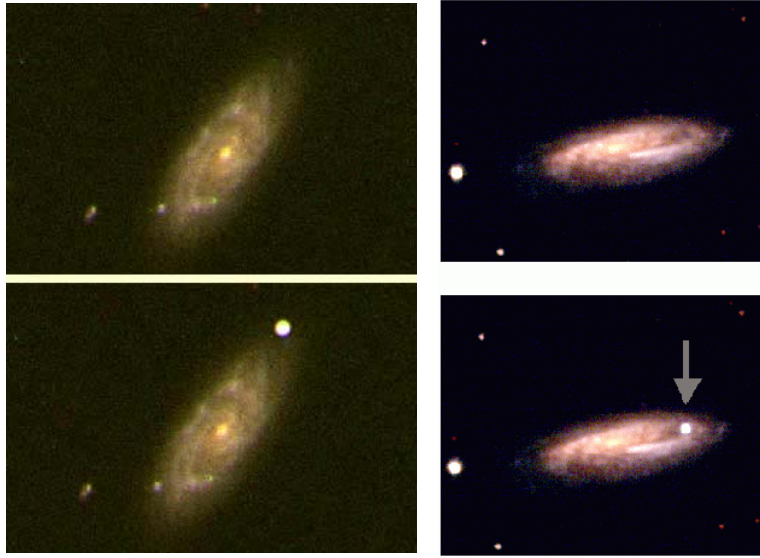
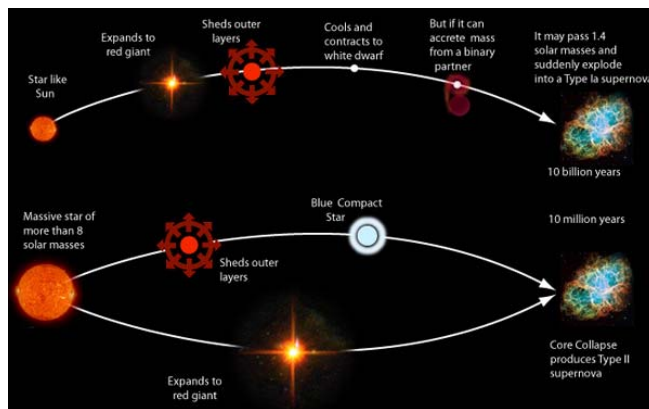


Supernovae and Others



Possible evolutionary paths of a supernova

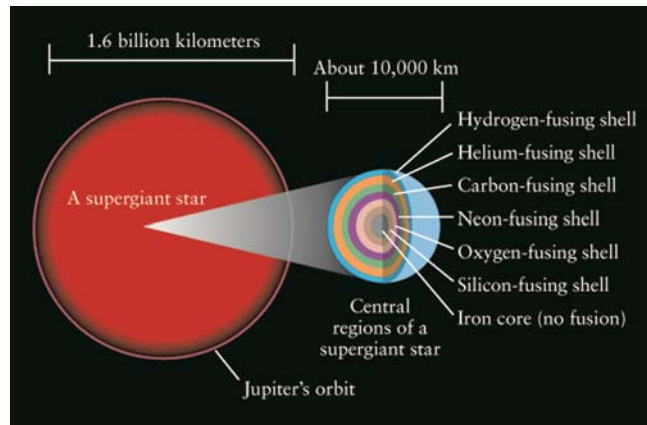
1. Core collapse
2. Thermonuclear runaway



<http://hyperphysics.phy-astr.gsu.edu/hbase/astro/snovcn.html>

Evolution of an Intermediate-mass (8 to 25 M_{\odot}) or High-mass ($> 25 M_{\odot}$) Star

- ❑ Core size \sim Earth
- ❑ Layers of nuclear reactions (cf an onion)
- ❑ Envelope as a supergiant, with the diameter comparable to the Jupiter's orbit



Each subsequent reaction proceeds ever faster; silicon \rightarrow iron

An iron nucleus is most compact between protons and neutrons

\rightarrow further fusion does not release energy

\rightarrow iron core collapses ($D \sim 3000$ km, collapses in ~ 0.1 s)

Evolutionary Stages of a 25- M_{\odot} Star			
Stage	Central temperature (K)	Central density (kg/m^3)	Duration of stage
Hydrogen fusion	4×10^7	5×10^3	7×10^6 yr
Helium fusion	2×10^8	7×10^5	5×10^5 yr
Carbon fusion	6×10^8	2×10^8	600 yr
Neon fusion	1.2×10^9	4×10^9	1 yr
Oxygen fusion	1.5×10^9	1×10^{10}	6 mo
Silicon fusion	2.7×10^9	3×10^{10}	1 d
Core collapse	5.4×10^9	3×10^{12}	0.2 s
Core bounce	2.3×10^{10}	4×10^{17}	milliseconds
Supernova explosion	about 10^9	varies	10 seconds

Iron core collapse \rightarrow 5 billion K \rightarrow **photodisintegration** by energetic gamma rays

The star spends millions of years on the main sequence, synthesizing simple nuclei such as H and He to iron, then takes less than a second to disintegrate back to protons, neutrons and electrons.

Density of the core \nearrow , reaching 4×10^{17} kg/m³ (cf density of a nucleus) in < 1 s \rightarrow even the electron degenerate pressure cannot support the core $\rightarrow e^- + p^+ \rightarrow n^0 + \nu$

Core supported by neutron degenerate pressure \rightarrow **a neutron star**

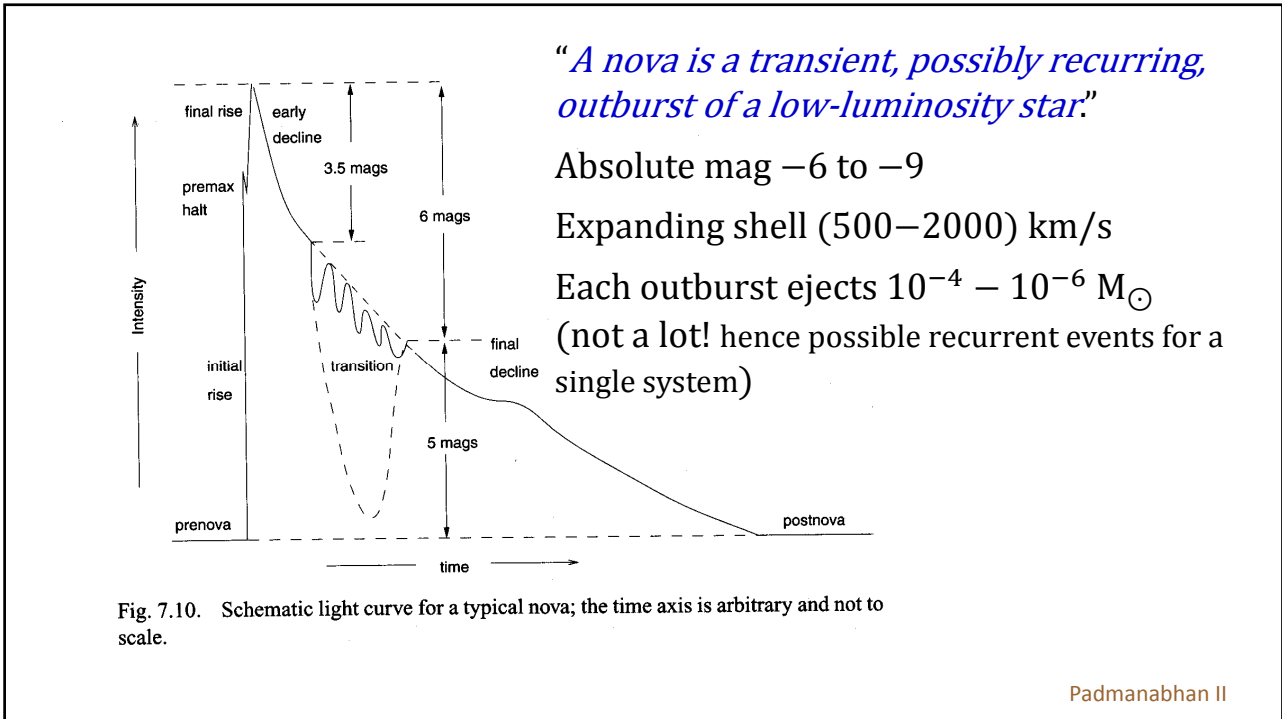
Core bounces \rightarrow **supernova explosion** + **supernova remnant**

Evolution of a Binary System

- Both stars of a few solar masses
 - More massive component \rightarrow RG \rightarrow transfers and loses mass \rightarrow a hot WD
 - Secondary \rightarrow RG \rightarrow fills the Roche lobe \rightarrow transfers mass to the hot WD via an accreting disk
 - Accreted material is compressed and heated, and if $T > 10^7$ K \rightarrow CNO takes place at the base of the accreted layer (even with a thermonuclear runaway if the material is degenerate)
- \rightarrow A **nova** explosion

If accretion onto a C-O WD \rightarrow core mass $> M_{\text{Ch}} = 1.4 M_{\odot}$

\rightarrow Catastrophic collapse + C burning \rightarrow a Type Ia **supernova**



Padmanabhan II

Accreting Binary Systems

- A semi-detached binary system with the primary being a WD: (in increasing L)
- ✓ dwarf nova
 - ✓ classical nova (these may be cataclysmic variables)
 - ✓ type Ia supernova

Table 7.4. Taxonomy of binary systems

Name	Description	Remarks
Algols	Two normal stars (main sequence or subgiants): semidetached binary	Provide checks on stellar evolution, information on mass loss
RS Canum Venaticorum	Chromospherically active binaries	Useful for studies of dynamo-based magnetic activity; exhibits starspot chromospheres, corona, and flares similar to the Sun
W Ursae Majoris	Short period (0.2–0.8 days) Contact binaries	High levels of magnetic activity, important for studying stellar dynamo model
Cataclysmic variables and novae	White dwarfs with cool M-type secondaries; short periods	Exhibits accretion phenomena and accretion disks
X-ray binaries	Neutron star or black hole as the compact component; powerful x-ray sources with $L_x > 10^{35}$ ergs s^{-1}	Study of structure and evolution of compact remnants; indirect evidence for black holes
ζ Aurigae/VV Cephei	Long-period interacting binaries; Late-type supergiant plus a hot companion	Study of supergiant phase, especially atmospheres of supergiants

Padmanabhan II

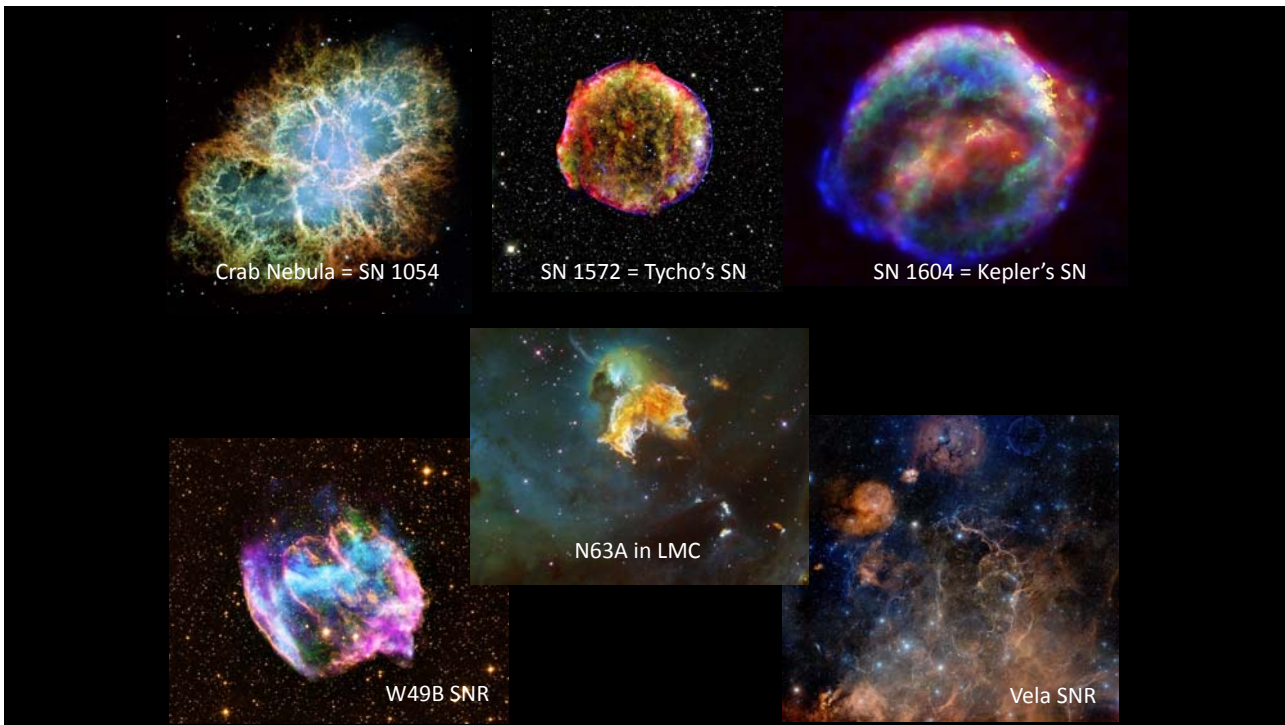
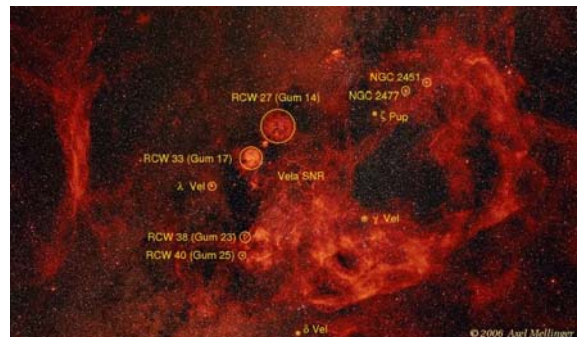


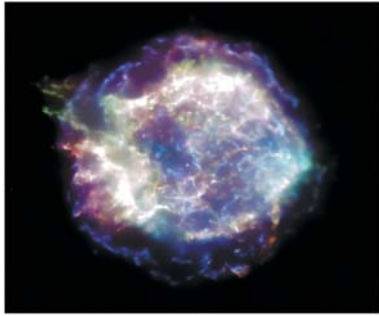
Figure 13-11
Discovering the Universe, Seventh Ed
© 2006 W.H. Freeman and Company

Gum Nebula is the largest SNR in the sky, originated from a supernova explosion perhaps a Myr ago.



Gum Nebula has a angular extent > 40 deg \rightarrow linear size more than 2300 ly across \rightarrow The closest part from Earth ~ 300 ly

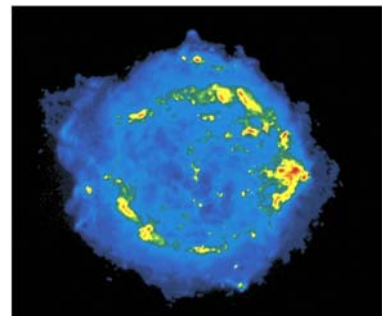
Cassiopeia A SNR is 3.4 kpc from us. The explosion should have been seen 300 years ago, but was not recorded.



X rays



Visible
(HST)



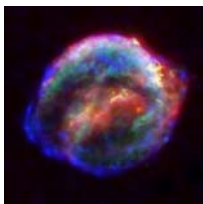
Radio

Supernovae in History

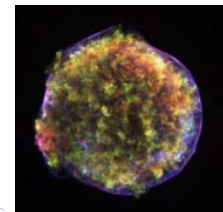
- OB association in Scorpius-Centaurus
Solar system within 150 ly 2 Myr ago; should have experienced SN explosions

Table 10.1 Historical supernovae

<i>Galaxy:</i> Name	Year	Distance × 3000 ly
Milky Way:		
Lupus	1006	1.4
Crab	1054	2.4
3C 58	1181(?)	2.6
Tycho	1572	2.5
Kepler	1604	4.2
Cas A	1658±3	2.8
Andromeda	1885	700
LMC: SN1987A	1987	50



Chandra SN1604



Chandra SN1572

Crab Nebula (in Taurus)

The Expanding Crab Nebula 1973 to 2001

SN clearly recorded in AD1054 by Chinese astronomers
→ "Chinese supernova"



西元1054年七月(宋仁宗)
 元和元年五月(金太宗)
 起新星爆炸, 據記載
 最明亮時相當於太白
 (金)星的光芒, 長達到
 23天在白天可見, 直
 1056年四月(嘉祐元
 年三月)肉眼才看
 天闕客星

凡十一日没三年三月乙巳出東南方大中祥符四年正月丁丑朔斗魁前天禧五年四月丙辰出軒轅前星西北大知機運行經軒轅太星入太微垣極右執法犯大將歷星西北凡七十五日入濁没明道元年六月乙巳出東北方近濁有芒彗至丁巳凡十三日没至和元年五月己丑出天關東南可數寸歲餘稍没熙寧二年六月丙辰出箕度中至七月丁卯犯箕乃散三年十一月丁未出天因元祐六年十一月辛亥出參度中犯掩制星壬子犯九游星十二月癸酉入奎至七年三月辛亥乃散紹興八年五月守妻

SN 1987A

First observed 24 Feb, 1987

not quite SN II

pre SN progenitor observed and sp. classified

Sanduleak - 69 202

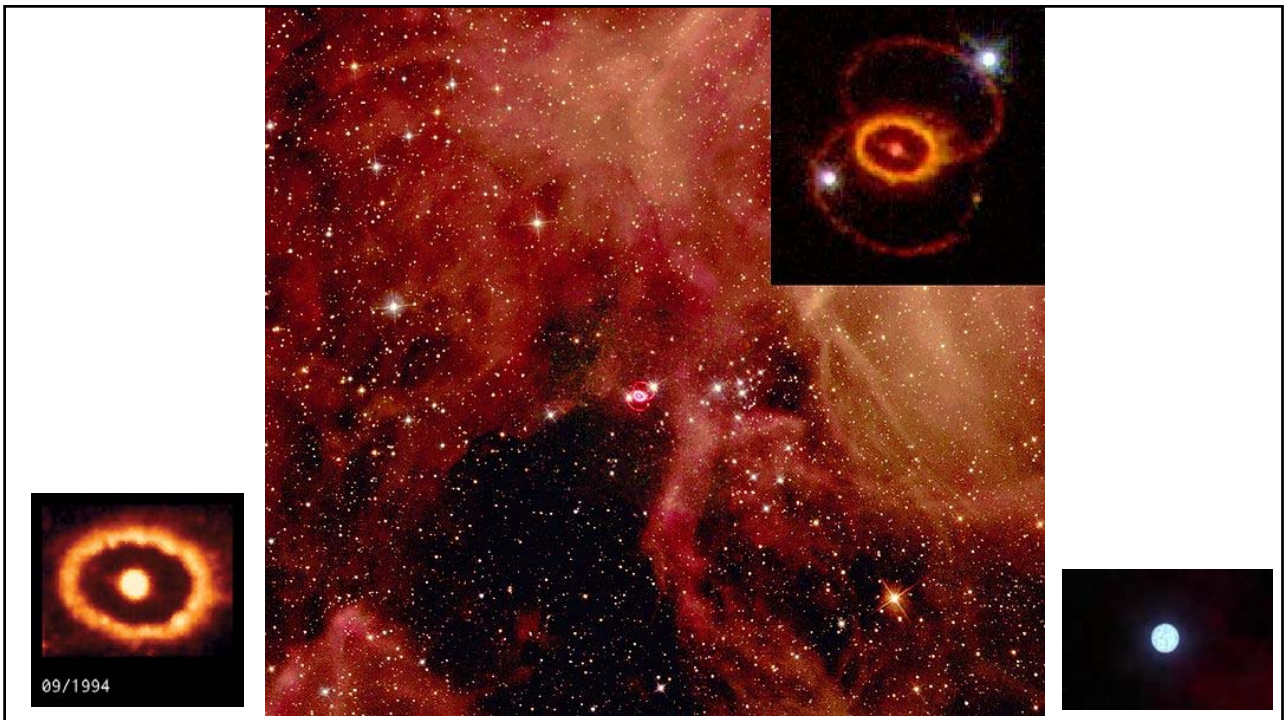
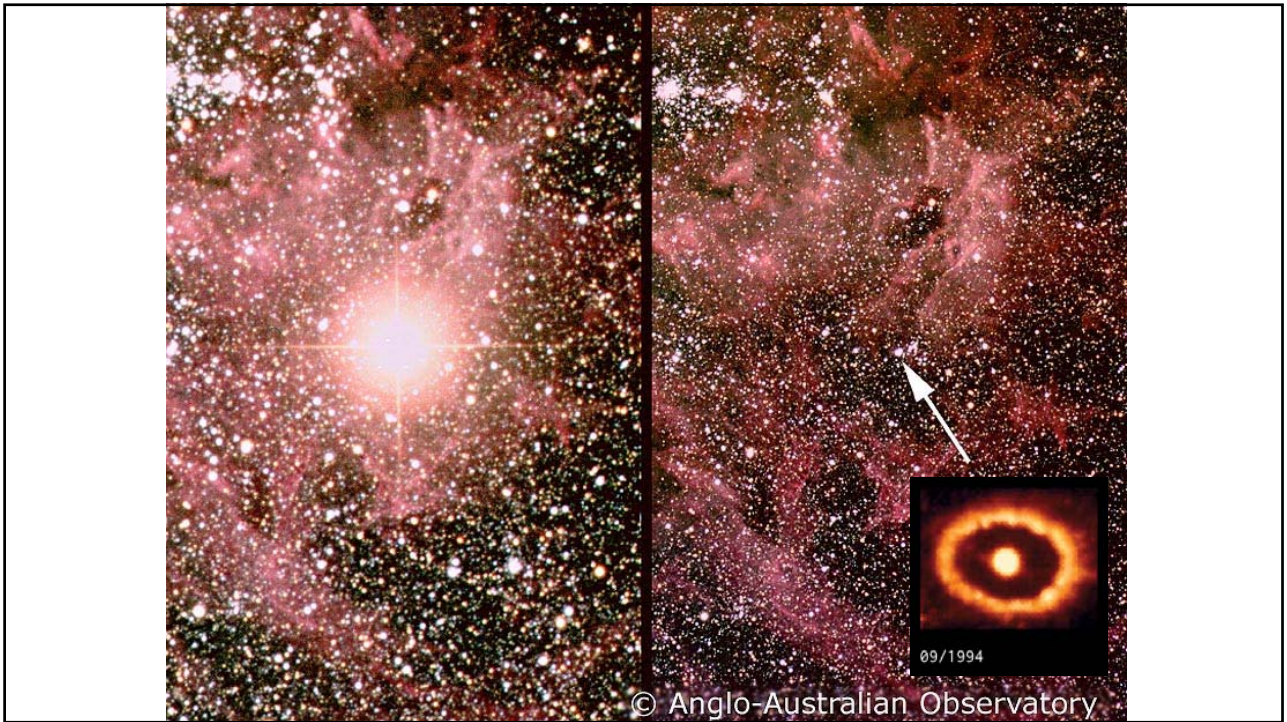
Sp = B3 I

$L \sim 1.1 \times 10^5 L_{\odot}$; $T_{\text{eff}} \sim 16,000 \text{ K}$

($M \sim 16-22 M_{\odot}$)

Pop I but metal-poor

Neutrino events (kamiokande) detected
 hours before SN visible

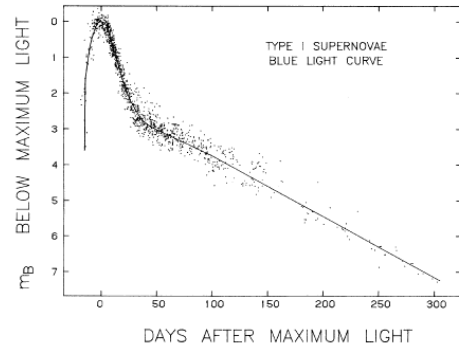


Supernova classification

Divided into two types based on spectra

Type I – with no H lines

- Further classification based also on spectra:
 - ✓ Ia – strong Si line
 - ✓ Ib – no H or Si line, but have He lines
 - ✓ Ic – no Si, He or H lines
- Ia found in all types of galaxies
 - ➔ associated with white dwarfs in binary systems



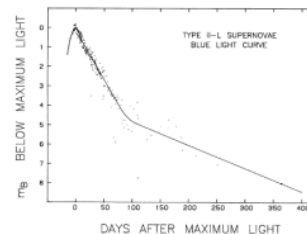
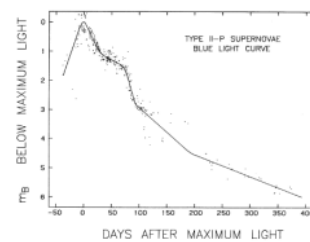
Doggett and Branch (1985)
Astron. J., **90**, 2303

Supernova classification II

Type II – with H lines

Further classification based on light curve

- ✓ II P – flat ‘plateau’ in LC
 - ✓ II L - linear light curve
- Type II, Ib, Ic found only in spiral arms of spiral galaxies (i.e. regions of recent star formation) ➔ massive stars
 - Core collapse supernovae with mass loss in Ib and Ic



Doggett and Branch (1985)
Astron. J., **90**, 2303

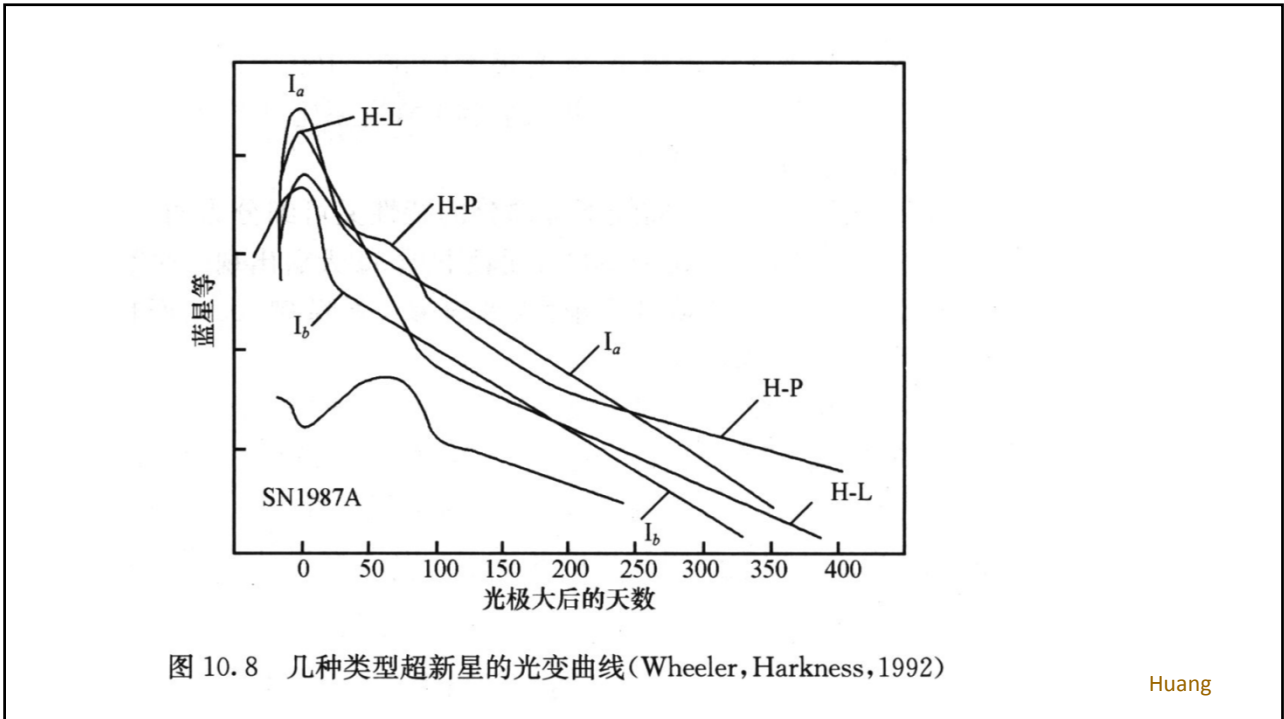
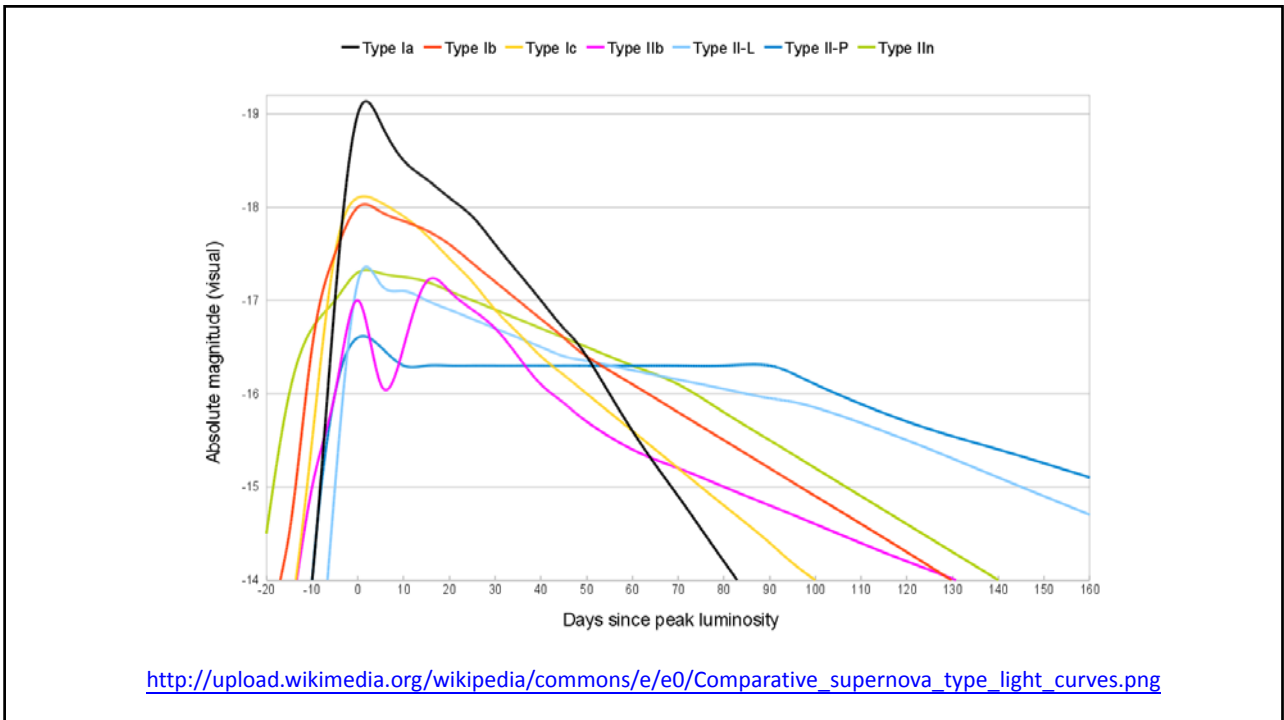
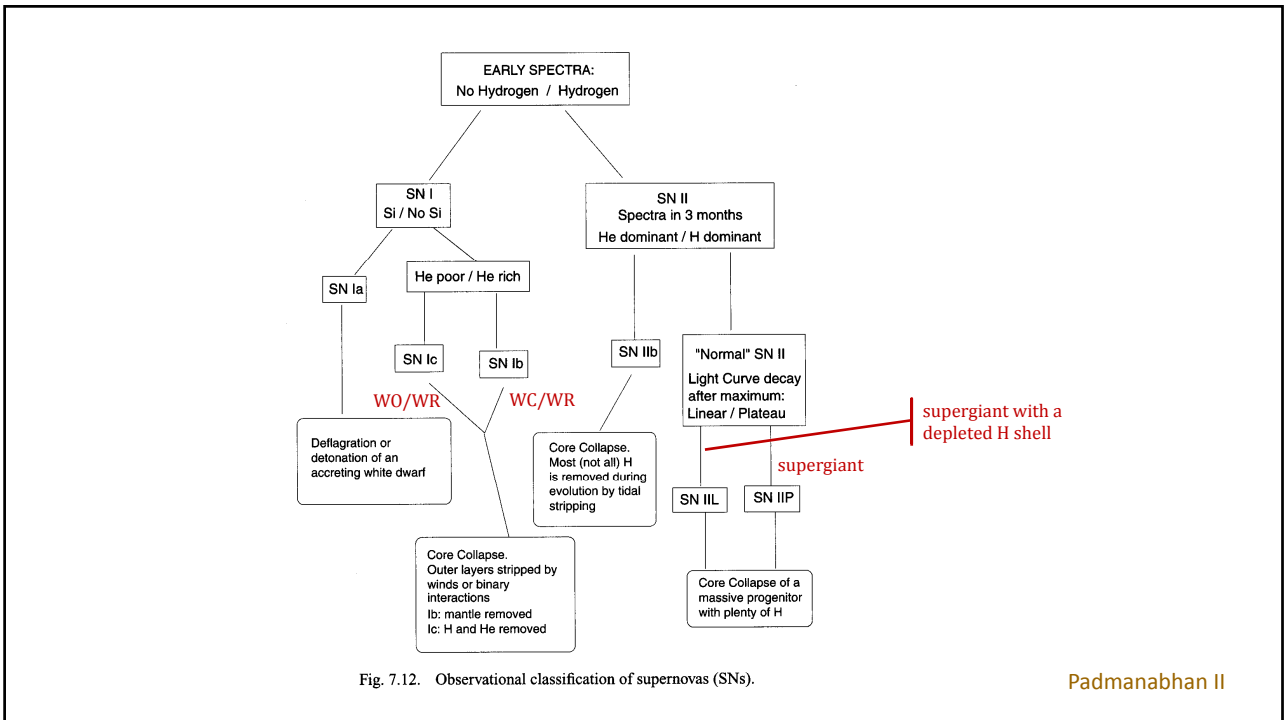
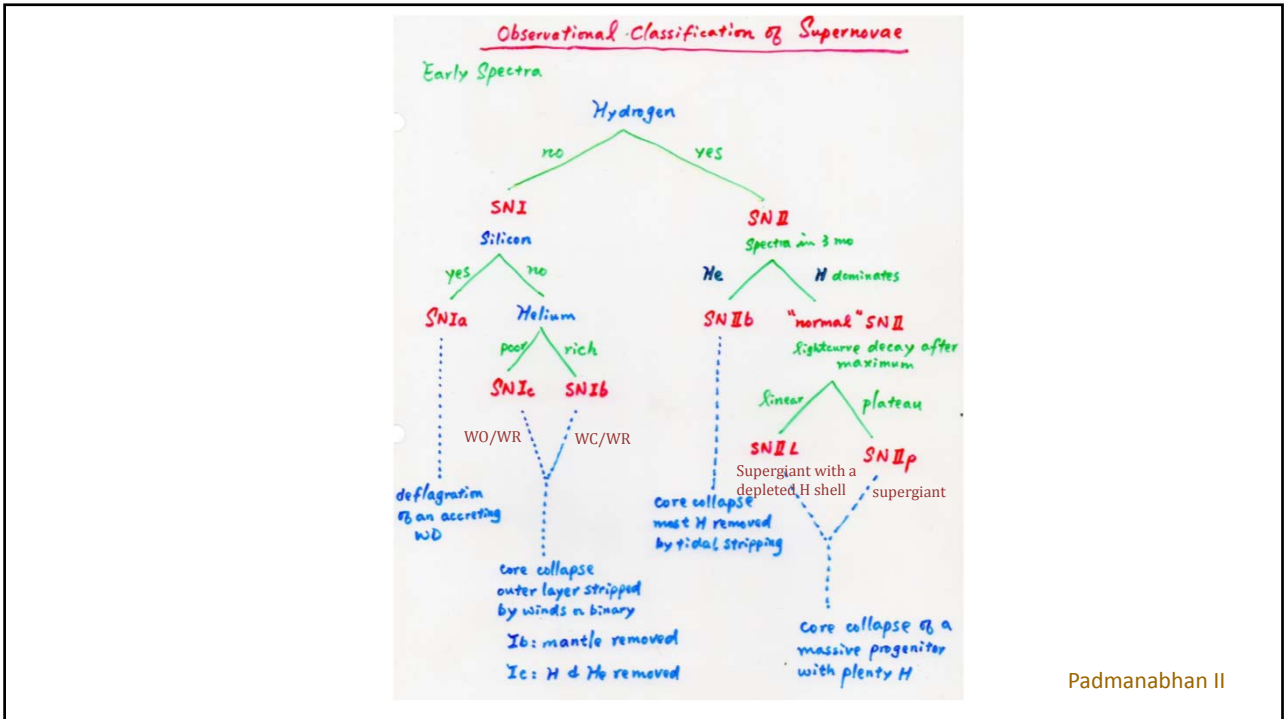


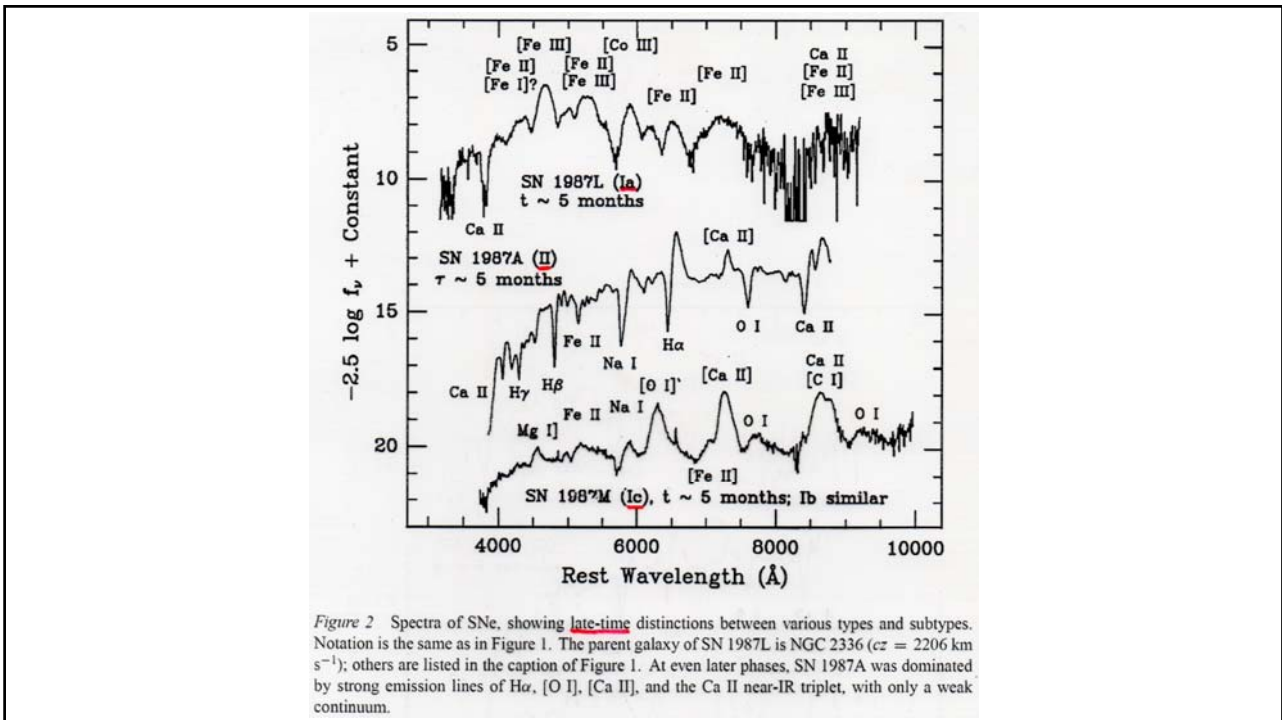
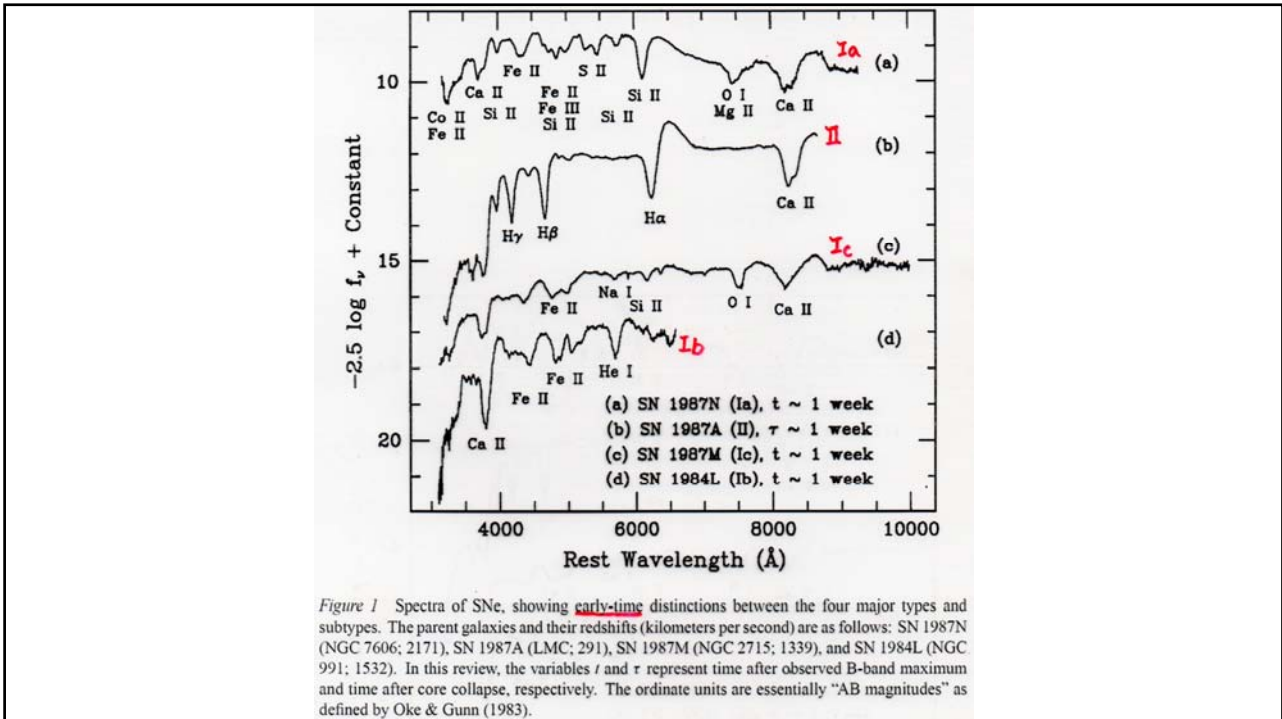
图 10.8 几种类型超新星的光变曲线(Wheeler, Harkness, 1992)

Huang



http://upload.wikimedia.org/wikipedia/commons/e/e0/Comparative_supernova_type_light_curves.png





Elements observed in SNI spectra

subclass	~ maximum	~ 6 months
SN Ia	O, Mg, Si, S, Ca, Fe	Fe, Co
SN Ib	O, Ca, Fe	O, Ca, Mg
SN Ic	He, Fe, Ca	O, Mg

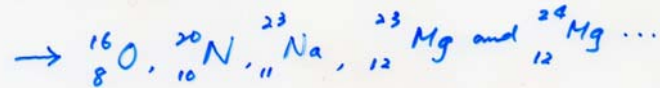
Hansen + Kawaler

- The energy source of the type Ia supernovae comes from nuclear fusion. The explosion produces various radioactive isotopes, e.g., nickel becomes cobalt.
- So far, a few thousands SNe have been detected in external galaxies.
- Applying the statistics, the Milky Way should have occurred one type Ia SN every 36 years, and one type II SN every 44 years.
- Each century, therefore, we should have seen about 5 supernovae. So, what happened?
- Which star is most likely the next?
In the solar neighborhood?



Supernovae

$M > 8 M_{\odot}$ core carbon burning



Eventually ${}^{54}_{26}\text{Fe}, {}^{56}_{26}\text{Fe}$, and ${}^{56}_{28}\text{Ni}$

Three critical processes

"iron" core

① Neutrino cooling

At this stage, a lot of ν 's

Ex. during Si burning, a $20 M_{\odot}$

$$L_{20M_{\odot}} \sim 4.4 \times 10^{38} \text{ erg s}^{-1}$$

$$L_{\nu} \sim 3.1 \times 10^{45} \text{ erg s}^{-1}$$

Solar neutrino flux
 $= 7 \times 10^{10} / \text{cm}^2 / \text{s}$

Neutrino mass
 $< 0.32 \text{ eV}$ for the sum of
 masses of 3 known flavors

② Photodisintegration

Energetic photons disintegrate iron nuclei
 into α particles and protons

This is an 吸熱 endothermic process; i.e. takes
 energy away and lowers pressure support
 at the core



3. Neutronization

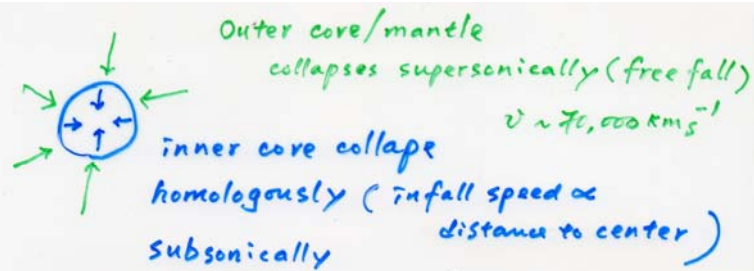
possible inverse β decay $p^+ + e^- \rightarrow n^0 + \nu$

\downarrow
 $n_e \downarrow \Rightarrow P_{deg} \downarrow$

ν escape \Rightarrow cooling

\Rightarrow A rapid collapse of the core

Note 放熱
 exothermic
 releasing energy



Inner core collapses until $\rho_c \sim 8 \times 10^{14} \text{ g cm}^{-3}$
 This is $3 \times \rho_{\text{nucleus}} \rightarrow$ nuclear reactions
 produce repulsive force
 (cannot "squeeze" anymore)

This sends an outgoing pressure wave through
 the infalling material

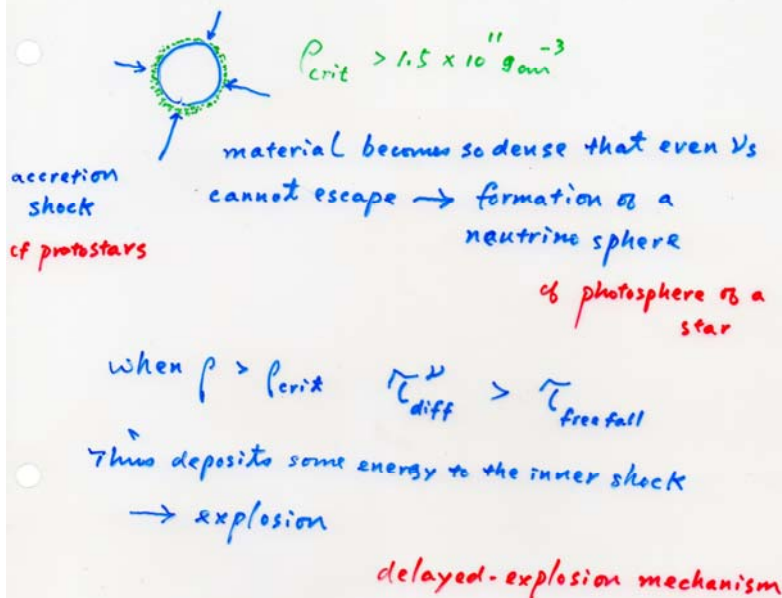
Two possibilities

When the shock propagates through the inner core \rightarrow photodisintegration

- (i) If the iron core is small, shock emerges energetically \rightarrow an explosion on the outer material
prompt hydrodynamic explosion

This can explain the explosion of MS stars with $8 \sim 12 M_{\odot}$, ending with a core $< 1.2 M_{\odot}$. But the progenitor of SN1987A had $20 M_{\odot} \rightarrow$ need an alternative mechanism to explain more massive SNe

(ii) If the core is massive, inner shock stalls



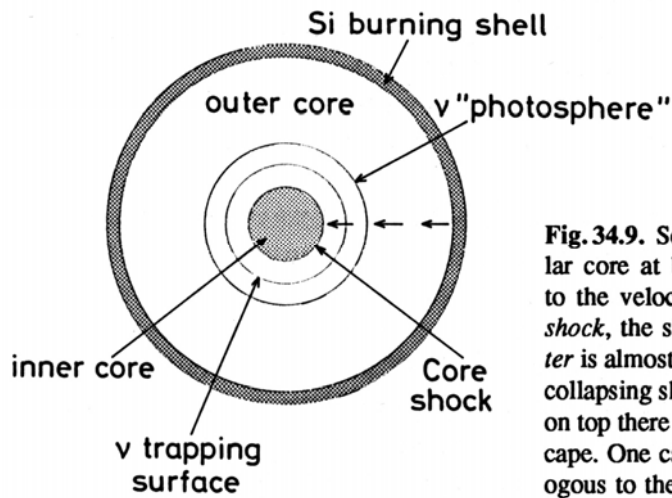


Fig.34.9. Schematic picture of a collapsing stellar core at bounce. The short arrows correspond to the velocity field. At the sphere labelled *core shock*, the shock is formed inside which the *matter* is almost at rest. Above the shock there is a still collapsing shell in which neutrinos are trapped. But on top there is a shell from which neutrinos can escape. One can define a neutrino photosphere analogous to the photosphere in a stellar atmosphere

Total kinetic energy of outgoing shock
 $E_{kin} \sim 10^{51} \text{ ergs}$
 (This is only 1% of the energy in energy neutrinos)
 \rightarrow outer material expands & becomes optically thin
 \Rightarrow SN explosion, releasing $\sim 10^{49} \text{ ergs}$ in photons
 with $L_{peak} \sim 10^{43} \text{ ergs}^{-1} \sim 10^9 L_{\odot}$
 c.f. Milky Way

Roughly if original mass $< 2.5 M_{\odot}$, can be supported neutron pressure; may survive the explosion \rightarrow a neutron star

If $M > 2.5 M_{\odot} \rightarrow$ collapse to a black hole

Neutrino Trapping

Mean free path $\lambda = 1/n\sigma$

cross section $\sigma = \sigma_0 \epsilon^2$

For neutrinos, $\sigma_0 \sim 2 \times 10^{-44} \text{ [cm}^2\text{]}$

$\epsilon =$ relative energy in unit of e^- rest mass

In lead $\rho = 11.34 \text{ g cm}^{-3}$, $A = 208$

A neutrino of 1 MeV, or $\epsilon = 2$, $\lambda \sim 3.8 \times 10^{20} \text{ cm}$
 $\sim 380 \text{ ly}$

In a collapsing stellar core

$$\rho \sim 4 \times 10^{14} \text{ g cm}^{-3}$$

Neutrinos have $\sim 150 \text{ MeV}$, or $\epsilon \sim 300$

$$\rightarrow \lambda = 2.2 \text{ cm}$$

So if $R \sim 10 \text{ km}$, the mean free time, or diffusion time $\tau \sim 5 \text{ s}$

Supernova Observations

$$L_{\text{peak}} \sim 10^9 - 10^{10} L_{\odot}$$

Time before peak (rising time) $\sim 2 \text{ wks}$

$$\text{Shell expansion } v \sim 5 - 10 \times 10^3 \text{ km s}^{-1}$$

supernova remnant (SNR)

lasting $\sim 10^3 \text{ yrs}$

$$\bar{E}_{\text{total}} \sim 10^{51} - 10^{53} \text{ ergs} = \bar{E}_{\text{photons}} + \bar{E}_{\text{neutrinos}} + \bar{E}_{\text{kinetic}}$$

usually minor ($\sim 1\%$) } predominant

cooling core \rightarrow a neutron star

$$\rho \sim 10^{14} \text{ g cm}^{-3}, M \sim M_{\odot}$$

- 1932 Chadwick discovered the neutron.
- Landau thought neutron stars might exist.
- 1934 Baade & Zwicky suggested neutron stars as remnants of supernova explosions.
- 1939 Oppenheimer & Volkoff proposed the first model for neutron stars, with estimates of masses and sizes.
- 1967 Hewish & Bell discovered the pulsar.
- Gold & Pacini proposed pulsars as fast spinning, highly magnetized neutron stars.

Mass limit of neutron degenerate stars uncertain because of uncertain EOS at $\rho > \rho_{\text{nuclear}}$, ranging from $0.7 M_{\odot}$ for non-interacting neutrons
 (Tolman-Oppenheimer-Volkoff limit)
 up to $\sim 2.5 M_{\odot}$

A pulsar $\left\{ \begin{array}{l} R \sim 10 \text{ km} \\ B \sim 10^{13} \text{ G} \\ \text{Spin down from periods } \sim \text{ms} \end{array} \right.$

Some SNRs host no pulsars.

- not enough e^- , not strong enough \vec{B} ?
- we are not in the 'lighthouse beam'?
- neutron star destroyed completely
- neutron star 'kicked out'

some NSs (or pulsars) have space motion $\sim 1000 \text{ km s}^{-1}$

Annu. Rev. Astron. Astrophys. 1992. 30: 359–89

TYPE Ia SUPERNOVAE AS STANDARD CANDLES

David Branch

Department of Physics and Astronomy, University of Oklahoma,
Norman, Oklahoma 73019

G. A. Tammann

Astronomisches Institut der Universität Basel, Venusstrasse 7,
CH-4102 Binningen, Switzerland, and European Southern Observatory,
Karl-Schwarzschild-Str. 2, D-8049 Garching/München, Germany

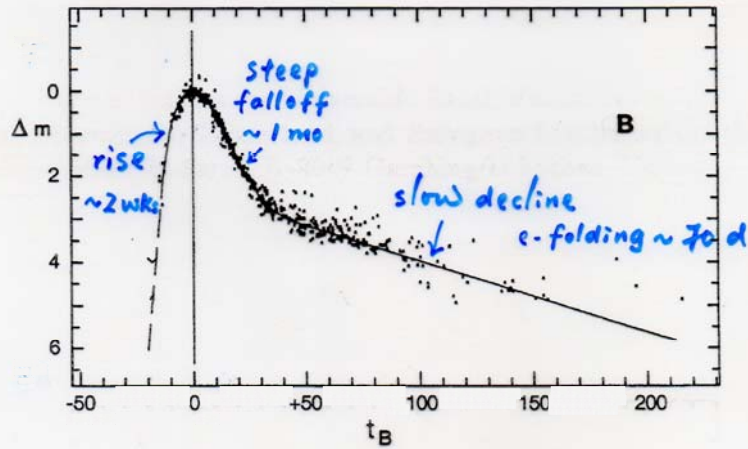


Figure 2 The standard B light curve (adapted from Cadonau 1987), based on observations of 22 SNe Ia.

Many sky survey projects, e.g., Pan-STARRS (PS), Palomar Transient Factory (PTF), Sky Mapper, Large Synoptic Survey Telescope (LSST), to catch SNe early on, for pre-SN characterization

Type I

No H in spectra

Located in spirals or ellipticals

If in spirals, usually NOT in arms

but some seen near H II regions or

arms → Ib

Ia

Standard model

A WD close to Chandrasekhar limit

+ a mass losing companion

→ accretion onto WD → $R_{WD} \downarrow$

→ $T \uparrow$, if heat not carried away

⇒ ignition of C, O, ...

thermonuclear explosion

Fate of WD depends on accretion rate and M_{WD}

- partial explosion w/ a WD left behind
- disrupt completely; no stellar remnant
- NS?

Population II progenitor

SNIa \sim 80% of Type II $M_{\text{peak}} \sim -17$ mag

All SNIa lightcurves similar
 \rightarrow standard candles

Averaged 1 SNI/100 yrs in a spiral

Type II $M_{\text{peak}} \sim -19$ mag

With hydrogen lines in spectra

Found in spiral arms or Irr.

If formed in the same arm

timescale $< 10^7$ yr $\Rightarrow M > 10 M_{\odot}$
 progenitor

Standard model,

End of massive star evolution

gravitational collapse

Population I progenitor

Fate \rightarrow NS, BH

Type II (core collapse) SN progenitors

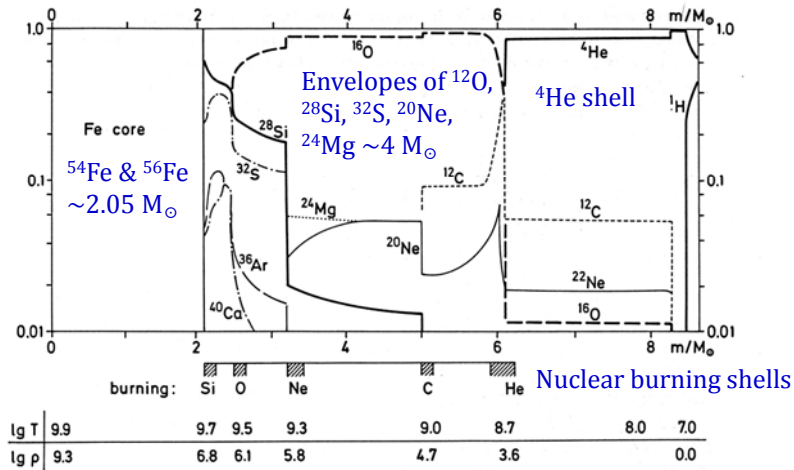


Fig. 34.7. The chemical composition in the interior of a highly evolved model of a $25M_{\odot}$ star of population I. The mass concentrations of a few important elements are plotted against the mass variable m . Below the abscissa the location of shell sources and typical values of temperature (in K) and density (in g cm^{-3}) are indicated. (After [WOOSLEY, WEAVER, 1986](#))

Ann. Rev. Astron. Astrophys. 1986. 24 : 205–53

THE PHYSICS OF SUPERNOVA EXPLOSIONS¹

S. E. Woosley

Board of Studies in Astronomy and Astrophysics, Lick Observatory,
University of California, Santa Cruz, California 95064

Thomas A. Weaver

Special Studies Group, Lawrence Livermore National Laboratory,
Livermore, California 94550

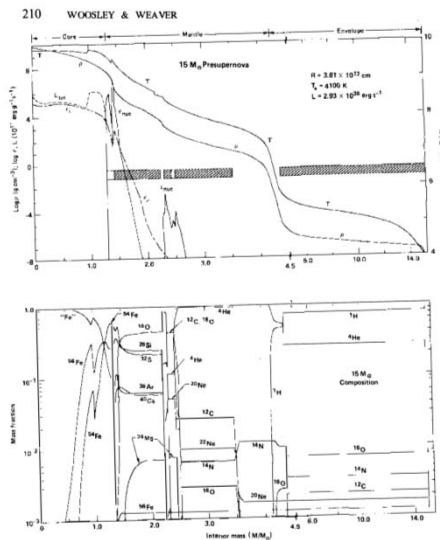
¹ The US Government has the right to retain a nonexclusive royalty-free license in and to any copyright covering this paper.

Table 1 Presupernova models and explosions^a

Main sequence mass	Helium core mass	Iron core mass	Explosion energy ^b (10^{50} erg)	Residual baryon mass ^b	Neutron star mass ^b	Heavies ejected ($Z \geq 6$)
11	2.4	— ^c	3.0	1.42	1.31	~0
12	3.1	1.31	3.8	1.35	1.26	0.96
15	4.2	1.33	2.0	1.42	1.31	1.24
20	6.2	1.70	—	—	—	2.53
25	8.5	2.05	4.0	2.44	1.96	4.31
35	14	1.80	—	—	—	9.88
50	23	2.45	—	—	—	17.7
75	36	— ^d	—	—	BH?	30?
100	45	~2.3 ^d	≥4	—	BH?	39?

^a All masses given in units of M_{\odot} .
^b All except for 100 M_{\odot} determined by Wilson et al. (1985).
^c Never developed iron core in hydrostatic equilibrium.
^d Pulsational pair instability at oxygen ignition.

Woosley & Weaver



210 WOOSLEY & WEAVER
 Ann. Rev. Astr. Astrophys. 1986.24:205-253. Downloaded from www.annualreviews.org by National Central University on 05/26/14. For personal use only.

Figure 1 Structure and composition of a $15-M_{\odot}$ presupernova star at a time when the edge of its iron core begins collapsing at 1000 km s^{-1} . Neutrino emission from electron capture (ϵ) dominates photodisintegration in the total energy losses (L_{ν}) throughout most of the iron core. Central temperature here is $7.62 \times 10^9 \text{ K}$, and density is $9.95 \times 10^7 \text{ g cm}^{-3}$. Spikes in the nuclear-energy generation rate (ϵ_{nuc}) show the location of active burning shells, while cross-hatched, blank, and open bars indicate regions that are convective, semiconvective, and radiative respectively. The species "Fe" includes all isotopes from $48 \leq A \leq 65$ having a neutron excess greater than ^{56}Fe . Note a scale break at $4.5 M_{\odot}$. Figure adapted from Woosley & Weaver (1985).

Woosley & Weaver

- ◆ Core collapse in free-fall,
 $\tau_{\text{ff}} \approx (G\bar{\rho})^{-1/2} \approx 1 \text{ ms}$, if $\rho = 10^{10} \text{ g cm}^{-3}$
- ◆ Central density and pressure $\uparrow \uparrow$ and becomes subsonic;
 outer material remains free-fall and supersonic.
- ◆ Transition zone = constant speed, force free, relativistic
 electron degenerate pressure balances gravity
 \rightarrow Chandrasekhar limit
- ◆ Inside M_{ch} , $\rho \approx 2.3 \times 10^{14} \text{ g cm}^{-3}$ (nuclear),
 strong force; material incompressible; neutron degeneracy
 Outside $M_{\text{ch}} \rightarrow$ supersonic accretion
- \rightarrow Shock wave and bounce

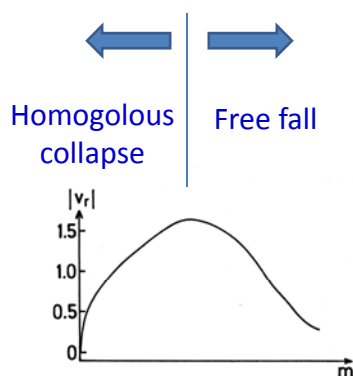


Fig. 34.8. Schematic picture of the velocity distribution in a collapsing stellar core originally of $1.4 M_{\odot}$ after numerical calculations (VAN RIPER, 1978). Note the two regimes: on the left $|v_r|$ (in units of 10^9 cm s^{-1}) increases in the outward direction. It corresponds to a (roughly) homologously collapsing part, while on the right $|v_r|$ decreases with m . This corresponds to the free-fall regime

Energy released in a core collapse

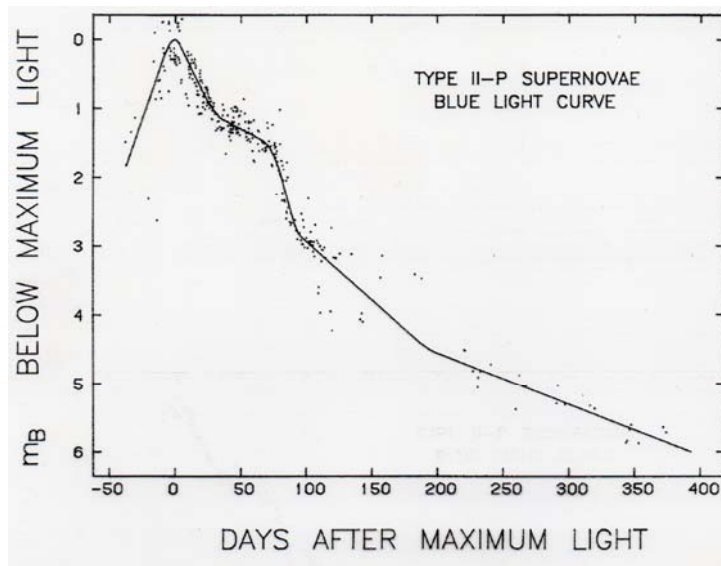
$$R: R_{WD}(0.01 R_{\odot}) \rightarrow R_{NS}(10 \text{ km})$$

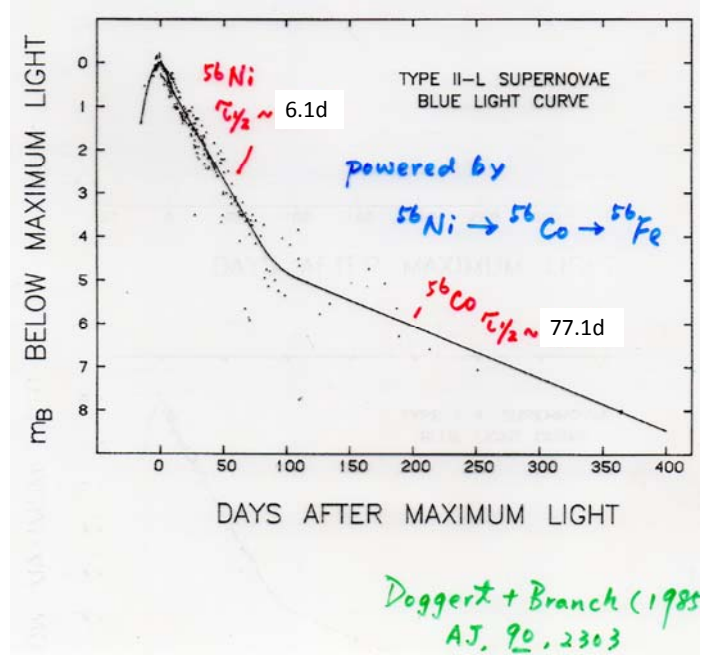
$$\Delta \tilde{E}_{\text{grav}} \sim \frac{GM_{\odot}^2}{R_{NS}} \sim 3 \times 10^{53} \text{ ergs}$$

10% used up by nuclear processes

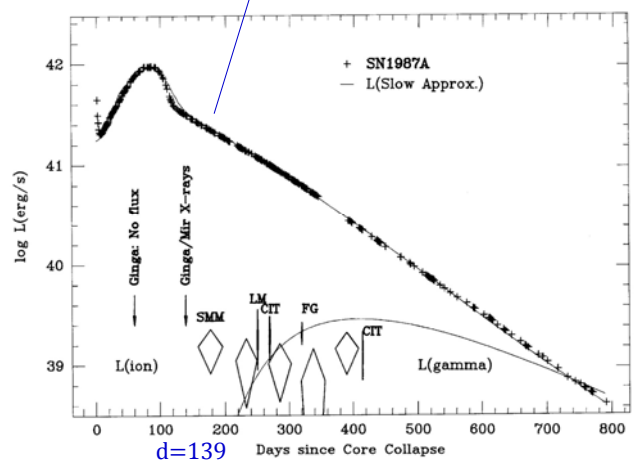
rest to radiation and ejecting material

↓
(luminosity & neutrinos)





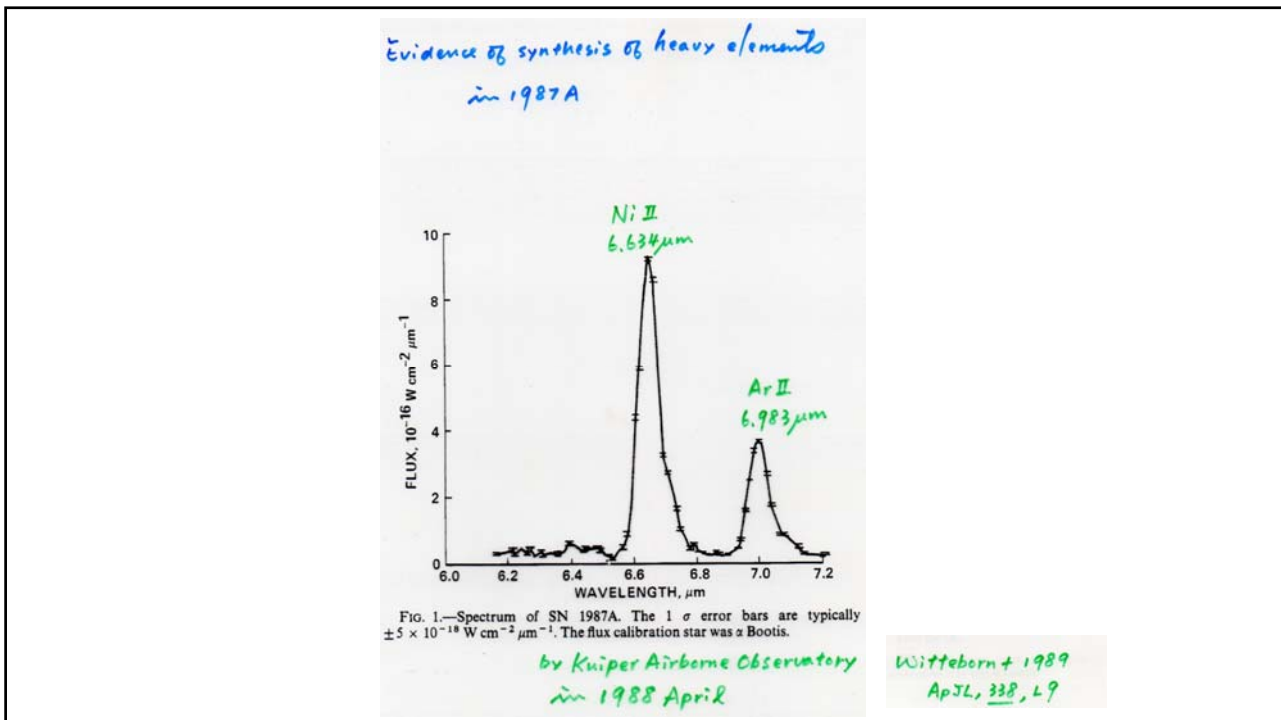
UVOIR light curve



d=139
x-rays

d=178
gamma-ray

Arnett



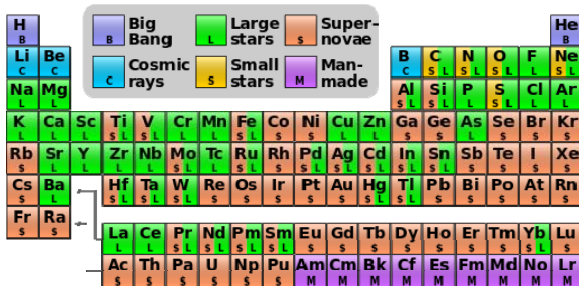
- ◆ During a type II SN explosion, the neutron star reaches $T \approx 10^{11} \sim 10^{12}$ K, but cools down quickly by neutrinos, to $T \approx 10^9$ K in a day, 10^8 K in 100 years.
- ◆ This is cold, $kT \approx 10$ keV
cf. Fermi energy ($\rho \approx 10^{14} \text{ g cm}^{-3}$), $\varepsilon_F \approx 1000$ MeV,
so $T_{\text{neutron star}} \rightarrow 0$, and all electrons, protons, and neutrons are at the lowest energy states.
- ◆ Neutron beta decay process, $n \rightarrow p + e^- + \bar{\nu}_e$, does not take place, because the resultant electron and neutrino are not energetic enough (energy difference between n and p)
- ◆ But inverse beta decay $p + e^- \rightarrow n + \nu_e$ OK
- ➔ All neutrons

- So far thousands of SNe have been detected in external galaxies.
- In the Milky Way, a type Ia SN is expected every 36 years, and a type II SN is expected every 44 years. Then each century should see about 5 SNe.

Notable Historical supernovae in the Milky Way

SN 1006	Lupus	Ia	-7.5 mag, brightest in history
SN 1054	Taurus	II	Chinese SN; Crab Nebula as the SNR
SN 1572	Cassiopeia	Ia	Tycho's Nova
SN 1604	Ophiuchus	Ia	Kepler's Star
SN 1680	Cassiopeia	IIB	Not observed, Cas A as the SNR

Solar System Abundances



The 25 Most Abundant Nuclei

Rank	Z	Symbol	A	Nucleon Fraction	Source (process)
1	1	H	1	7.057e-01	Big Bang
2	2	He	4	2.752e-01	Big Bang, CNO, pp
3	8	O	16	9.592e-03	Helium
4	6	C	12	3.032e-03	Helium
5	10	Ne	20	1.546e-03	Carbon
6	26	Fe	56	1.169e-03	e-process
7	7	N	14	1.105e-03	CNO
8	14	Si	28	6.530e-04	Oxygen
9	12	Mg	24	5.130e-04	Carbon
10	16	S	32	3.958e-04	Oxygen
11	10	Ne	22	2.076e-04	Helium
12	12	Mg	26	7.892e-05	Carbon
13	18	Ar	36	7.740e-05	Silicon, Oxygen
14	26	Fe	54	7.158e-05	e-process, Silicon
15	12	Mg	25	6.893e-05	Carbon
16	20	Ca	40	5.990e-05	Silicon, Oxygen
17	13	Al	27	5.798e-05	Carbon
18	28	Ni	58	4.915e-05	Silicon, e-process
19	6	C	13	3.683e-05	CNO
20	2	He	3	3.453e-05	Big Bang, pp
21	14	Si	29	3.448e-05	Carbon, Neon
22	11	Na	23	3.339e-05	Carbon
23	26	Fe	57	2.840e-05	e-process
24	14	Si	30	2.345e-05	Carbon, Neon
25	1	H	2	2.317e-05	Big Bang

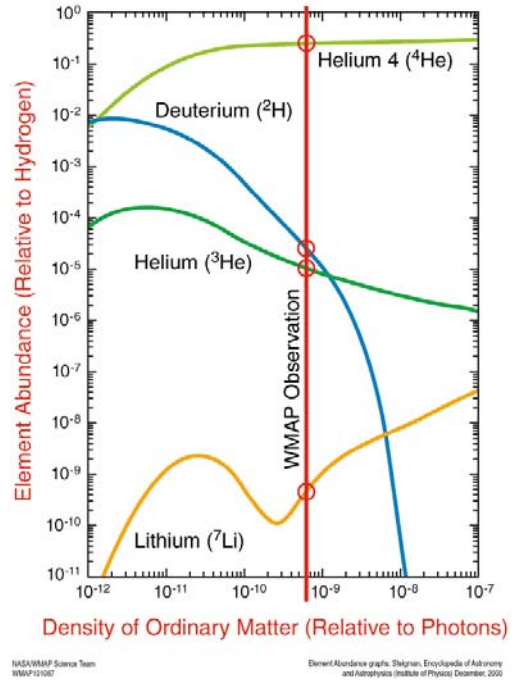
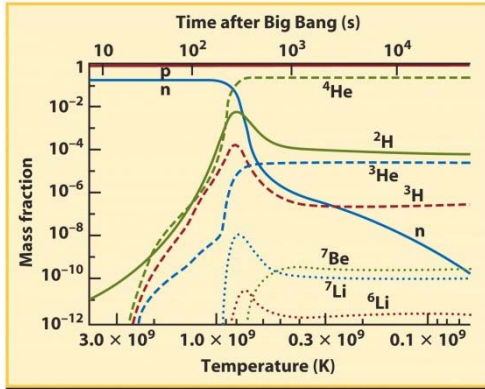
Arnett

https://en.wikipedia.org/wiki/R-process#/media/File:Nucleosynthesis_periodic_table.svg

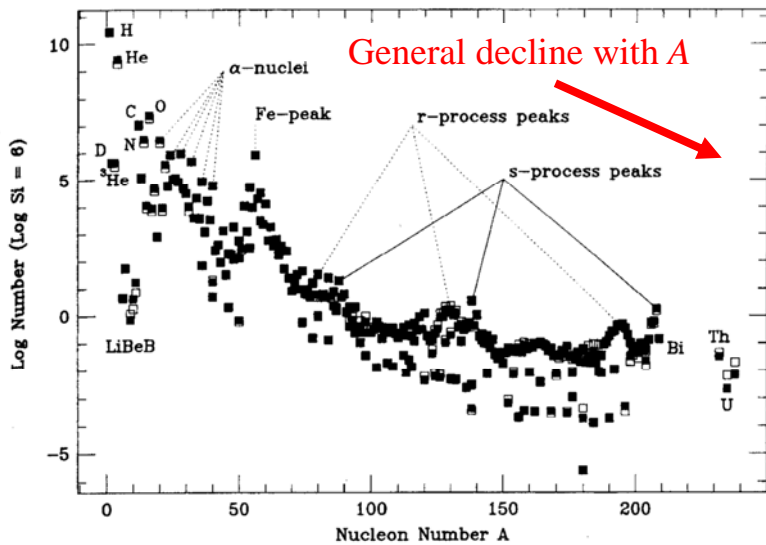
Prediction:

- ✓ $[^4\text{He}/\text{H}] \approx 0.25 \rightarrow$ obs OK
- ✓ $[\text{D}/\text{H}], [^4\text{He}/\text{H}], [^3\text{He}/\text{H}], [\text{Li}/\text{H}]$
density dependent \rightarrow obs all same densities

WMAP (CMB) obs \rightarrow consistent result



Solar System Abundances



General decline with A

$Z \uparrow$, Coulomb barrier
 $\uparrow \uparrow$ for charged particle reactions
 \rightarrow elements produced by neutron capture

Different symbols from different compilations

Arnett

Cosmic abundance and stellar/galaxy evolution (Burbidge, E. M., Burbidge, G. R., Fowler, W. A., & Hoyle, F. (1957)

Big Bang \rightarrow H:He=10:1

Stellar Interior

10^7 K \rightarrow p-p, CNO (fusing proton, in a proton rich or neutron poor gas) (**p process**)

10^8 K \rightarrow triple-alpha to C \rightarrow continue to fuse α particles
 \rightarrow mass number multiples of 4 by fusing (**α process**)

4×10^9 K \rightarrow nuclear equilibrium \rightarrow V, Cr, Mn and elements of the iron group (**e process**)

Explosive events

Neutron capture rapidly (compared to the competing β decays) \rightarrow neutron-rich isotopes (**r process**)
e, g., the radioactive elements ^{235}U , ^{238}U , at the expense of the iron group

Neutron capture slowly (compared to the competing β decays) \rightarrow neutron-rich isotopes (**s process**)

Valleys at $A=5$ to 15 (LiBeB) and $A \sim 45$ (Sc=scandium)

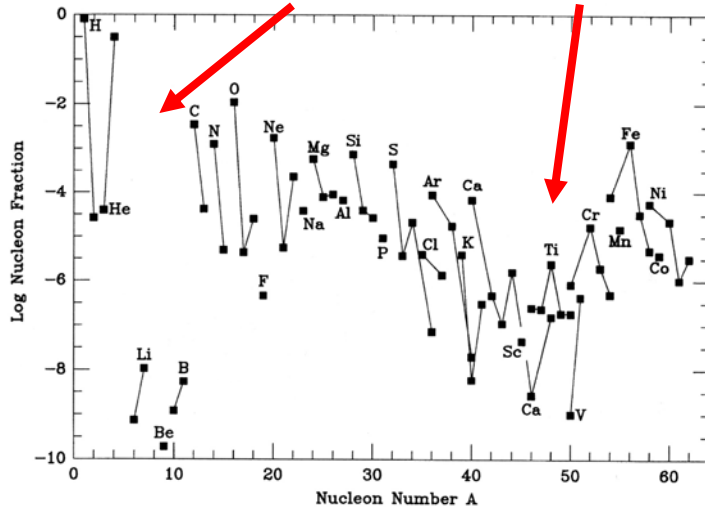


Fig. 2.2. Abundance ($A = 1, 64$)

Isotopes connected by lines.

Arnett

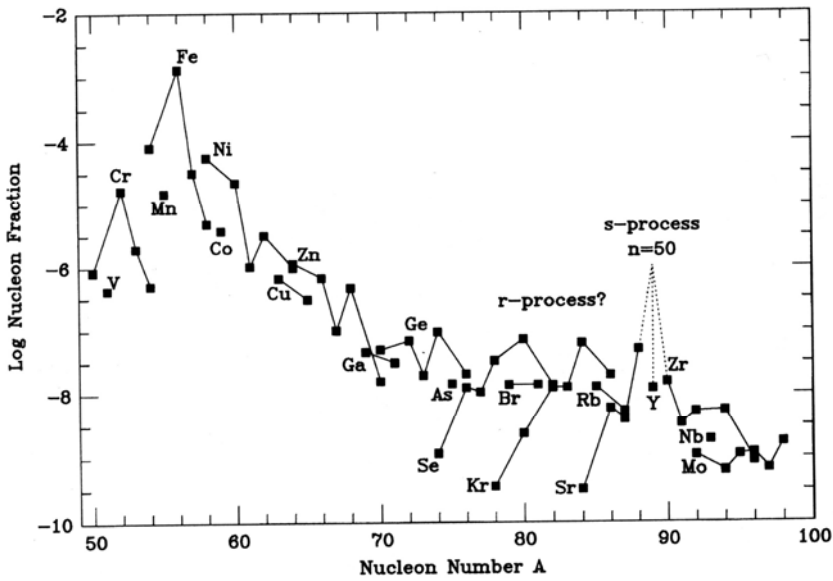


Fig. 2.3. Abundance ($A = 50, 100$)

- ◆ Other than H and He, the rest ('metals') is rare
 - ∴ penetration prob. between positively charged nuclei has an exponential dependence ($Z_1 Z_2$)
e.g., $O + O \rightarrow$ 64 times stronger than in $H + H$
- ◆ Even A nuclei are favored; especially for even-even elements, i.e., even Z and even N .
- ◆ $Z=N \rightarrow$ **α particle nuclei** e.g., ^{12}C , ^{16}O , ^{20}Ne , ^{24}Mg , ^{28}Si , ^{32}S , ^{36}Ar , ^{40}Ca
- ◆ First odd- A element is ^{25}Mg ; placed the 15th
- ◆ Among the top, only ^{14}N is not even-even.

- ◆ Nuclei, like atoms, have a shell structure;
 - "**magic numbers**" of protons are particularly tightly bound, e.g., ^4He ($Z=N=2$), ^{16}O ($Z=N=8$)
- ◆ ^{56}Fe not even-even; most tightly bound is ^{56}Ni .
SN I and II light curves provide evidence that $\text{Ni} \rightarrow \text{Co} \rightarrow \text{Fe}$
for $A=56 \rightarrow$ Abundance peaks at ^{56}Fe
- ◆ For $A > 60$, via neutron capture
 - ✓ **r-process**: rapid relative to beta-decay
 - ✓ **s-process**: slow *nuclei already tightly bound \rightarrow small cross section for neutron capture (slow compare to beta decays)*
(Burbidge, Burbidge, Fowler, & Hoyle; see Clayton)

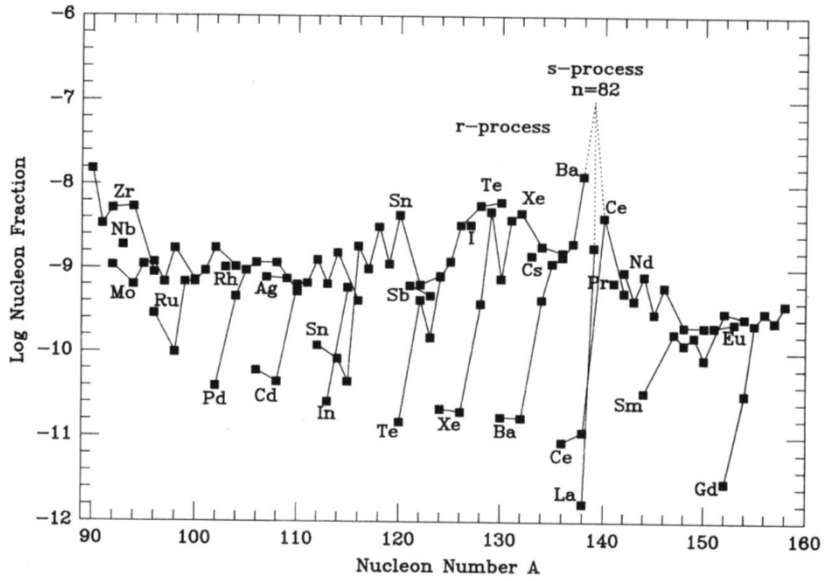


Fig. 2.4. Abundance ($A = 90, 160$)

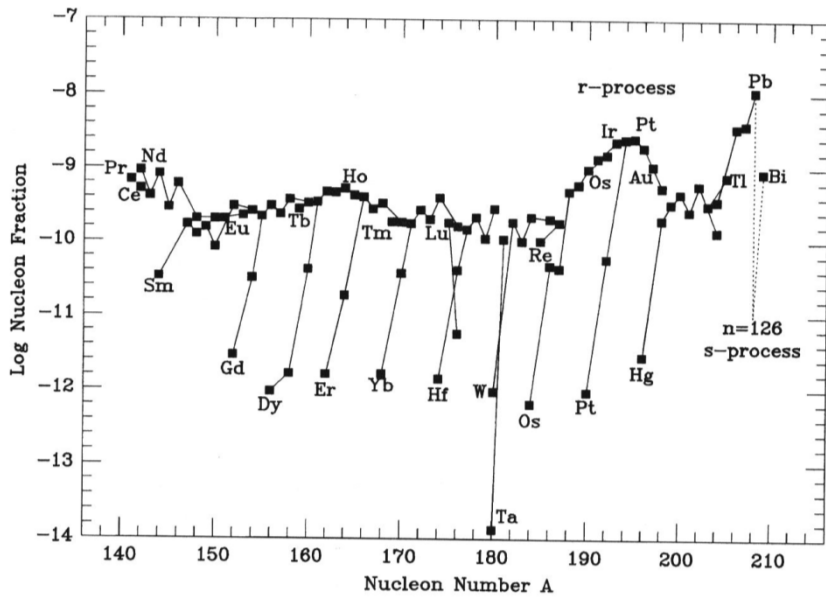
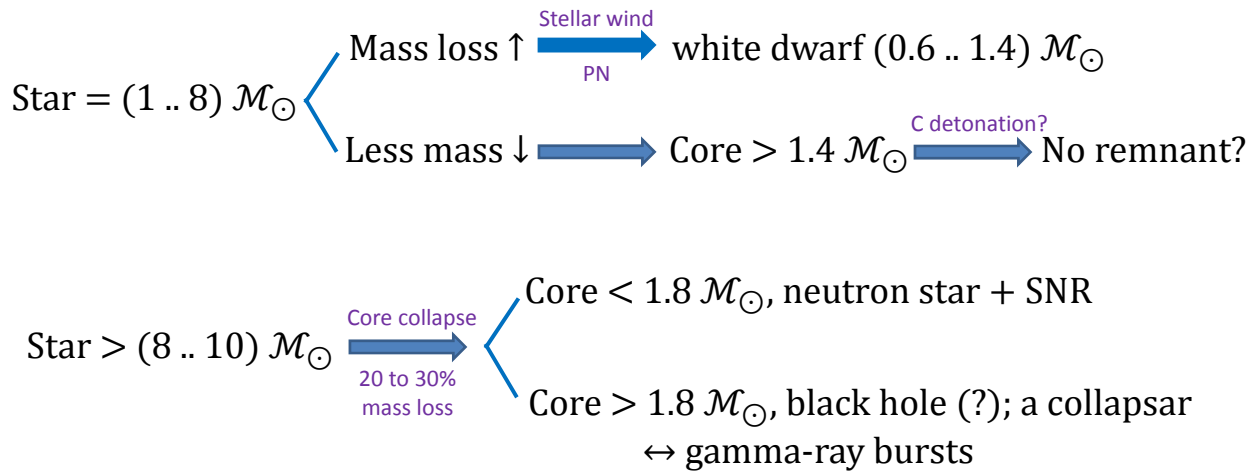


Fig. 2.5. Abundance ($A = 140, 210$)

Stellar Evolutionary Path



Black Holes predicted by General Relativity

Spacetime near a mass is warped

Total solar eclipse



A full treatment of a BH requires GR. But for an electrically neutral, non-rotating BH, classical derivations give the same results as with the relativistic approach.

$v_{\text{escape}} = \sqrt{\frac{2GM}{R}} = c$
 \therefore Too much mass in a volume.
 Schwarzschild radius
 $R_s = \frac{2GM}{c^2} \approx 3 \frac{M}{M_\odot} \text{ [km]}$
 $\therefore M \uparrow, R_{\text{BH}} \downarrow$
 Surface of R_s = Event Horizon for uncharged, non-rotating BHs
 Schwarzschild black hole

BH ($M=10^8$ sun), average density \sim water

	Nonrotating ($J=0$)	Rotating ($J>0$)
Uncharged ($Q=0$)	Schwarzschild	Kerr
Charged ($Q \neq 0$)	Reissner-Nordström	Kerr-Newman

General BH metric, with M, J and Q = Kerr-Newman metric.

The two physical relevant surfaces of a Kerr black hole.

Table 1.4
Compact Objects in the Solar Neighborhood^a

Object	Mass Range of Parent Star (M_{\odot})	Integrated Galactic Birth Rate (yr^{-1})	Number Density (pc^{-3})	$\frac{\rho}{\rho_T}$	$\langle d \rangle$ (pc)
White dwarfs	1–4	0.16	1.5×10^{-2}	0.070	2.5
Neutron stars	4–10	0.021	2.0×10^{-3}	0.020	4.9
Black holes	> 10	0.0085	8.0×10^{-4}	0.22	6.7

^aThese values are obtained from Eqs. (1.3.17)–(1.3.21).

Note: Nearest known white dwarf: Sirius B, 2.7 pc. Nearest known neutron star: PSR 1929 + 10, 50 pc. Nearest known black hole candidate: Cygnus X-1, ~ 2 kpc.

Size of the Universe

13.7 billion yrs

$$R_{\text{observable}} \sim 137 \times 10^8 \times 10^{13} \text{ km}$$

$$\sim 1.4 \times 10^{23} \text{ km}$$

$$M_{\text{obs}} \sim 10^{11} M_{\odot} / \text{gal} \cdot 10^{12} \text{ gal.} \left(\begin{array}{l} + \text{ dark} \\ \text{matter} \\ + \text{ dark energy} \end{array} \right)$$

$$\sim 10^{23} M_{\odot}$$

$$\left(R_S \sim 3 \frac{M}{M_{\odot}} [\text{km}] \right)$$

$$R_{\text{obs}} \sim R_S$$

The whole Universe is a BH!

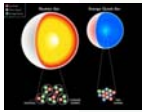
Hypernovae, Kilonovae

- Black-hole mergers
- White dwarf merger → Type I SN
- Neutron-star mergers → gravitational wave radiation → spiral inwards ; merging → a NS or a BH → a short GRB + a kilonovae + r-process elements produced and ejected
 a kilonova: luminosity 100 x of a classical nova
- Hypernova = superluminous supernova
 a hypernova: luminosity > 10 x of a standard

Quark Stars / Strange Stars

hypothetical type of stars composed of quark matter or strange matter

currently 6 "flavors" of quarks
 up, down, strange, charm, top, bottom
 spin 1/2



When a neutron star is further compressed
 neutrons → break down to up and down quarks → break down
 Strange quarks

dark matter candidates?

These highly mathematical & speculative

Some recent observations, e.g. in some SNe
 → existence of quark stars?

Magnetars

A neutron star w/ an extremely strong \vec{B}
 (10^{11} teslas or 10^{15} gauss)

Earth/Sun ~ 1 G
 Ap/Bp $\sim 10^3$ G
 WDs $\sim 10^6$ G
 NSs $\sim 10^{12}$ G

collapse → energy sources

i) $\dot{E}_{\text{grav}} \sim 0.2 \text{ Mc}^2 \sim 10^{53.8} \text{ erg/s}$

ii) $\dot{E}_{\text{rot}} \sim \frac{1}{2} I \Omega^2 \sim 10^{52.7} \text{ erg/s}$ $I_{45} \Omega_4^2$

\vec{B} links the fast spinning core to the outlying envelopes
 magnetic braking

$D \sim 20 \text{ km}$; spin : several times/s

Time spans short, $\lesssim 10^4 \text{ yr}$
 \vec{B} decays

