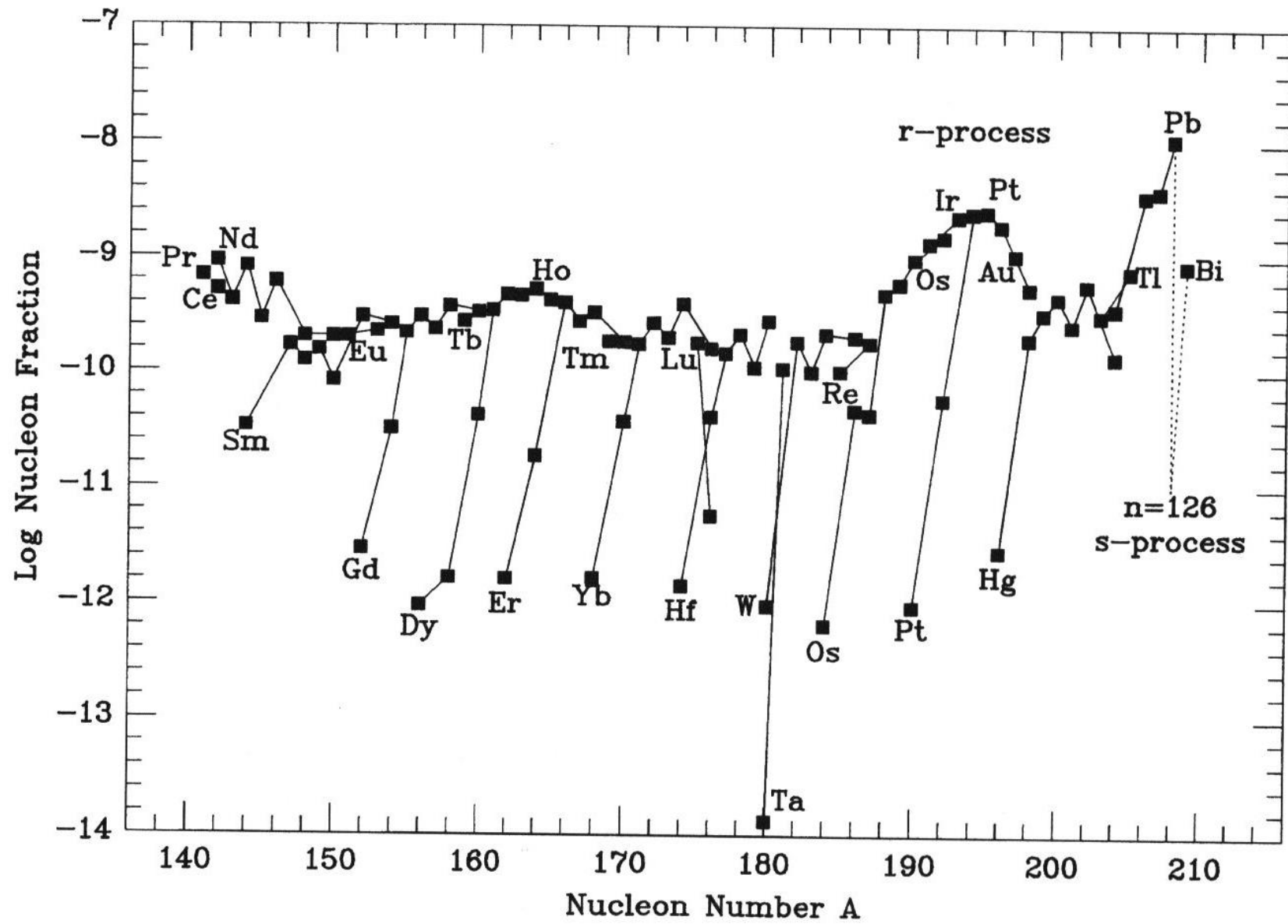
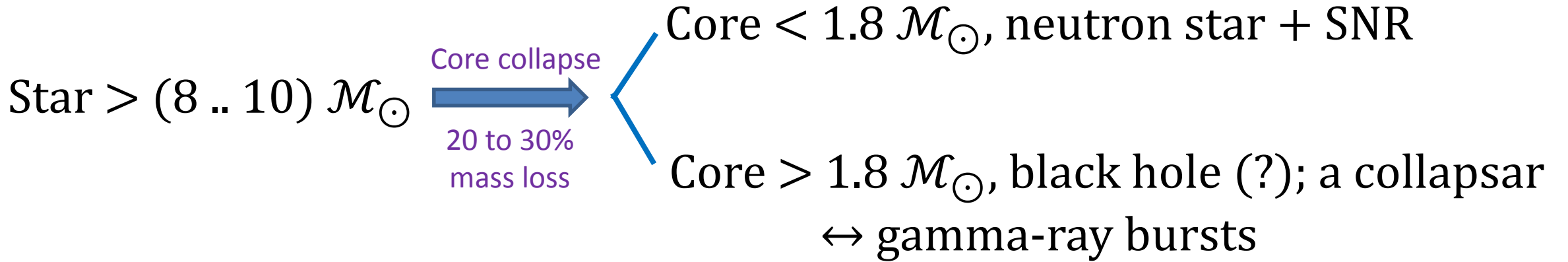
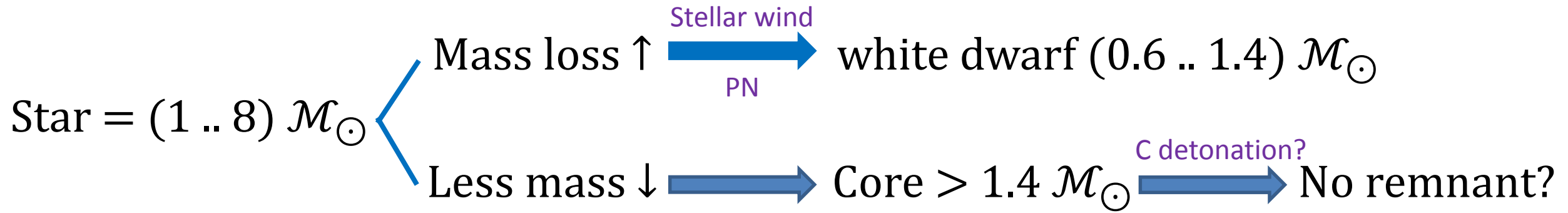


Fig. 2.5. Abundance ( $A = 140, 210$ )

# Stellar Evolutionary Path



# Black Holes predicted by General Relativity

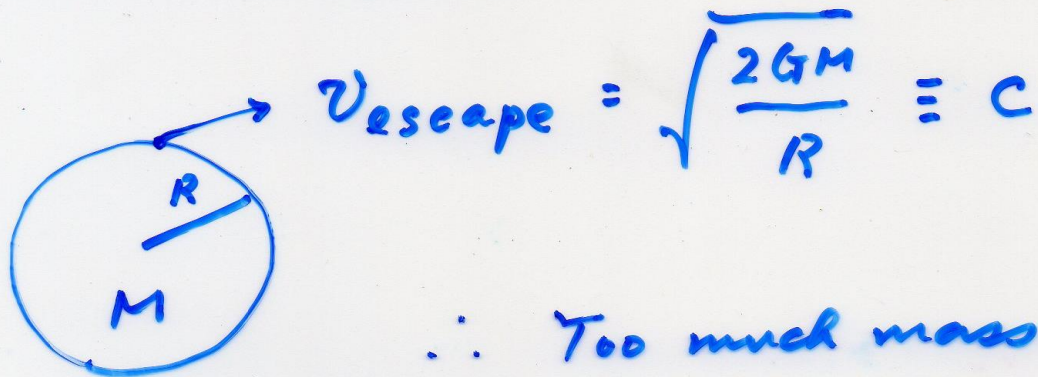
Spacetime near a mass is warped

Total solar eclipse



A full treatment of a BH requires GR. But for an electrically neutral, non-rotating BH, classical derivations give the same results as with the relativistic approach.





$\therefore$  Too much mass in a volume.

Schwarzschild radius

$$R_s = \frac{2GM}{c^2} \approx 3 \frac{M}{M_\odot} \text{ [km]}$$

$\therefore M \uparrow, R_{\text{BH}} \downarrow \downarrow$

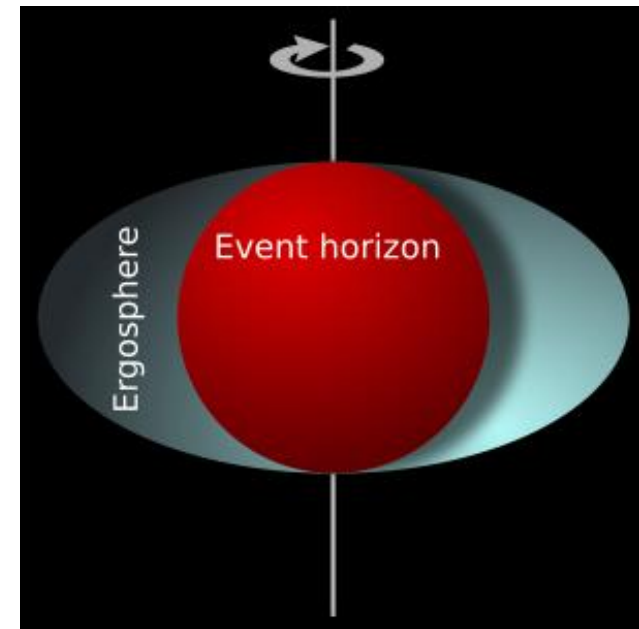
BH ( $M=10^8$  sun), average  
density  $\sim$  water

Surface of  $R_s$  = Event Horizon for  
uncharged, non-rotating BHs

Schwarzschild black hole

	Nonrotating ( $J = 0$ )	Rotating ( $J > 0$ )
Uncharged ( $Q = 0$ )	<a href="#"><u>Schwarzschild</u></a>	<a href="#"><u>Kerr</u></a>
Charged ( $Q \neq 0$ )	<a href="#"><u>Reissner-Nordström</u></a>	<a href="#"><u>Kerr-Newman</u></a>

General BH metric, with  $M$ ,  $J$  and  $Q =$  Kerr-Newman metric.



The two physical relevant surfaces of a Kerr black hole.

**Table 1.4**  
**Compact Objects in the Solar Neighborhood<sup>a</sup>**

Object	Mass Range of Parent Star ( $M_{\odot}$ )	Integrated Galactic Birth Rate ( $\text{yr}^{-1}$ )	Number Density ( $\text{pc}^{-3}$ )	$\frac{\rho}{\rho_T}$	$\langle d \rangle$ (pc)
White dwarfs	1–4	0.16	$1.5 \times 10^{-2}$	0.070	2.5
Neutron stars	4–10	0.021	$2.0 \times 10^{-3}$	0.020	4.9
Black holes	> 10	0.0085	$8.0 \times 10^{-4}$	0.22	6.7

<sup>a</sup>These values are obtained from Eqs. (1.3.17)–(1.3.21).

*Note:* Nearest known white dwarf: Sirius B, 2.7 pc. Nearest known neutron star: PSR 1929 + 10, 50 pc. Nearest known black hole candidate: Cygnus X-1, ~ 2 kpc.

Size of the Universe

13.7 billion yrs

$$R_{\text{observable}} \sim 137 \times 10^8 \times 10^{13} \text{ km}$$
$$\sim 1.4 \times 10^{23} \text{ km}$$

$$M_{\text{obs}} \sim 10^{11} M_{\odot} / \text{gal} \cdot 10^{12} \text{ gal.} \left( \begin{array}{l} + \text{ dark} \\ \text{matter} \\ + \text{ dark energy} \end{array} \right)$$

$$\sim 10^{23} M_{\odot}$$

$$\left( R_s \sim 3 \frac{M}{M_{\odot}} [\text{km}] \right)$$

$$R_{\text{obs}} \sim R_s$$

The whole Universe is a BH!

## Quark Stars / Strange Stars

hypothetical type of stars composed of quark matter or strange matter

currently 6 "flavors" of quarks

up, down, strange, charm,  
top, bottom

spin  $\frac{1}{2}$

When a neutron star is further compressed

neutrons  $\rightarrow$  break down to up and down

quarks  $\rightarrow$  break down

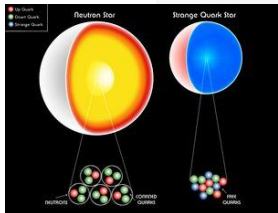
Strange quarks

dark matter candidates?

These highly mathematical & speculative

Some recent observations, e.g. in some SNe

$\rightarrow$  existence of quark stars?



## Magnetars

A neutron star w/ an extremely strong  $\vec{B}$   
(10<sup>11</sup> teslas or 10<sup>15</sup> gauss)

Earth/sun  $\sim 1$  G

Ap/Bp  $\sim 10^3$  G

WDs  $\sim 10^6$  G

NSs  $\sim 10^{12}$  G

collapse  $\rightarrow$  energy sources

(i)  $\dot{E}_{\text{grav}} \sim 0.2 M c^2 \sim 10^{53.8}$  ergs

(ii)  $\dot{E}_{\text{rot}} \sim \frac{1}{2} I \Omega^2 \sim 10^{52.7}$  ergs  $I_{45} \Omega_4^2$

$\vec{B}$  links the fast spinning core to the outlying envelopes

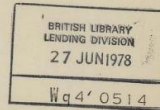
magnetic braking

$D \sim 20$  km; spin: several times/s

Time spans short,  $\lesssim 10^4$  yr  
 $\vec{B}$  decays

3  
THE  
INTERNAL CONSTITUTION  
OF THE STARS

21 BY 11  
A. S. EDDINGTON  
M.A., LL.D., D.Sc., F.R.S.  
*Plumian Professor of Astronomy in the  
University of Cambridge*



16  
CAMBRIDGE  
AT THE UNIVERSITY PRESS  
1926



DIFFUSE MATTER IN SPACE

393

To recall Kelvin's classic phrase, there are two clouds obscuring the theory of the structure and mechanism of the stars. One is the persistent discrepancy in absolute amount between the astronomical opacity and the results of calculations based either on theoretical or experimental physics. The other is the failure of our efforts to reduce the behaviour of subatomic energy to anything approaching a consistent scheme. Whether these clouds will be dissipated without a fundamental revision of some of the beliefs and conclusions which we have here regarded as securely established, cannot be foreseen. The history of scientific progress teaches us to keep an open mind. I do not think we need feel greatly concerned as to whether these rude attempts to explore the interior of a star have brought us to anything like the final truth. We have learned something of the varied interests involved. We have seen how closely the manifestations of the greatest bodies in the universe are linked to those of the smallest. The partial results already obtained encourage us to think that we are not far from the right track. Especially do we realise that the transcendently high temperature in the interior of a star is not an obstacle to investigation but rather tends to smooth away difficulties. At terrestrial temperatures matter has complex properties which are likely to prove most difficult to unravel; but it is reasonable to hope that in a not too distant future we shall be competent to understand so simple a thing as a star.

