

Stellar Evolution onto and off the Main Sequence

Stellar Structure

$$\frac{dP}{dM_r} = -\frac{GM_r}{4\pi r^4}$$

$$\frac{dr}{dM_r} = \frac{1}{4\pi r^2 \rho}$$

$$\frac{dT}{dM_r} = \begin{cases} -\frac{3k}{64\pi^3 ac} \left(\frac{1}{T^3}\right) \left(\frac{L_r}{r^4}\right), & \nabla_{\text{rad}} < \nabla_{\text{ad}} \\ -\frac{\nabla_{\text{ad}}}{4\pi} \left(\frac{T}{P}\right) \left(\frac{GM_r}{r^4}\right), & \nabla_{\text{rad}} > \nabla_{\text{ad}} \end{cases}$$

$$\frac{dL_r}{dM_r} = \epsilon(\rho, T, X)$$

Boundary Conditions

At stellar center, $M_r = 0$, $r = L_r = 0$

At stellar surface, $M_r = M$, $\rho = T = 0$

Given $M \Rightarrow L, T_c, P_c$

$$\begin{cases} \frac{dr}{dM} = \frac{1}{4\pi r^2 \rho} \\ \frac{dP}{dM} = -\frac{GM}{4\pi r^2} \\ \frac{dL}{dM} = \epsilon - T \frac{dS}{dT} \\ \frac{dT}{dM} = -\frac{3k}{4ac} \frac{L}{T^3} \frac{1}{16\pi^3 r^4} \quad (\text{rad.}) \\ = \frac{\gamma-1}{\gamma} \frac{dE_{\text{in}}}{dE_{\text{out}}} \quad (\text{conv.}) \end{cases}$$

Given M, μ
→ a stable structure, uniquely determined

Russell-Vogt theorem
⇒ a unique position in H-R diagram for a MS star

⇒ mass-radius & mass-lum. relations

$$\kappa \equiv \kappa(\rho, T, \mu)$$

$$\beta \equiv \beta(\rho, T, \mu)$$

$$\text{B.C.} \begin{cases} M(r=0) = 0; L(r=0) = 0 \\ \rho(r=R) = 0; T(r=R) \rightarrow T_{\text{eff}} \approx 0 \end{cases}$$

• Stellar evolution → μ changes

To compute structural changes with appropriate time steps

At a given time, with a given mass

→ set of $(r, T, P, \epsilon, L, \mu)$

→ plotted as evolutionary tracks on HRD
e.g. T_{eff}, L

Luminosity

$$\frac{L}{L_0} = \frac{L}{L_0} (M/M_0)$$

$$\frac{L}{L_0} \propto \begin{cases} 7^{1.75} (M/M_0)^3, & M \geq 7 M_0 \\ (M/M_0)^{4.8}, & 0.4 M_0 \leq M_0 \leq 7 M_0 \\ 0.4^{2.85} (M/M_0)^{1.9}, & M \leq 0.4 M_0 \end{cases}$$

Approximately, for $M \geq M_0$, $L \propto M^{2.5}$

Main sequence lifetime ($H \rightarrow He$)

$$\tau_{MS} \sim 0.1 \epsilon \frac{M}{L}$$

After this fraction stellar evolution becomes important, so star not in stable state

$$\approx 10^{10} \left(\frac{M}{M_0} \right) / (L/L_0) \text{ [yr]}$$

$$\approx 10^{10} (M/M_0)^{-2.5} \text{ [yr]}$$

Note: $M-L$, strong dependence on mass (index of 2.5) \leftarrow strong dep of ϵ on T for $M \geq M_0$

Radius

$$\frac{R}{R_0} = \frac{R}{R_0} (M/M_0)$$

$$R \propto M^{0.85} \quad M \leq M_0$$

$$R \propto M^{0.56} \quad M \geq M_0$$

different structure

Temperature

$$\frac{T_c}{T_{0,c}} = \frac{T_c}{T_{0,c}} (M/M_0)$$

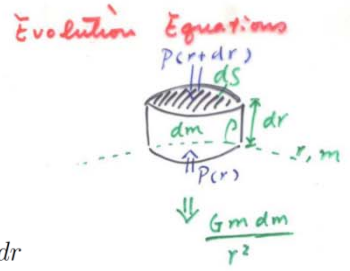
$$T_{0,c} \sim 1.44 \times 10^7 \text{ K}$$

- For $M \geq M_0$, T_c changes 2-3x
- For $M \leq M_0$, $T_c \uparrow$ as $M \uparrow$
- For $T_c \geq 1.4 \times 10^7 \text{ K}$, CNO cycle starts to dominate nuclear reaction process in the core of a star
- $T_c < 1.4 \times 10^7 \text{ K}$, pp chain dominates

$$\epsilon_{pp}(\rho, T) \sim \frac{2.4 \times 10^{-4} \rho X^2}{(T/10^9)^{3/2}} e^{-3.380/(T/10^9)^{1/3}} \text{ [erg s}^{-1}\text{g}^{-1}\text{]}$$

$$\epsilon_{CNO}(\rho, T) \sim \frac{4.4 \times 10^{-25} \rho X Z}{(T/10^9)^{3/2}} e^{-15.220/(T/10^9)^{1/3}} \text{ [erg s}^{-1}\text{g}^{-1}\text{]}$$

Evolution Equations



$$dm = \rho dr dS = \rho 4\pi r^2 dr$$

$$\frac{\partial^2 r}{\partial t^2} = \ddot{r} dm$$

$$= -\frac{Gm dm}{r^2} + P(r) dS - \frac{P(r+dr) dS}{P(r) + \frac{\partial P}{\partial r} \cdot dr}$$

The equation of motion is

$$\ddot{r} = -\frac{Gm}{r^2} - \frac{1}{\rho} \frac{\partial P}{\partial r} \quad \text{or} \quad \ddot{r} = \frac{Gm}{r^2} - 4\pi r^2 \frac{\partial P}{\partial m}$$

In case of hydrostatic equilibrium, i.e., $\ddot{r} \rightarrow 0$

$$\frac{dP}{dr} = -\rho \frac{Gm}{r^2} < 0$$

$X = 0.708, Y = 0.272, Z = 0.020$

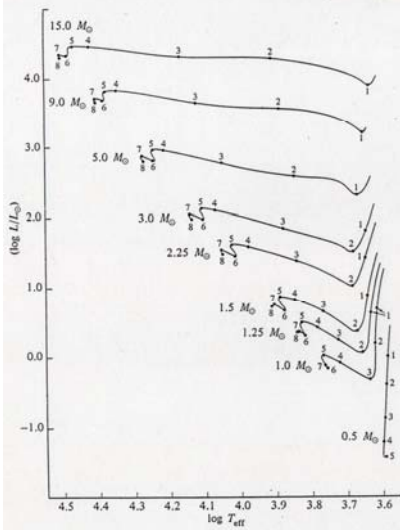


Fig. 7-3A Evolutionary Tracks of Pre-Main-Sequence Stars in the Hertzsprung-Russell Diagram. The mass, in units of the solar mass, is given at the left of each track. The small numbers correspond to the points in Table 7-4A, which give the time measured from the initial model for each mass. The units of T_{eff} are degrees Kelvin. [After I. Iben, Jr., 1965 (321).] *ApJ 141, 993*

Table 7-4A Time t in Years Measured from the Initial Model for Each Mass. The last point for each mass represents the main sequence.* [From I. Iben, Jr., 1965 (321).]

POINT IN FIG. 7-3A	MASS OF MODEL (UNITS OF THE SOLAR MASS)								
	15	9	5	3	2.25	1.5	1.25	1.0	0.5
	10^6	10^6	10^6	10^6	10^6	10^6	10^6	10^6	10^6
1	0.067	0.014	0.294	0.034	0.079	0.023	0.045	0.012	0.003
2	0.377	0.015	1.069	0.208	0.594	0.236	0.396	0.106	0.018
3	0.935	0.364	2.001	0.763	1.883	0.580	0.880	0.891	0.087
4	2.203	0.699	2.860	1.135	2.505	0.758	1.115	1.821	0.309
5	2.657	0.792	3.137	1.250	2.818	0.862	1.404	2.529	1.550
6	3.984	1.019	3.880	1.465	3.319	1.043	1.755	3.418	—
7	4.585	1.915	4.559	1.741	3.993	1.339	2.796	5.016	—
8	6.190	1.505	5.759	2.514	5.855	1.821	2.954	—	—

* Each entry must be multiplied by 10^6 as given at the head of each column.

Table 7-4B The Logarithm of the Time in Seconds, $\log t$, Measured From the Initial Models for Masses $1 M_{\odot}$ and $15 M_{\odot}$. [From data of I. Iben, Jr., 1965 (321).]

POINT IN FIG. 7-3A	MASS OF MODEL (UNITS OF THE SOLAR MASS)	
	15	1.0
1	10.33	12.57
2	11.07	13.52
3	11.47	14.45
4	11.84	14.76
5	11.92	14.90
6	12.10	15.03
7	12.16	15.20
8	12.29	—

$\log \tau \approx 14.5$
 $\log \tau \approx 15.0$

"Introduction to Stellar Atmospheres and Interiors"
 by Eva Novotny

1965ApJ...141..993I

STELLAR EVOLUTION. I. THE APPROACH TO THE MAIN SEQUENCE*

ICKO IBEN, JR.

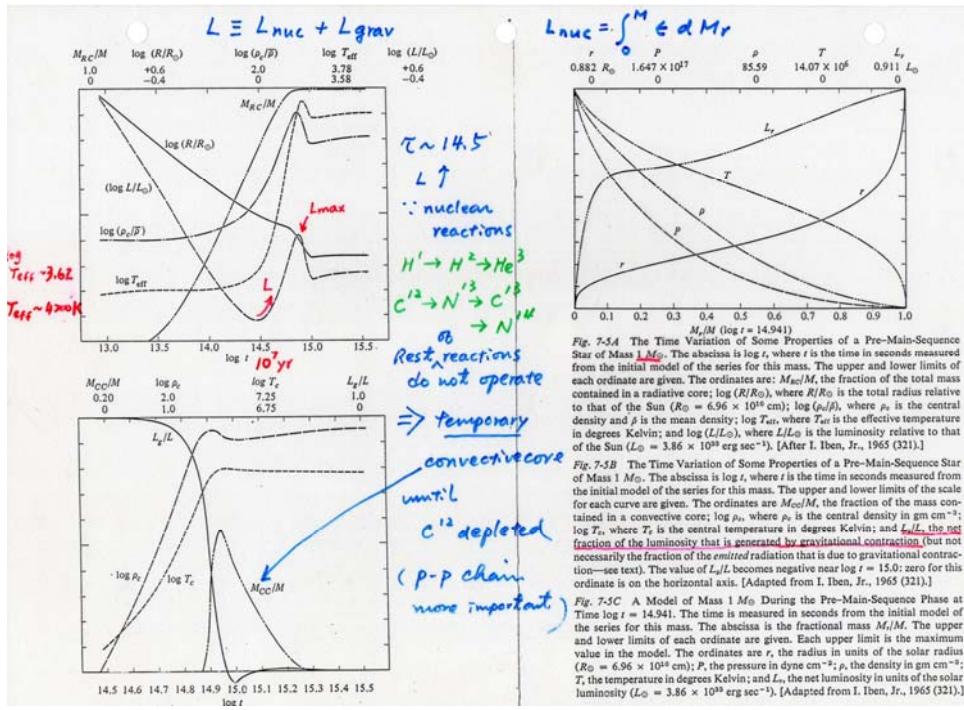
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ABSTRACT

The manner in which nuclear reactions replace gravitational contraction as the major source of stellar luminosity is investigated for model stars of population I composition in the mass range $0.5 < M/M_{\odot} < 15.0$. By following in detail the depletion of C^{12} from high initial values down to values corresponding to equilibrium with N^{14} in the C-N cycle, the approach to the main sequence in the Hertzsprung-Russell diagram and the time to reach the main sequence, for stars with $M \geq 1.25 M_{\odot}$, are found to differ significantly from data reported previously.

1 M_⊙



Pre-main Sequence Evolution of a 1 M_⊙ star

$\tau < 2 \times 10^{14} \text{ s}$ (i.e. $7 \times 10^6 \text{ yr}$)

$T_{eff} \sim \text{const} \sim 4200 \text{ K}$ $R \downarrow \Rightarrow L \downarrow$
 due to ionization of H & He
 a deep convective envelope

$\rho_c / \bar{\rho} \sim \text{const}$ (Hayashi track)

Star completely convective in the first 10^6 yr

L_g/L : energy from gravitational contraction

$\tau \sim 14.5$, $L \uparrow \Rightarrow$ nuclear reactions
 (10^7 yr)

(cont.)

~ 15

\Rightarrow expanding the core

$\rho_c \downarrow$, $T_c \downarrow$

But T_c not high enough

only ${}^1\text{H} \rightarrow {}^2\text{D} \rightarrow {}^3\text{He}$

${}^{12}\text{C} \rightarrow {}^{13}\text{N} \rightarrow {}^{13}\text{C} \rightarrow {}^{14}\text{N}$

The rest of PP chains or CNO cycle do not operate yet

Note $L_{\text{nuc}} + L_g \equiv L$
 $\tau \sim 15$, $L_g < 0$ (\therefore core expansion)

$\epsilon_{\text{nuc}} \uparrow \rightarrow \nabla T \uparrow$

\Rightarrow A temporary convective core ($\tau \sim 14.9$)
 until ${}^{12}\text{C}$ is depleted and
 PP chains become important

Eventually $\nabla T \downarrow$ at core, convective core \downarrow
 ($\tau \sim 15.3$)

$\tau \sim 15$, $L \rightarrow L_{\text{max}}$

Structure of star adjusts

\therefore Energy sources from gravitational
to nuclear processes

\Rightarrow ^{12}C main sequence ! Point 5

short lasting, depletion rapidly

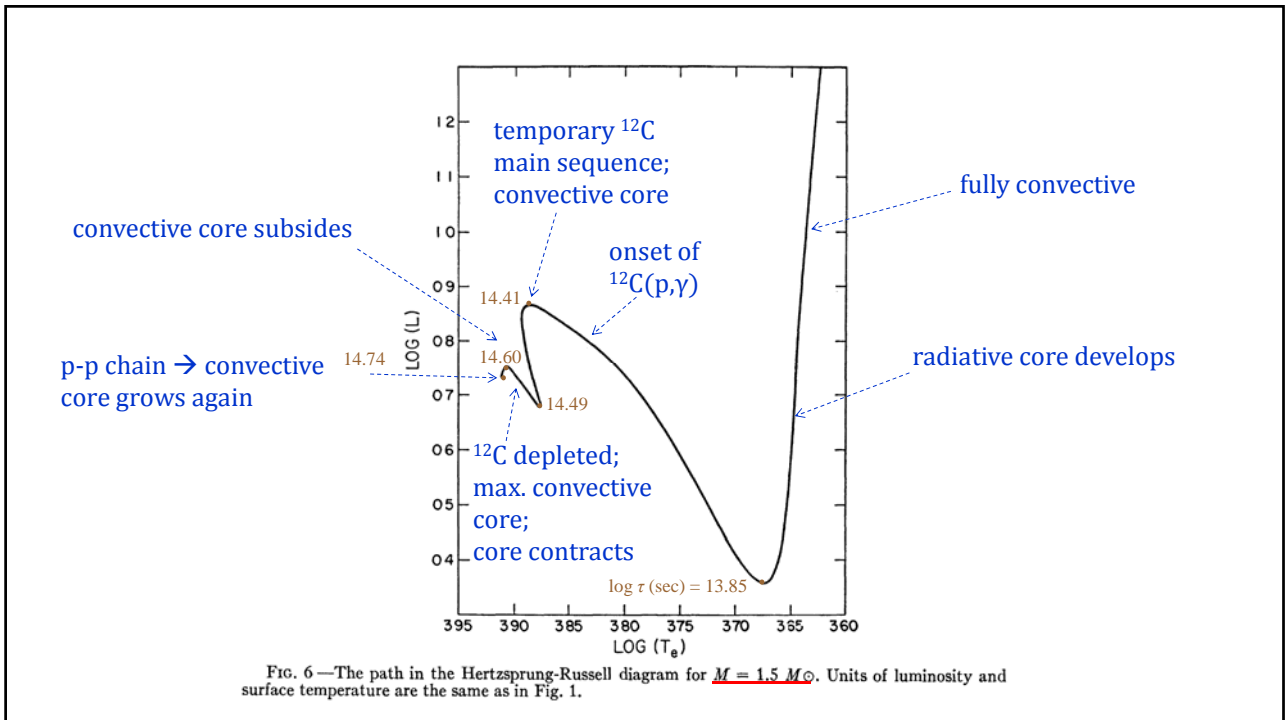
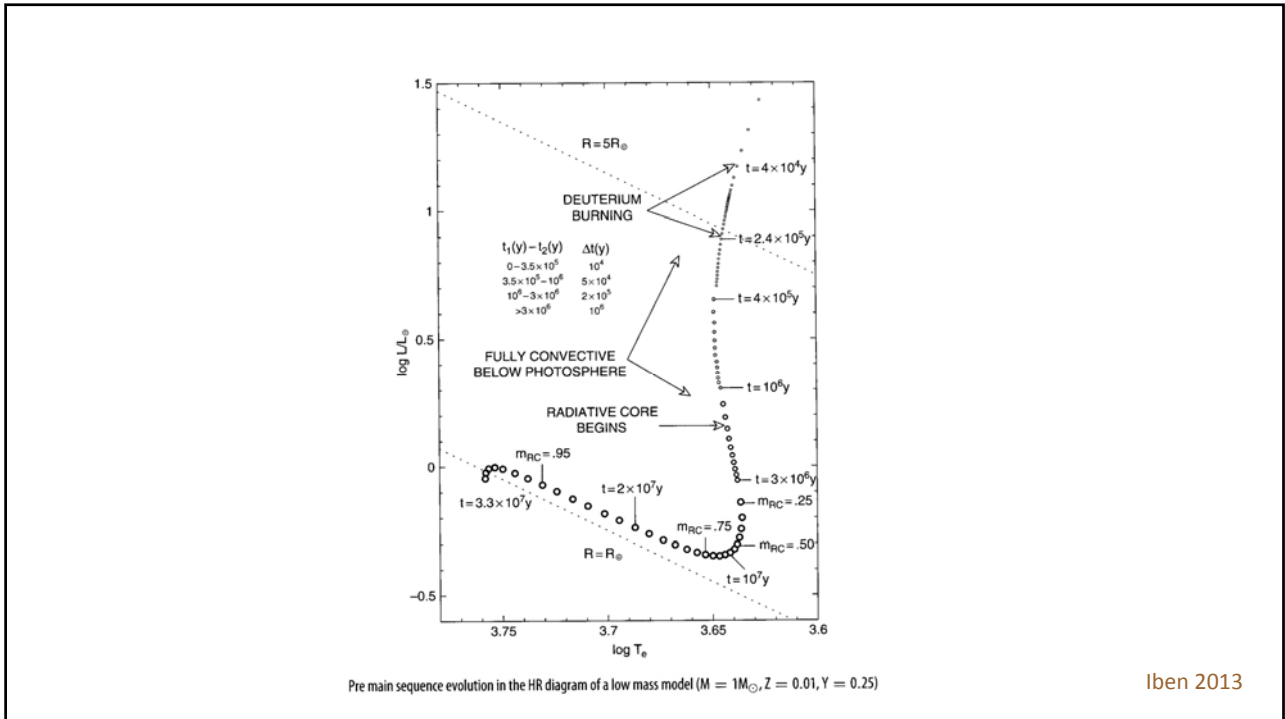
\rightarrow slight contraction

T_c, ρ_c high enough for PP reactions
to be the sole energy source.

For all stars $M \gtrsim M_{\odot} \Rightarrow$ convective core

^{12}C burning \rightarrow recedes

For stars $M \gtrsim 1.25 M_{\odot} \Rightarrow$ double luminosity
maxima and minima



For $0.5 M_{\odot}$ stars,

P_c, T_c not high enough for ^{12}C burning

For $M \lesssim 0.1 M_{\odot}$ (dependent on μ)

T_c not high enough for even H burning

\Rightarrow contraction continues

\rightarrow degenerate core

\Rightarrow black dwarfs ... nowadays called brown dwarfs

only the initial, nearly vertical descent

$\therefore T_c, P_c$ never high enough to ignite ^{12}C

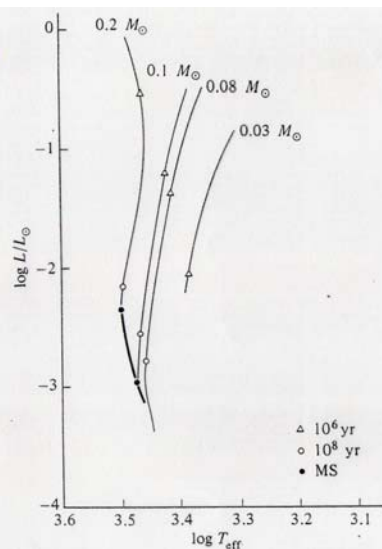
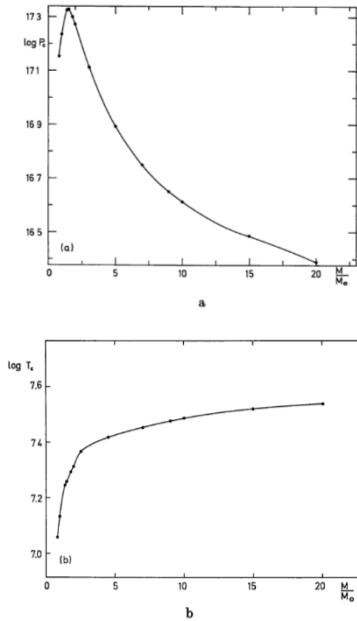


Fig. 7-3B Evolutionary Tracks of Pre-Main-Sequence Stars of Low Mass in the Hertzsprung-Russell Diagram. The masses, and the ages at two points on each track, are indicated. The heavy curve (MS) is the hydrogen-burning main sequence. The convective parameter is assumed to have the value $1/H = 1.0$. [Adapted from A. S. Grossman and H. C. Graboske, Jr., 1971 (400).]

Parameters at the stellar cores for non-rotating single MS stars



Figs. 3a and 3b. For non-rotating stars, the central pressure and central temperature variation with mass along the main-sequence

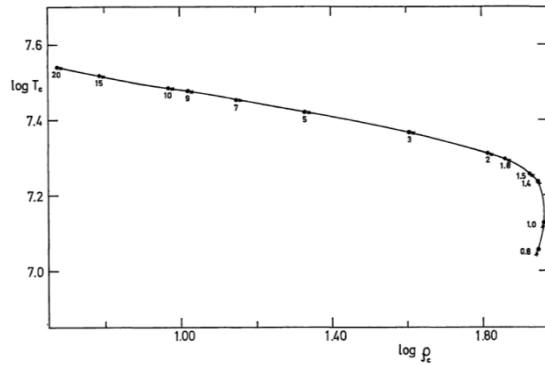


Fig. 4. The central temperature versus the central density for main-sequence stars. The curve is drawn through the data referring to non-rotating stars (dots). The crosses refer to critically, uniformly rotating stars. The Arabic numeral refers to the mass of the model

Sackman (1970) A&A, 8, 76

Effect of Stellar Rotation

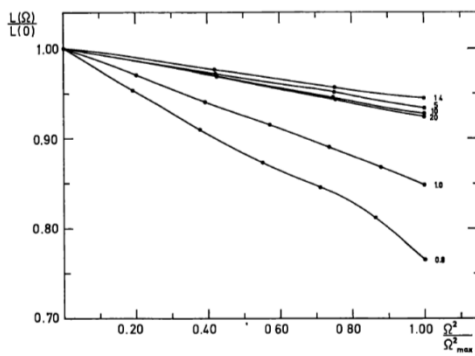


Fig. 1. The decrease of the luminosity with increasing rotation measured by Ω^2/Ω_{max}^2 , where Ω refers to the angular velocity of rotation and the subscript max to the critical case. The Arabic numeral refers to the mass of each sequence in solar units

$$\frac{\Omega}{\Omega_{crit}} \nearrow \Rightarrow L \searrow$$

More so for lower-mass stars

Rotation effectively lowers the stellar mass.

Sackman (1970) ApJ, 8, 76

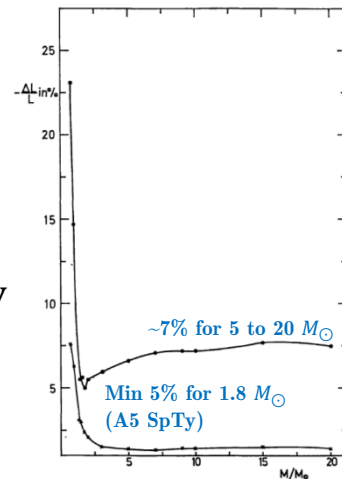


Fig. 5. The maximum change in the luminosity of a critically rotating star from that of a non-rotating star of the same mass, expressed in percent, against the mass of the main-sequence model. The dots refer to the actual results of the Stellar Interior models, while the crosses refer to the approximations made for Eq. (12)

Rotation → star cooler and fainter

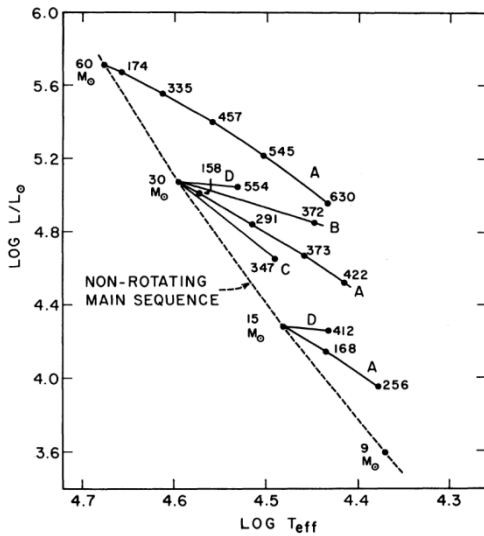


FIG. 2.—Theoretical H-R diagram showing model sequences of increasing angular momentum (solid curves). Numbers on curves give calculated velocities at the equator in km sec⁻¹. The distribution of angular momentum for each sequence is indicated by the letter A, B, C, or D.

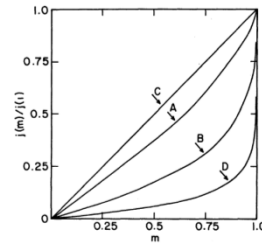


FIG. 1.—Angular momentum per unit mass, as a function of mass fraction interior to a given cylinder about the axis of rotation, for three assumed laws of differential rotation (Cases A, B, and C) and for a uniformly rotating model (Case D) of 30 M_⊙, log J = 52.73.

D: solid body rotation

Rotation law:
angular momentum distribution $j(m_w)$ as a function of, m_w , the mass fraction interior to the cylinder of radius w about the rotation axis.

Bodenheimer (1971) ApJ, 167, 153

Rotation → line broadening

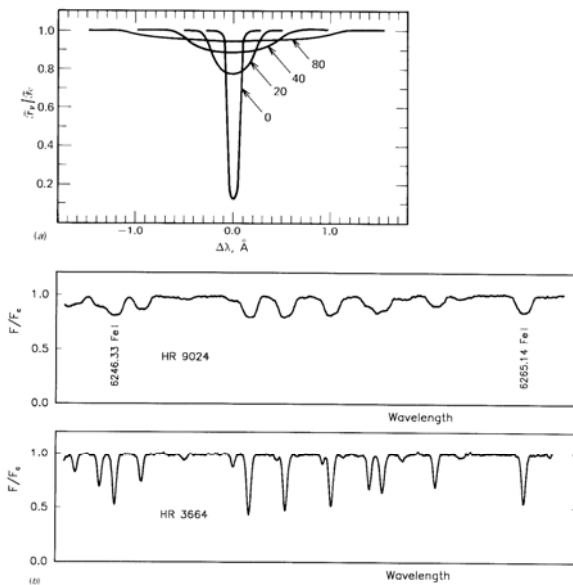


Fig. 17.7. (a) Computed profiles illustrate the broadening effect of rotation. The profiles are labeled with $v \sin i$. the wavelength is 4243 Å, and the line has an equivalent width of 100 mÅ. (b) These two early-G giants illustrate the Doppler broadening of the line profiles by rotation.

Gray p. 376

Rotation vs Spectral Type

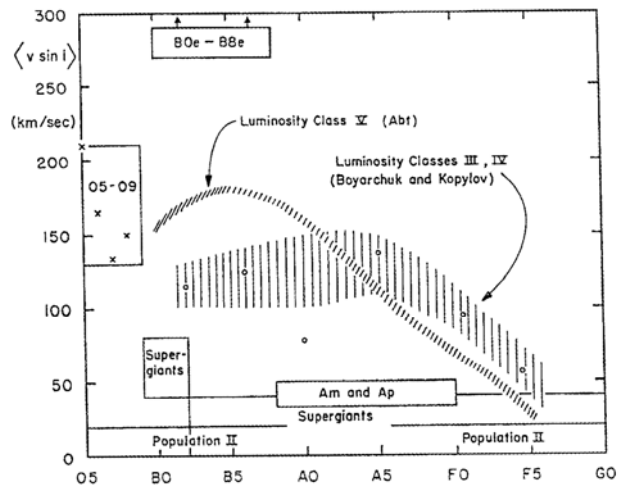
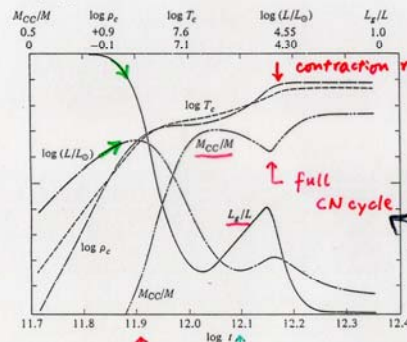


Fig. 3. Projected equatorial velocities, averaged over all possible inclinations, as a function of spectral type. On the main sequence (luminosity class V), early-type stars have rotational velocities that reach and even exceed 200 km/s; these velocities drop to a few km/s for late-type stars, such as the Sun (type G2) (Slettebak [20]; courtesy Gordon & Breach)

$15 M_{\odot}$

Fig. 7-6 The Time Variation of Some properties of a pre-main-sequence Star of Mass $15 M_{\odot}$. The abscissa is $\log t$, where t is the time in seconds measured from the initial model of the series for this mass. The upper and lower limits of each ordinate are given. The ordinates are M_{cc}/M , the fraction of the total mass contained in a convective core; $\log \rho_c$, where ρ_c is the central density in gm cm^{-3} ; $\log T_c$, where T_c is the central temperature in degrees Kelvin; $\log (L/L_{\odot})$, where L/L_{\odot} is the luminosity relative to the solar luminosity ($L_{\odot} = 3.86 \times 10^{33} \text{ erg sec}^{-1}$); and L_p/L , the net fraction of the luminosity that is generated by gravitational contraction (but not necessarily the fraction of the emitted radiation that is due to gravitational contraction—see text). [Adapted from I. Iben, Jr., 1965 (321).]



$\epsilon_{\text{grav}} \downarrow$ $\epsilon_{\text{nuc}} \uparrow$
 cf. L_g/L \downarrow
 $\Delta T \uparrow$
 \downarrow
 cf. M_{cc}/M convection

$^{12}\text{C} \rightarrow ^{13}\text{N}$
 $^1\text{H} \rightarrow ^3\text{He}$

$\epsilon_{\text{nuc}} \Rightarrow$ grav. contraction retarded temporarily
 ρ_c, T_c leveled out
 Total $L \downarrow$ ($\because L_g$)

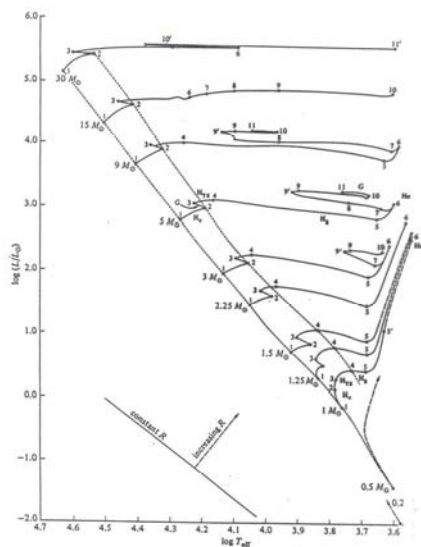
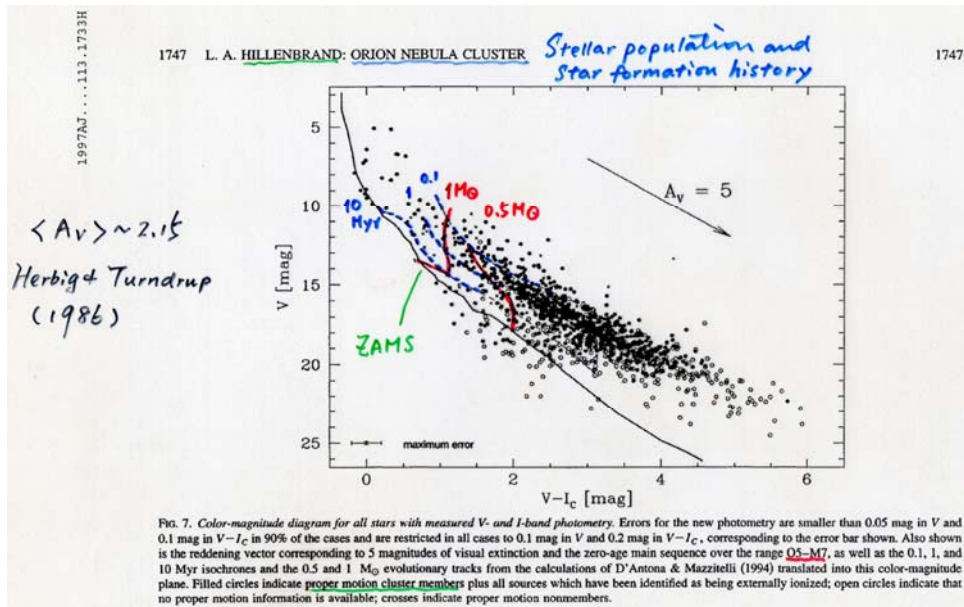


Table 7-7 Evolutionary Times. The times, expressed in years, refer to the points in Fig. 7-25.* [Adapted from I. Iben, Jr., 1967 (327).]

MASS (M_{\odot})	INTERVAL	1-2	2-3	3-4	4-5	5-6
30		4.80 (6)	8.64 (4)	~ 1.0 (4)		
15		1.010 (7)	2.270 (5)	7.55 (4)		
9		2.144 (7)	6.033 (5)	9.113 (4)	1.477 (5)	6.532 (4)
5		6.547 (7)	2.173 (6)	1.372 (4)	7.532 (5)	4.837 (5)
3		2.312 (8)	1.042 (7)	1.033 (7)	4.505 (6)	4.238 (6)
2.25		4.802 (8)	1.647 (7)	3.696 (7)	1.310 (7)	3.829 (7)
1.5		1.553 (9)	8.10 (7)	3.490 (8)	1.049 (8)	> 2 (8)
1.25		2.803 (9)	1.824 (8)	1.045 (9)	1.463 (8)	> 4 (8)
1.0		7 (9)	2 (9)	1.20 (9)	1.57 (8)	> 1 (9)

MASS (M_{\odot})	INTERVAL	6-7	7-8	8-9	9-10 ⁶	10 ⁶ -11 ⁶
30			53.1 (4)			1.3 (4)
15		7.17 (5)	6.20 (5)	1.9 (5)	3.5 (4)	
9		4.92 (5)	9.50 (4)	3.28 (6)	1.55 (5)	2.84 (4)
5		6.05 (6)	1.02 (6)	9.00 (6)	9.30 (5)	7.69 (4)
3		2.51 (7)		4.08 (7)	6.00 (6)	

* A number in parenthesis is the power of 10 by which an entry is to be multiplied.

Fig. 7-25 Evolutionary Tracks in the Hertzsprung-Russell Diagram. The mass of each star is given at the left of the track. The composition is $X = 0.708$, $Y = 0.272$, and $Z = 0.020$ for all masses except $30 M_{\odot}$, for which the composition is $X = 0.70$, $Y = 0.27$, $Z = 0.03$. Dashed portions of the curves are estimates. The letters along the tracks for 1 M_{\odot} and 5 M_{\odot} have the following significance: H_c = hydrogen-burning near the center; G = gravitational contraction of the entire star; H_{ts} = hydrogen-burning in a thick shell; H_t = hydrogen-burning in a thin shell; H_e = helium-burning near the center plus hydrogen-burning in a thin shell. The times required to reach the encircled points are given in Table 7-7. The dotted lines indicate the boundaries of the main sequence. The line (lower left) shows the slope of a path along which the radius remains constant. The track for 15 M_{\odot} does not turn back as do the other tracks because the semi-convective zone was treated as fully convective [see R. Stothers and C.-W. Chin, 1968 (377)]. [Adapted from I. Iben, Jr., 1967 (327). The track for 30 M_{\odot} is given by R. Stothers, 1966 (333).]

H_c : H core burning
 H_{ts} : H thick shell
 H_t : H thin shell

Evolution on the Main Sequence

Evolution on the Main Sequence (H core burning)

Hydrogen depletion core


$m_{\text{gas}} \uparrow \quad H \rightarrow He \Rightarrow \mu \uparrow \text{ increases}$
 $P_{\text{gas}} \propto \frac{1}{\mu}, P_{\text{gas}} \downarrow$

pressure not sufficient to support the core

\Rightarrow core contraction (v. slow)
 i.e. in equilibrium

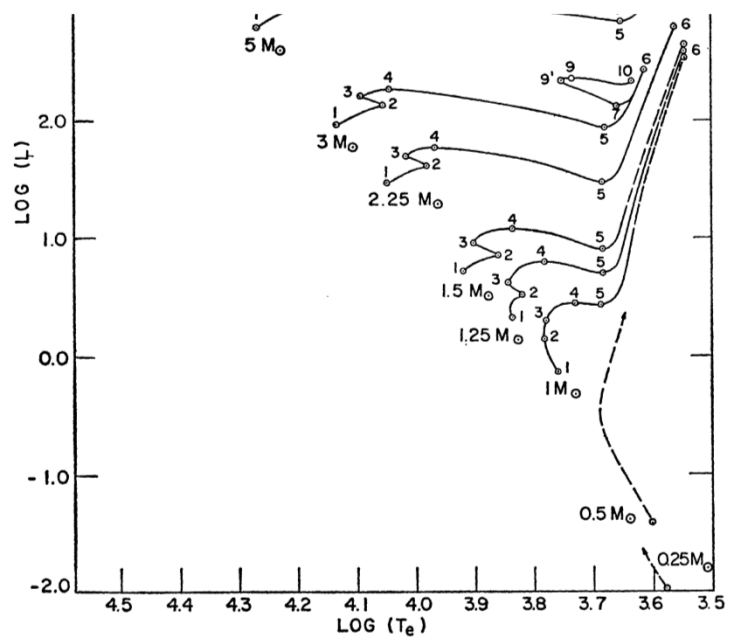
$\rho_c \uparrow, T_c \uparrow \quad \therefore$ even though $X_c \downarrow$
 but $\epsilon \uparrow \Rightarrow L \uparrow$ of HR diagram

\Rightarrow overlying layers expand
 L_{ν} in a thin shell $\Rightarrow T_{\text{eff}} \downarrow$



\rightarrow (Hydrogen shell burning)

- 1-2 main sequence
- 2-3 overall contraction
- 3-4 H thick shell burning
- 5-6 H thin shell burning
- 6-7 red giant
- 7-10 core He burning
- 8-9 envelope contraction



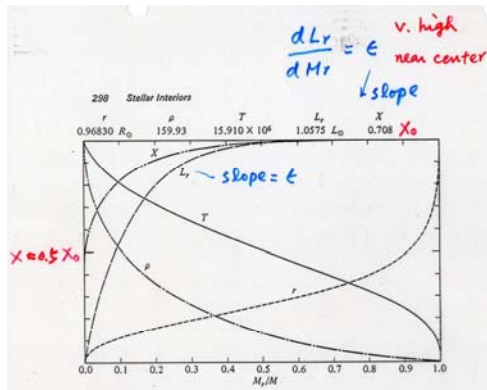


Fig. 7-10A A Model of Mass $1 M_{\odot}$ during the Main-Sequence Phase at Time $t = 4.269590 \times 10^8$ Years. Radius r , density ρ , temperature T , net luminosity L , and hydrogen abundance X are shown as functions of fractional mass M_r/M . The lower limit of the ordinate is zero for all variables. The upper limits, given in the figure, are the total radius R (units of $R_{\odot} = 6.96 \times 10^8$ cm), central density ρ_c (gm cm^{-3}), central temperature T_c in degrees Kelvin, total luminosity L (units of $L_{\odot} = 3.86 \times 10^{33}$ erg sec $^{-1}$), and initial hydrogen abundance $X = 0.708$. The central pressure (not shown) is 2.5186×10^{11} dyne cm $^{-2}$. The time t is measured from the initial model calculated for the pre-main-sequence phase (see Section 2). [Adapted from I. Iben, Jr., 1967 (326).]

Zen-age Main Sequence (ZAMS)
 \equiv homogeneous chemical composition
 Termination of MS
 \equiv end of H burning at core

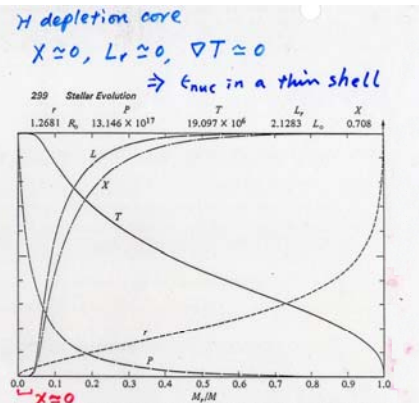


Fig. 7-10B A Model of Mass $1 M_{\odot}$ during the Main-Sequence Phase at Time $t = 9.20150 \times 10^8$ Years. Radius r , pressure P , temperature T , net luminosity L , and hydrogen abundance X are shown as functions of fractional mass M_r/M . The lower limit of the ordinate is zero for all variables. The upper limits, given in the figure, are $1.2681 R_{\odot}$ (with $R_{\odot} = 6.96 \times 10^8$ cm; however, the total radius is $1.3526 R_{\odot}$), central pressure P_c (dyne cm $^{-2}$), central temperature T_c in degrees Kelvin, total luminosity L (units of $L_{\odot} = 3.86 \times 10^{33}$ erg sec $^{-1}$), and initial hydrogen abundance $X = 0.708$. The central density (not shown) is 1026.0 gm cm $^{-3}$. The time t is measured from the initial model calculated for the pre-main-sequence phase (see Section 2). [Adapted from I. Iben, Jr., 1967 (326).]

As τ goes on, $M_{core}^{H=0} \uparrow$, until $M_{core} \sim 0.1 M_{\odot}$
 Schönberg-Chandrasekhar limit (1942) ApJ 95, 16
 maximum fraction of total mass maintainable within an isothermal core

1 M_{\odot} Stars on the Main Sequence

$4 H \rightarrow He \quad n \downarrow \rightarrow P \downarrow \rightarrow$ core contracts (slowly)

$$\rho_{pp} \sim \rho X^2 T_c^4$$

H depletion $X \downarrow$ but $T \uparrow, \rho \uparrow$

$$\therefore \rho \uparrow \Rightarrow L \uparrow$$

(Faint distant sun dilemma)

\rightarrow envelope $R \uparrow$

H depleted core $L_r = 0$, but ϵ_{nuc} in a thick shell around the core

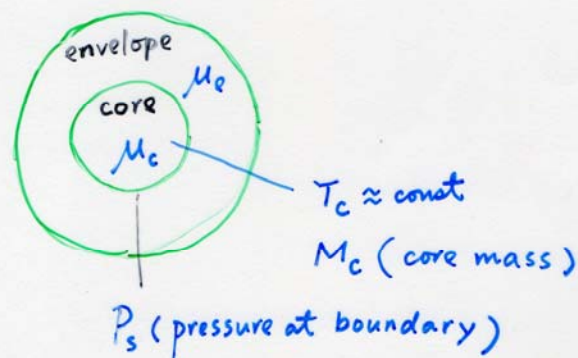
$$L_{\text{TS}} > L_{\text{core}}(\text{MS})$$

$$\Rightarrow L \uparrow \rightarrow R \uparrow \Rightarrow T_{\text{eff}} \downarrow$$

Point 4 \equiv End of MS

Star \rightarrow subgiant branch

until M_{SC} is reached
($\sim 8-10\%$)



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ON THE EVOLUTION OF THE MAIN-SEQUENCE STARS

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ABSTRACT

The evolution of the stars on the main sequence consequent to the gradual burning of the hydrogen in the central regions is examined. It is shown that, as a result of the decrease in the hydrogen content in these regions, the convective core (normally present in a star) eventually gives place to an isothermal core. It is further shown that there is an upper limit (~ 10 per cent) to the fraction of the total mass of hydrogen which can thus be exhausted. Some further remarks on what is to be expected beyond this point are also made.

$$\frac{M_c}{M} \approx 0.37 \left(\frac{\mu_e}{\mu_c} \right)^2 \left(\sim 10-15\% \text{ in reality} \right)$$

Take ionized H in env; pure He in core $\mu = 1.34$
 $\mu = 0.61$
 $M_c \sim 8-9\% M$ $\mu_c \sim 2 \mu_e$

Beech 1988

(Point 4, 5) shortly after the MS

ϵ_{nuc} in a thin shell

$L_r \uparrow \uparrow$ between 13% - 20%

core experiences gravitational contraction $L_g > 0$
 $\Rightarrow \nabla T$

$\rho_c \rightarrow 1.5 \times 10^4 \text{ g cm}^{-3}$, P_{deg} important ($= 0.46 P_{\text{total}}$)

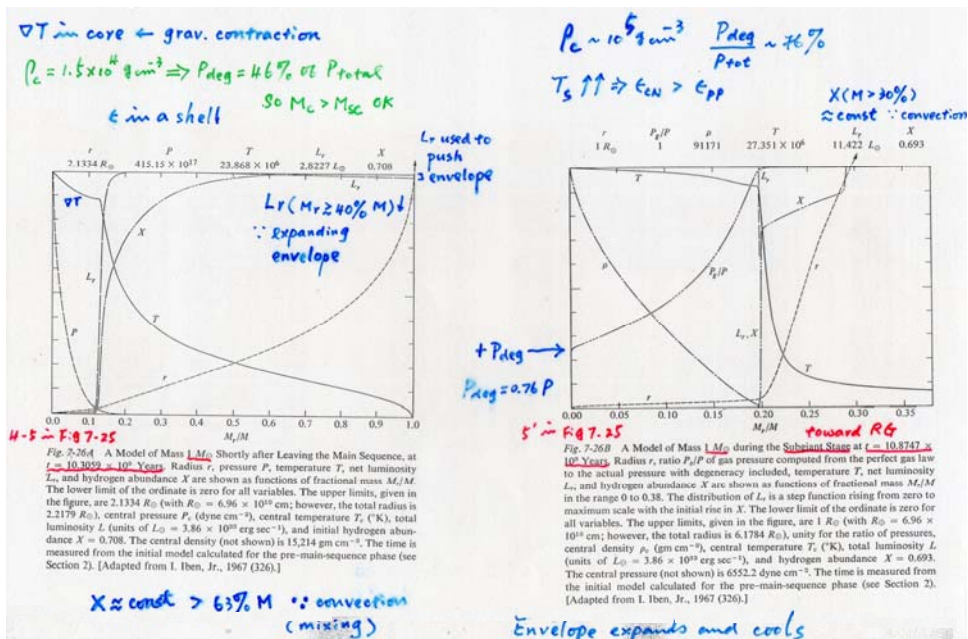
convection beyond 63% M \rightarrow mixing $\rightarrow X \approx \text{const}$

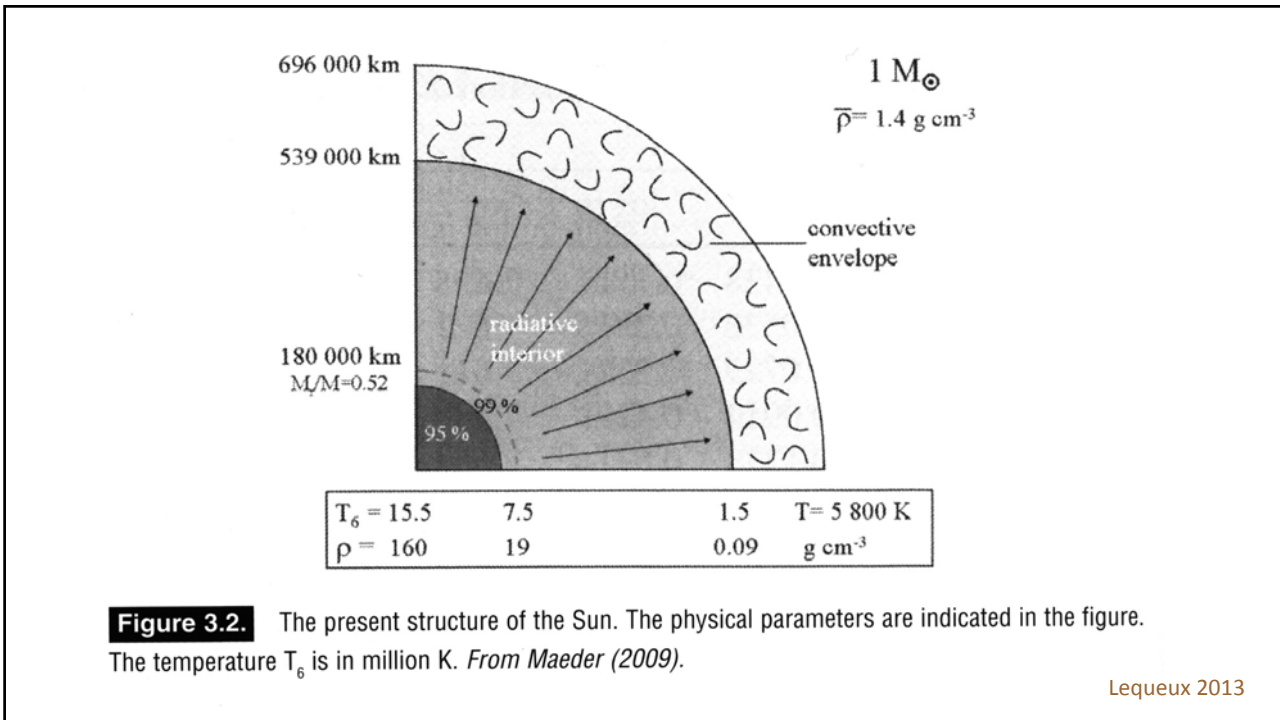
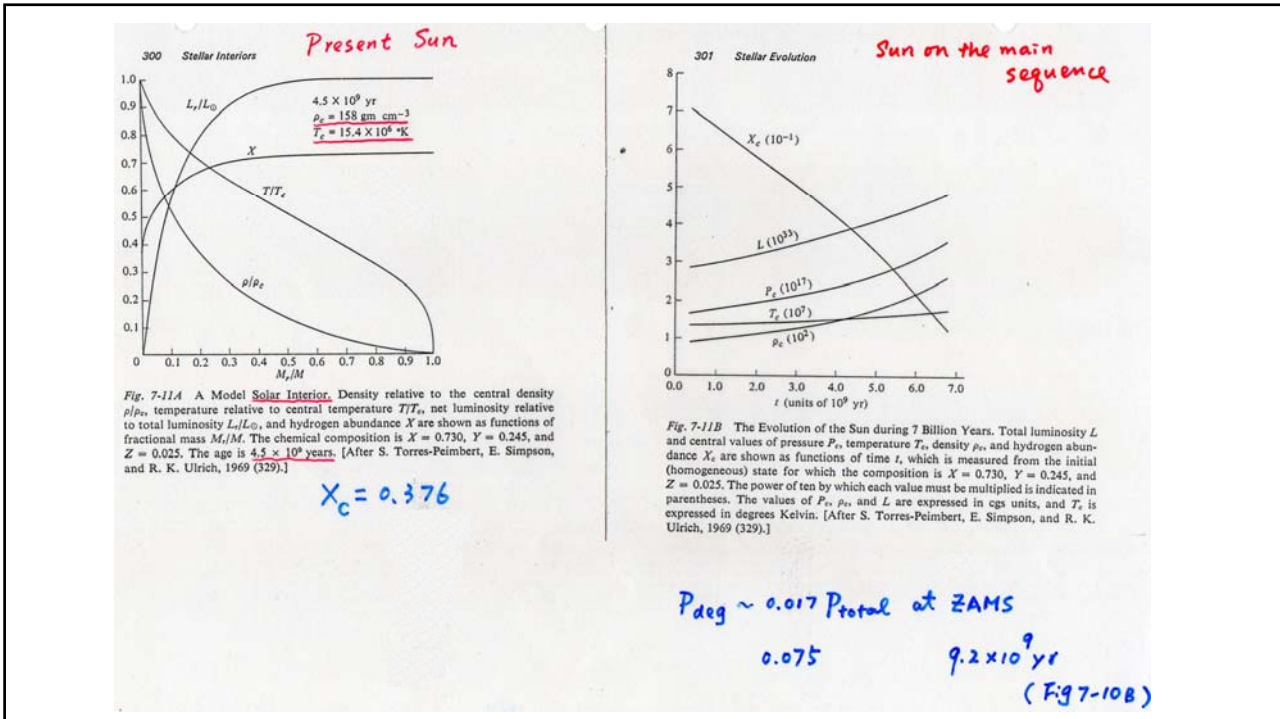
(Point 5') $P_{deg} = 76\% P_{total}$

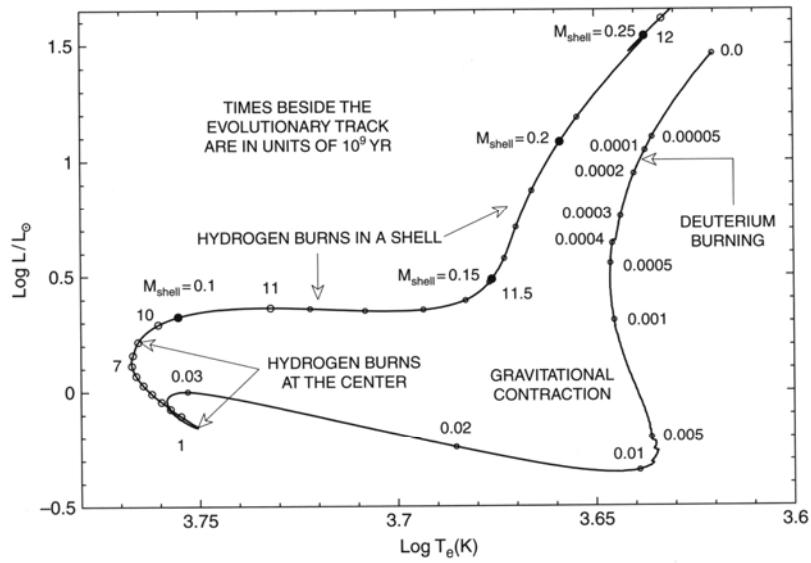
$T_{shell} \uparrow \uparrow \quad \epsilon_{CN} > \epsilon_{PP} \Rightarrow R \uparrow \uparrow, T_{eff} \downarrow \downarrow$

$K \uparrow$ in envelope \rightarrow convection for outer $71 \approx 70\% M$

$X \approx const$ for outer $29\% M$ beyond







Evolutionary track of a $1M_{\odot}$ model ($Z = 0.015$, $Y = 0.275$) during gravitational contraction and central and shell hydrogen-burning phases

Iben 2013

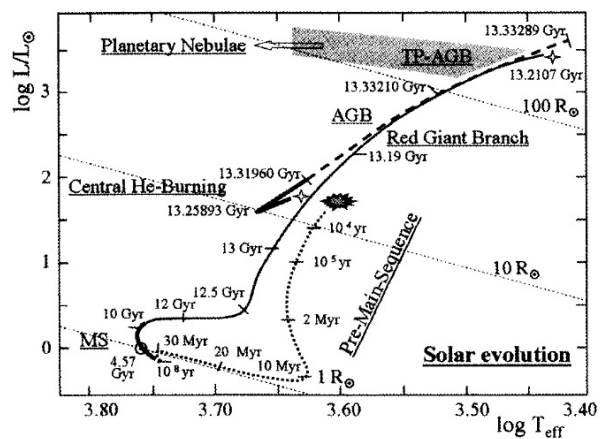
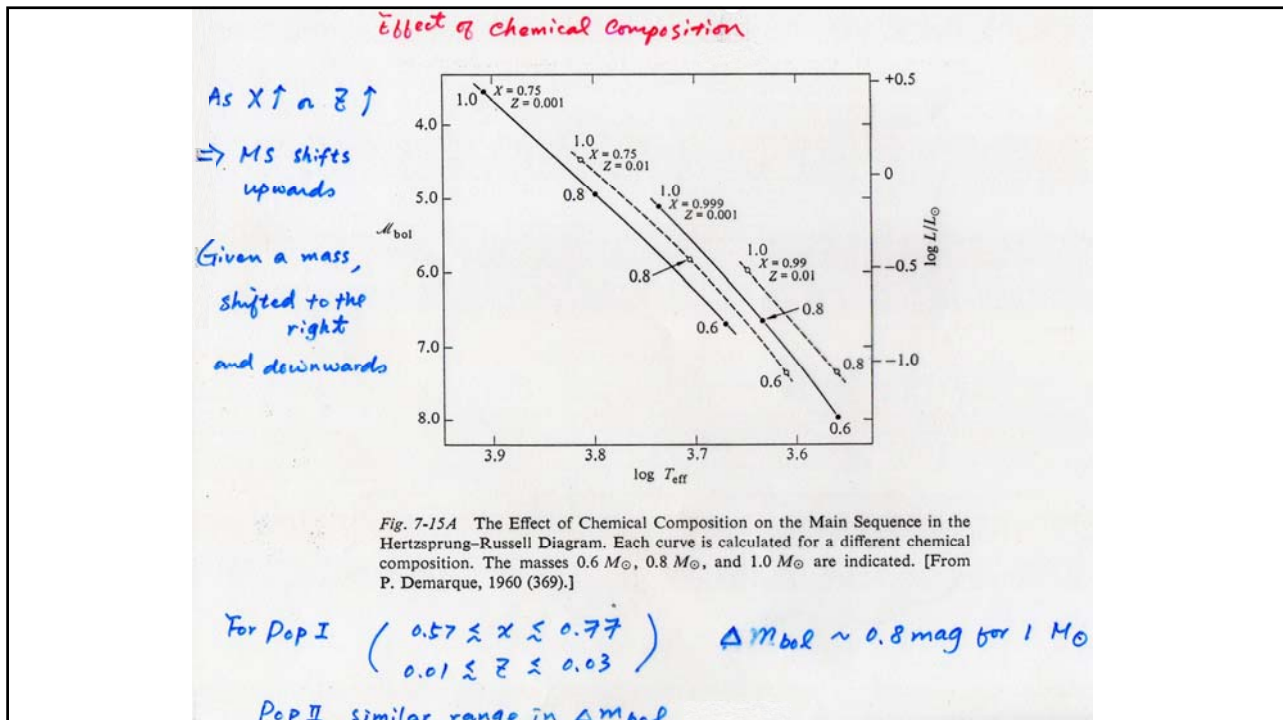


Figure 3.1. The evolution of the Sun. The evolution track of a solar-mass star is shown in the HR diagram from its formation to its death as a planetary nebula. Time is indicated at different steps along the track. The two 4-branch stars correspond to the helium flash and to the subsequent rapid rearrangement of the structure of the star. From Maeder (2009), data from Corinne Charbonnel.

Lequeux 2013



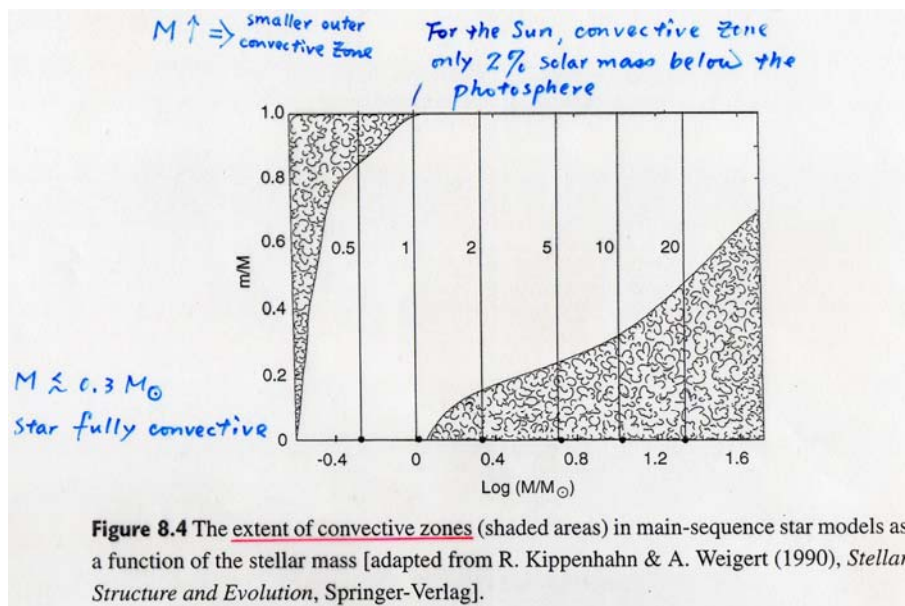
Main Sequence Phase = core H burning

Evidence of thermonuclear reactions at a star's center, i.e., stellar evolution

- (solar) neutrinos
- heavy elements in evolved stars
(isotope ratios \neq YSOs)

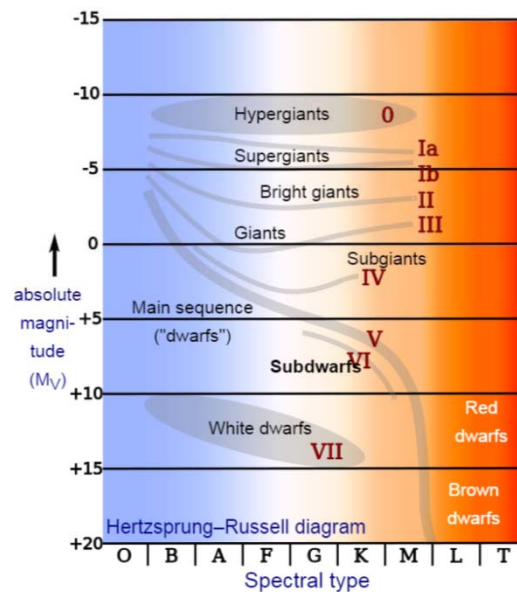
'dredge-up' \leftarrow convective zone
 to bring processed materials to surface

- Stars "disappear", e.g., supernovae



Subdwarfs: The Pop II Main Sequence

- ◆ Luminosity class VI
- ◆ 1.5 to 2 mag fainter than a Pop I MS stars of the same spectral type
- ◆ Low metallicity \rightarrow low opacity \rightarrow (UV excess) \rightarrow low radiation pressure, so smaller, hotter for the same stellar mass



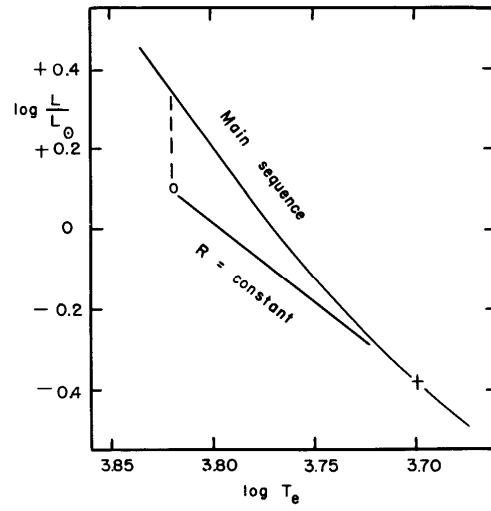


Fig. 17.1. Relation of subdwarfs to the main-sequence in the Hertzsprung-Russell diagram.

Schwarzschild